

Maths Assignment
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1) $y - 3x - 2 = 0$ & $3y + x + 9 = 0$

Solution

$$y - 3x - 2 = 0 \quad \dots \textcircled{1}$$

$$y = 3x + 2$$

$$\therefore y = mx + c$$

$$\therefore m_1 = 3$$

$$3y + x + 9 = 0 \quad \dots \textcircled{2}$$

$$3y = -x - 9$$

$$y = \frac{-x}{3} - \frac{9}{3}$$

$$y = -\frac{1}{3}x - 3$$

$$y \equiv y = mx + c$$

$$m = -\frac{1}{3}$$

$\therefore m_1, m_2 = -1$ [Prove it is perpendicular]

$$3 \times -\frac{1}{3} = -1$$
 [It is perpendicular]

2) $3y - 4 = 2x + 3 \quad \dots \textcircled{1}$

$$3y = 2x + 3 + 4$$

$$y = \frac{2x + 7}{3}$$

$$\therefore y = \frac{2}{3}x + \frac{7}{3} \quad \therefore y = mx + c$$

$$\therefore m_1 = \frac{2}{3}$$

$$y - 5 = x + 6$$

$$y = x + 6 + 5$$

$$y = x + 11 \quad \therefore y = mx + c$$

$$m_2 = 1$$

$\therefore m_1, m_2 \neq -1$; $\frac{2}{3} \times 1 = \frac{2}{3}$ [It is not perpendicular]

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3) $x^2 + y^2 + 3xy - 11 = 0$ at the point $x=1, y=2$

$$\frac{dy}{dx} = 2x + 2y \frac{dy}{dx} + 3(x \frac{dy}{dx} + y) = 0 \Rightarrow 0 = 0$$

$$\frac{dy}{dx} = 2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$\frac{dy}{dx} = 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 2 - 3y - 2x$$

$$\frac{dy}{dx} (1 - 2y - 3x) = 2 - 3y - 2x$$

$$\frac{dy}{dx} = \frac{2 - 3y - 2x}{-2y - 3x}$$

at the point $x=1, y=2$

~~$\frac{dy}{dx}$~~

$$m = \frac{dy}{dx} \Big|_{x=1, y=2} = \frac{2 - 3(2) - 2(1)}{-2(2) - 3(1)} = \frac{-6 - 2}{-4 - 3}$$

$$m = \frac{-8}{-7} = \frac{8}{7}$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{8}{7}(x - 1)$$

$$7(y - 2) = 8(x - 1)$$

$$7y - 14 = 8x - 8$$

$$7y + 8x - 22 = 0 \Rightarrow \text{Equation of tangent}$$

$$b) m = \frac{11}{-8/7}$$

$$m = 7/8$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8(y - 2) = 7(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y - 7x - 9 = 0 \Rightarrow \text{Equation of normal}$$