

Name: AKINTOMIDE AKINGBOLA

Matric number: 18/SCI01/013

1ii). Linear dependence of vectors occurs when the scalars in a linear combination are not all equal to zero.

i.e $\alpha_1u_1 + \alpha_2u_2 + \alpha_3u_3 + \dots + \alpha_nu_n = 0$

1iii). Linear combination of vectors is a mathematical method of combining vectors using addition and scalar multiplication.

i.e $\alpha_1v_1 + \alpha_2v_2 + \alpha_3v_3 + \dots + \alpha_mv_m$

2). $U\alpha + V\beta + W\gamma = (a, b, c)$

$$\begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix} \alpha + \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} \beta + \begin{bmatrix} 1 \\ 1 \\ -4 \end{bmatrix} \gamma = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

$$\alpha + 2\beta + \gamma = a \quad \dots \dots \dots \text{(i)}$$

$$\beta + \gamma = b \quad \dots \dots \dots \text{(ii)}$$

$$-\alpha + 3\beta - 4\gamma = c \quad \dots \dots \dots \text{(iii)}$$

From equ (ii)

$$\beta = b - \gamma \quad \dots \dots \dots \text{(iv)}$$

Put equ (iv) into (i) and (iii)

$$\alpha + 2(b - \gamma) + \gamma = a$$

$$\alpha + 2b - 2\gamma + \gamma = a$$

$$\alpha + 2b - \gamma = a$$

$$\alpha - \gamma = a - 2b \quad \dots \dots \dots \text{(v)}$$

For equ (iii)

$$-\alpha + 3(b - \gamma) - 4\gamma = c$$

$$-\alpha + 3b - 3\gamma - 4\gamma = c$$

$$-\alpha + 3b - 7\gamma = c$$

$$-\alpha - 7\gamma = c - 3b \dots\dots\dots(vi)$$

Compare equs (v) and (vi) by addition

$$\alpha - \gamma = a - 2b$$

$$-\alpha - 7\gamma = c - 3b$$

$$\underline{-8\gamma = a - 2b + c - 3b}$$

$$-8\gamma = a - 5b + c$$

$$\gamma = \frac{(a - 5b + c)}{-8}$$

$$\gamma = \frac{-(a - 5b + c)}{8}$$

$$\gamma = \frac{-a + 5b - c}{8}$$

Put γ in (ii)

$$\beta + \left[\frac{-a + 5b - c}{8} \right] = b$$

$$\beta = b - \left[\frac{-a + 5b - c}{8} \right]$$

$$\beta = b + \underline{a - 5b + c}$$

8

$$\beta = \underline{8b + a - 5b + c}$$

8

$$\beta = \underline{a + 3b + c}$$

8

Put β and γ into equ (i)

$$\alpha + 2 \left[\frac{a + 3b + c}{8} \right] + \left[\frac{-a + 5b - c}{8} \right] = a$$

$$\alpha + \left[\frac{a + 3b + c}{4} \right] + \left[\frac{-a + 5b - c}{8} \right] = a$$

$$\alpha = a - \left[\frac{a + 3b + c}{4} \right] - \left[\frac{-a + 5b - c}{8} \right]$$

$$\alpha = a - \underline{a - 3b - c} + \underline{a - 5b + c}$$

4 8

$$\alpha = \underline{8a + 2(-a - 3b - c) + a - 5b + c}$$

8

$$\alpha = \underline{8a - 2a - 6b - 2c + a - 5b + c}$$

8

$$\alpha = \underline{7a - 11b - c}$$

8

$$\left[\frac{7a - 11b - c}{8} \right]U + \left[\frac{a + 3b + c}{8} \right]V + \left[\frac{-a + 5b - c}{8} \right]W$$

3). – Commutativity of vector addition

- Associativity of vector addition
- Identity element of addition
- Inverse element of addition