

**AKUKWE MICHAEL LOTACHUKWU**

**18/SCI01/014**

**COMPUTER SCIENCE**

**MAT 204**

**QUESTION 1**

i). Linear dependence of vectors occurs when the scalars in a linear combination are not all equal to zero.

$$\text{i.e } \alpha_1 u_1 + \alpha_2 u_2 + \alpha_3 u_3 + \dots + \alpha_n u_n = 0$$

ii). Linear combination of vectors is a mathematical method of combining vectors using addition and scalar multiplication.

$$\text{i.e } \alpha_1 v_1 + \alpha_2 v_2 + \alpha_3 v_3 + \dots + \alpha_m u_m$$

**QUESTION 2**

$$U\alpha + V\beta + W\gamma = (a, b, c)$$

$$\begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix} \alpha + \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} \beta + \begin{bmatrix} 1 \\ 1 \\ -4 \end{bmatrix} \gamma = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

$$\alpha + 2\beta + \gamma = a \dots\dots\dots(i)$$

$$\beta + \gamma = b \dots\dots\dots(ii)$$

$$-\alpha + 3\beta - 4\gamma = c \dots\dots\dots(iii)$$

From equ (ii)

$$\beta = b - \gamma \dots\dots\dots(iv)$$

Put equ (iv) into (i) and (iii)

$$\alpha + 2(b - \gamma) + \gamma = a$$

$$\alpha + 2b - 2\gamma + \gamma = a$$

$$\alpha + 2b - \gamma = a$$

$$\alpha - \gamma = a - 2b \dots\dots(v)$$

For equ (iii)

$$-\alpha + 3(b - \gamma) - 4\gamma = c$$

$$-\alpha + 3b - 3\gamma - 4\gamma = c$$

$$-\alpha + 3b - 7\gamma = c$$

$$-\alpha - 7\gamma = c - 3b \dots\dots\dots(vi)$$

Compare equs (v) and (vi) by addition

$$\alpha - \gamma = a - 2b$$

$$-\alpha - 7\gamma = c - 3b$$

---

$$-8\gamma = a - 2b + c - 3b$$

$$-8\gamma = a - 5b + c$$

$$\gamma = \frac{(a - 5b + c)}{-8}$$

$$\gamma = -\frac{(a - 5b + c)}{8}$$

$$\gamma = \frac{-a + 5b - c}{8}$$

Put  $\gamma$  in (ii)

$$\beta + \left( \frac{-a + 5b - c}{8} \right) = b$$
$$\left( \quad \quad \quad \right)$$

$$\beta = b - \frac{-a + 5b - c}{8}$$

$$\beta = b + \frac{a - 5b + c}{8}$$

$$\beta = \frac{8b + a - 5b + c}{8}$$

$$\beta = \frac{a + 3b + c}{8}$$

Put  $\beta$  and  $\gamma$  into equ (i)

$$\alpha + 2 \left( \frac{a + 3b + c}{8} \right) + \left( \frac{-a + 5b - c}{8} \right) = a$$

$$\alpha + \left( \frac{a + 3b + c}{4} \right) + \left( \frac{-a + 5b - c}{8} \right) = a$$

$$\alpha = a - \left( \frac{a + 3b + c}{4} \right) - \left( \frac{-a + 5b - c}{8} \right)$$

$$\alpha = a - \frac{a - 3b - c}{4} + \frac{a - 5b + c}{8}$$

$$\alpha = \frac{8a + 2(-a - 3b - c) + a - 5b + c}{8}$$

$$\alpha = \frac{8a - 2a - 6b - 2c + a - 5b + c}{8}$$

$$\alpha = \frac{7a - 11b - c}{8}$$

$$\left(\frac{7a - 11b - c}{8}\right)U + \left(\frac{a + 3b + c}{8}\right)V + \left(\frac{-a + 5b - c}{8}\right)W$$

### QUESTION 3

- a. Commutativity of vector addition
- b. Associativity of vector addition
- c. Identity element of addition
- d. Inverse element of addition