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MATRIC NO: 19/MHSC01/107

SERIAL NO: 025

DEPARTMENT: MEDICINE AND SURGERY

MAT 104 ASSIGNMENT.

1. $y - 3x - 2 = 0$ and $3y + x + 9 = 0$.

Solution

Taking the first equation $y - 3x - 2 = 0$;

Equation of a straight line; $y = mx + c$.

The two are then compared.

$$y - 3x - 2 = 0 = y = 3x + 2$$

$$y = 3x + 2; m_1 = 3.$$

Taking the second equation $3y + x + 9 = 0$

Equation of a straight line; $y = mx + c$.

Comparing the two;

$$3y + x + 9 = 0;$$

$$3y = -x - 9$$

$$y = \frac{-x - 9}{3}$$

$$y = \frac{-x}{3} - 3; m_2 = -\frac{1}{3}.$$

For two lines to be perpendicular; $m_1 m_2 = -1$

$$m_1 = 3 \quad m_2 = -\frac{1}{3}$$

$$3 \times -\frac{1}{3} = -1.$$

\therefore The two lines $3y + x + 9 = 0$ and $y - 3x - 2 = 0$ are perpendicular to each other.

2) $3y - 4 = 2x + 3$ and $y - 5 = x + 6$.

Taking the first equation $3y - 4 = 2x + 3$

Equation of a straight line; $y = mx + c$.

Comparing the two;

$$3y = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2x + 7}{3}$$

$$M_1 = \frac{2}{3}$$

Taking the second equation $y - 5 = x + 6$

Comparing to equation of a straight line $y = mx + c$,

$$y = x + 6 + 5$$

$$y = x + 11$$

$$M_2 = 1$$

For two lines to be perpendicular; $M_1 M_2 = -1$

$$\frac{1}{3} \times \frac{2}{3} = \frac{2}{9}$$

\therefore The two lines $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ are not perpendicular to each other.

3) $x^2 + y^2 + 3xy - 11 = 0$ at point $x = 1, y = 2$.

Solution

$$\frac{dy}{dx} = 2x + 2y \cdot \frac{dy}{dx} + 3(x \cdot \frac{dy}{dx} + y \cdot 1) = 0$$

$$\frac{dy}{dx} = 2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$\frac{dy}{dx} (2y + 3x) = -3y - 2x$$

$$\frac{dy}{dx} = \frac{-3y - 2x}{2y + 3x}$$

$$\frac{dy}{dx} \Big|_{x=1, y=2} = \frac{-3(2) - 2(1)}{2(2) + 3(1)}$$

$$\frac{dy}{dx} \Big|_{x=1, y=2} = \frac{-8}{7} = M_1$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-8}{7}(x - 1)$$

$$7y - 14 = -8x + 8$$

$$7y - 14 + 8x - 8 = 0$$

$7y + 8x - 22 = 0$ which gives the equation of the tangent.

$$M_1 M_2 = -1$$

$$M_2 = -1 / -8/7 = 7/8$$

Equation of the normal -

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y - 16 + 7 - 7x = 0$$

$8y - 9 - 7x = 0$ which gives the equation of the normal.