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19/MHSOI/358.

MEDICINE AND SURGERY.

MATH 104 ASSIGNMENT.

Examine whether or not these pair of lines are perpendicular to each other.

1. $y - 3x - 2 = 0$ and $3y + x + 9 = 0$

for the lines to be perpendicular then $m_1 m_2 = -1$

$$y - 3x - 2 = 0$$

Making y the subject of the formula.

$$y = 3x + 2$$

$$y = 3x + 2$$

By comparison with $y = mx + c$

$$m_1 = 3$$

$$3y + x + 9 = 0$$

Making y the subject of formula.

$$3y = -x - 9$$

$$y = \frac{-x}{3} - \frac{9}{3}$$

$$y = \frac{-1x}{3} - 3$$

$$y = mx + c \quad \text{and} \quad m_2 = -1/3$$

$$m_1 m_2 = 3 \times -1/3 = -1$$

Since $m_1 m_2 = -1$ then the lines $y - 3x - 2 = 0$ and $3y + x + 9 = 0$ are perpendicular.

2. $3y - 4 = 2x + 3$ and $y - 5 = x + 6$

Let $3y - 4 = 2x + 3$ ———— (1)

and $y - 5 = x + 6$ ———— (2)

Making y the subject of formula in 1

$$3y = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2x}{3} + \frac{7}{3}$$

By comparing with $y = mx + c$, then $m_1 = \frac{2}{3}$

For equation (2)

Making y the subject of formula,

$$y = x + 6 + 5$$

$$y = x + 11$$

By comparing with $y = mx + c$ then, $m_2 = 1$

But for the lines to be perpendicular,

$$m_1 m_2 = -1$$

~~$$m_1 m_2 = 2 \times 3 \times 1 + 11$$~~

But $m_1 m_2 = \frac{2}{3} \times 1 = \frac{2}{3}$

Therefore $m_1 m_2 \neq -1$

Hence the lines $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ are

NOT PERPENDICULAR

$$3. \quad x^2 + y^2 + 3xy - 11 = 0 \quad \text{at the point } x=1 \text{ and } y=2$$

$$= 2x + 2y \frac{dy}{dx} + 3 \left[x \frac{dy}{dx} + y \right] - 0 = 0$$

$$= 2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$= 2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

m at the point $x=1$ and $y=2$

$$m = \frac{dy}{dx} \Big|_{x=1, y=2} = \frac{-2(1) - 3(2)}{2(2) + 3(1)} = \frac{-2-6}{4+3}$$

$$m = \frac{-8}{7} \quad \text{or} \quad -1 \frac{1}{2}$$

$$a) \quad y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-8}{7} (x - 1)$$

~~$$7(y - 2) = -8(x - 1)$$~~

~~$$7y - 14 = -8x + 8$$~~

~~$$7y$$~~

$$7(y - 2) = -8(x - 1)$$

$$7y - 14 = -8x + 8$$

$$7y + 8x = 14 - 8 = 0$$

$$7y + 8x - 22 = 0 \quad \text{[Equation of tangent]}$$

b) Equation of normal,

$$m = \frac{-1}{-8/7} = +1 \times \frac{7}{+8}$$

$$m = \frac{7}{8}$$

$$y - y_1 = \frac{7}{8}(x - x_1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8(y - 2) = 7(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y - 7x - 16 + 7 = 0$$

$$8y - 7x - 9 = 0 \text{ (Equation of normal)}$$