

$$2) \quad 3y - 4 = 2x + 3$$

$$y - 5 = x + 6$$

$$3y - 4 = 2x + 3 \dots \text{eqn 1}$$

Make y subject formula

$$3y = 2x + 3 + 4$$

divide through by 3

$$y = \frac{2x}{3} + \frac{7}{3}$$

Recall $y = mx + c$

$$m_1 = \frac{2}{3}$$

$$y - 5 = x + 6$$

make y subject formula

$$y = x + 6 + 5$$

$$y = x + 11$$

Recall $y = mx + c$

$$m = 1$$

$m_1, m_2 = -1$ (for perpendicularity)

$$m_1 \times m_2 = \frac{2}{3} \times 1$$

$$= \frac{2}{3}$$

∴ therefore line $3y - 4 = 2x + 3$
and $y - 5 = x + 6$ are not
perpendicular

3) find the equation of the tangent
and normal to the curve $x^2 + y^2 + 3xy - 11 = 0$
at the point $x = 1$
 $y = 2$

Solution

$$x^2 + y^2 + 3xy - 11 = 0 \quad (x=1, y=2)$$

$$m = \frac{dy}{dx}$$

$$x^2 + y^2 + 3xy - 11 = 0$$

$$\frac{dy}{dx}$$

$$2x + 2y \frac{dy}{dx} + 3\left(x - \frac{dy}{dx} + y\right) = 0$$

$$2x + 2y \frac{dy}{dx} + 3\left(x - \frac{dy}{dx} + y\right) = 0$$

$$2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$m = \frac{dy}{dx} = \frac{-2(1) - 3(2)}{2(2) + 3(1)}$$

$$\frac{-2 - 6}{4 + 3} = \frac{8}{7}$$

$$m = \frac{8}{7}$$

~~7~~