

~~NAME~~  
AISE TENIOLA PRECIOUS

MBBS

MHS

19/MHS01/069

ASSIGNMENT

Examine whether or not these pair of lines are perpendicular to each other.

1)  ~~$y = 3x - 2 = 0$~~  and  $3y + x + 9$

2)  $3y - 4 = 2x + 3$  and  $y - 5 = x + 6$

1.)  $y - 3x - 2 = 0$

$3y + x + 9 = 0$

Lines to be perpendicular then  ~~$m_1 m_2 = -1$~~   $m_1 m_2 = 1$

$y - 3x - 2 = 0$

Making  $y$  the subject of the formula

$y = 3x + 2$

By comparing with  $y = mx + c$

$m_1 = 3$

$3y + x + 9 = 0$  Making  $y$  the subject of formula

$3y = -x - 9$

$y = \frac{-x}{3} - \frac{9}{3}$

$y = \frac{-1}{3}x - 3$

$y = mx + c$   $m_2 = -1/3$

$$1.) y - 3x - 2 = 0$$

$$3y + x + 9 = 0$$

Lines to be perpendicular then  ~~$m_1 m_2 = -1$~~   $m_1 m_2 = 1$

$$y - 3x - 2 = 0$$

Making  $y$  the subject of the formula

$$y = 3x + 2$$

By comparing with  $y = mx + c$

$$m_1 = 3$$

$3y + x + 9 = 0$  Making  $y$  the subject of formula

$$3y = -x - 9$$

$$y = \frac{-x}{3} - \frac{9}{3}$$

$$y = \frac{-1}{3}x - 3$$

$$= mx + c \quad m_2 = -\frac{1}{3}$$

$m_1 m_2 = 1$ : for perpendicularity

$3 \times \frac{1}{3} = -1$  Since  $m_1 m_2 = -1$  hence the lines  $y - 3x - 2 = 0$  and  $3y + x + 9 = 0$  ARE

... of formula in 2.

$$y - 5 = x + 6$$

$$y = x + 6 + 5$$

$$y = x + 11$$

Comparing with  $y = mx + c$

$$m_2 = 1$$

For the lines to be perpendicular

$$m_1 m_2 = -1$$

$$m_1 m_2 = \frac{2}{3} \times 1 = \frac{2}{3}$$

$$m_2 \neq -1$$

∴ the lines  $3y - 4 = 2x + 3$  and  $y - 5 = x + 6$  are NOT PERPENDICULAR

$$2) \begin{aligned} 3y - 4 &= 2x + 3 \\ y - 5 &= x + 6 \end{aligned}$$

Making  $y$  the subject of formula in 1

$$3y = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2x}{3} + \frac{7}{3}$$

By comparing with  $y = mx + c$   
 $m_1 = \frac{2}{3}$

Making  $y$  the subject of formula in 2.

$$y - 5 = x + 6$$

$$y = x + 6 + 5$$

$$y = x + 11$$

By comparing with  $y = mx + c$   
 $m_2 = 1$

For the lines to be perpendicular

$$m_1 m_2 = -1$$

$$m_1 m_2 = \frac{2}{3} \times 1 = \frac{2}{3}$$

$$m_1 m_2 \neq -1$$

hence the lines  $3y - 4 = 2x + 3$  and  $y - 5 = x + 6$  are NOT perpendicular

$$x^2 + y^2 + 3xy - 11 = 0 \quad (x=1, y=2)$$

$$m = \frac{dy}{dx}$$

$$x^2 + y^2 + 3xy - 11 = 0$$

$$\frac{dy}{dx}$$

$$2x + 2y \frac{dy}{dx} + 3(x \cdot \frac{dy}{dx} + y \cdot 1) = 0$$

$$2x + 2y \frac{dy}{dx} + 3(x \cdot \frac{dy}{dx} + y) = 0$$

$$2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$= \frac{dy}{dx} \Big|_{x=1, y=2} = \frac{-2(1) - 3(2)}{2(2) + 3(1)} = \frac{-2 - 6}{4 + 3} = \frac{-8}{7}$$

Equation of tangent

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-8}{7} (x - 1)$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$m = \left. \frac{dy}{dx} \right|_{x=1, y=2} = \frac{-2(1) - 3(2)}{2(2) + 3(1)} = \frac{-2 - 6}{4 + 3} = \frac{-8}{7}$$

Equation of tangent

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-8}{7} (x - 1)$$

$$7(y - 2) = -8(x - 1)$$

$$7y - 14 = -8x + 8$$

$$7y + 8x - 14 - 8 = 0$$

$7y + 8x - 22 = 0$  is the equation of tangent

Equation of normal

$$-y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 2 = \frac{-1}{-8/7} (x - 1)$$

$$-2 = \frac{7}{8} (x - 1)$$

$$8(y - 2) = 7(x - 1)$$

$$8y - 16 = 7x - 7$$

$8y - 7x - 16 + 7 = 0$ ,  $8y - 7x - 9 = 0$  is the equation of normal.