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 Course: Math 104

Assignment MATH 104

Answers

Differentiation

$$1) y = (x+1)^2 (x-2)^{1/2} (2x-1) (x-3)^{4/3}$$

$$\ln y = \ln[(x+1)^2] + \ln[(x-2)^{1/2}] - \ln(2x-1) - \ln[(x-3)^{4/3}]$$

$$\frac{1}{y} \frac{dy}{dx} = \frac{1}{(x+1)^2} (2x+2) + \frac{1}{(x-2)^{1/2}}$$

$$\frac{-1}{(2x-1)} - \frac{1}{(x-3)^{4/3}} \frac{4}{3} (x-3)^{1/3}$$

$$\frac{1}{y} \frac{dy}{dx} = \frac{2x+2}{(x+1)^2} + \frac{1}{2} \frac{(x-2)^{-1/2}}{(x-2)^{1/2}} - \frac{2}{2x-1}$$

$$- \frac{4}{3} \frac{(x-3)^{1/3}}{(x-3)^{4/3}}$$

$$\frac{1}{y} = y \left[ \frac{2}{(x+1)} + \frac{1}{2} - \frac{2}{2x-1} - \frac{4}{3} \frac{(x-3)^{1/3}}{(x-3)^{4/3}} \right]$$

$$\frac{dy}{dx} = y \frac{(x+1)^2 (x-2)^{1/2}}{(2x-1) (x-3)^{4/3}} \left[ \frac{2}{(x+1)} + \frac{1}{2} - \frac{2}{(2x-1)} - \frac{4}{3} \right]$$

$$(x-3)^{1/3}$$

$$(x-3)^{4/3}$$

(2)

$$2) y = \frac{3e^k \sin 2k}{k^{5/2}}$$

$$\ln y = \ln(3e^k) + \ln(\sin 2k) - \ln(k^{5/2})$$

$$\frac{1}{y} \frac{dy}{dk} = \frac{1}{3e^k} \cdot 3e^k + \frac{1}{\sin 2k} \cdot 2 \cos 2k - \frac{1}{k^{5/2}} \cdot 5k^{3/2}$$

$$\frac{1}{y} \frac{dy}{dk} = 1 + \frac{2 \cos 2k}{\sin 2k} - \frac{5k^{3/2}}{2k^{5/2}}$$

$$\frac{1}{y} \frac{dy}{dk} = 1 + 2 \tan 2k - \frac{5k^{3/2}}{2k^{5/2}}$$

$$\frac{dy}{dk} = \frac{3e^k \sin 2k}{k^{5/2}} \left[ 1 + 2 \tan 2k - \frac{5k^{3/2}}{2k^{5/2}} \right]$$

Integration

$$1) \int 4 \sec^2(3m+1)$$

$$\text{let } u = 3m+1$$

$$du = 3 \quad \leftarrow \quad dx = du$$

$$dm$$

$$= \int 4 \sec^2 u \cdot \frac{du}{3} = \frac{1}{3} \int 4 \sec^2 u \cdot du$$

$$\Rightarrow \frac{1}{3} [4 \tan u + c] = \frac{4 \tan u + c}{3}$$

$$\Rightarrow \frac{4 \tan(3m+1) + c}{3}$$

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$$2.) \int 2t(3t^2-1)^{1/2} dt$$

$$\text{let } u = 3t^2 - 1$$

$$du = 6t \quad \therefore dt = \frac{du}{6t}$$

$$\Rightarrow \int 2t u^{1/2} \frac{du}{6t} = \int u^{1/2} \frac{du}{3}$$

$$\frac{1}{3} \int u^{1/2} du \Rightarrow \frac{1}{3} \left[ \frac{u^{3/2}}{3/2} + c \right]$$

$$\Rightarrow \frac{2u^{3/2}}{9} + c$$

$$3.) \int \frac{2x}{(4x^2-1)^{1/2}} dx$$

$$\text{let } u = 4x^2 - 1$$

$$du = 8x \quad \therefore dx = \frac{du}{8x}$$

$$\Rightarrow \int \frac{2x}{u^{1/2}} dx = \int \frac{2x}{u^{1/2}} \frac{du}{8x}$$

$$= \frac{1}{4} \int u^{-1/2} du = \frac{1}{4} \left[ \frac{u^{1/2}}{1/2} + c \right]$$

$$= u^{1/2} + c \Rightarrow (4x^2 - 1)^{1/2} + c$$

$$\text{OR } \frac{\sqrt{4x^2-1}}{2} + c$$