

19/MHS01/853

making y subject of formula in 2.

$$y - 5 = x + 6$$

$$y = x + 11$$

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By comparing with $y = mx + c$

$$\therefore m_1, m_2 = -1$$

$$m_1, m_2 = \frac{2}{3} \times 1 = \frac{2}{3}$$

$$m_1, m_2 = -1$$

\therefore the lines $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ are not perpendicular.

3) $x^2 + y^2 + 3xy - 11 = 0$ ($x=1, y=2$)

$$m = \frac{dy}{dx}$$

$$x^2 + y^2 + 3xy - 11 = 0$$

$$\frac{dy}{dx}$$

$$2x + 2y \frac{dy}{dx} + 3(x \frac{dy}{dx} + y) = 0$$

$$2x + 2y \frac{dy}{dx} + 3(x \frac{dy}{dx} + y) = 0$$

$$2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$m = \frac{dy}{dx} \Big|_{x=1, y=2}$$

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$$= \frac{-2(1) - 3(2)}{2(2) + 3(1)} = \frac{-2-6}{4+6} = \frac{-8}{10} = -\frac{4}{5}$$

1) Equation of tangent

$$y - y_1 = m(x - x_1)$$
$$y - 2 = -\frac{8}{7}(x - 1)$$

$$7(y - 2) = -8(x - 1)$$

$$7y - 14 = -8x + 8$$

$$8x + 7y - 14 - 8 = 0$$

$\rightarrow 8x + 7y - 22 = 0$ is the equation of tangent

2) Equation of normal

$$y - y_1 = \frac{1}{m}(x - x_1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8(y - 2) = 7(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y - 7x - 16 + 7 = 0$$

$$8y - 7x - 9 = 0$$

is the equation of normal.

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1) $y - 3x - 2 = 0$ and $3y + x + 9 = 0$
let $A = y - 3x - 2 = 0$
 $\frac{dy}{dx} - 3 = 0 = 0$

$$\frac{dy}{dx} - 3 = 0$$

$$\frac{dy}{dx} = 3$$

let $B = 3y + x + 9 = 0$

$$3 \frac{dy}{dx} + 1 = 0$$

$$3 \frac{dy}{dx} + 1 = 0$$

$$\frac{dy}{dx} = -\frac{1}{3}$$

A+B

i.e. $y - 3x - 2 = 0$ is perpendicular to $3y + x + 9 = 0$

2) $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ (2)

$$y - 5 = x + 6 \quad (2)$$

making y the subject of formula in 1

$$3y = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2x}{3} + \frac{7}{3}$$

$$y = mx + c$$

$$m_1 = \frac{2}{3}$$