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17/EXC07/007

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Q.C.T.

In order to avoid pressure build up gas at atmospheric pressure in a pipe is vented to atmosphere through a pipe of 3mm diameter and 20m length. Determine the mass of the gas diffusing out and mass of air diffusing in per hour. Assume $D = 0.28 \times 10^{-4} \text{ m}^2/\text{s}$, $M = 17 \text{ kg/kgmol}$

Solution:

$$M_a = \frac{M_a}{M} \quad \dots \quad \text{eq } ①$$

$$P_{a_1} = 1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2$$

$$P_{a_2} = 0 \text{ (gas vented to atmosphere)}$$

$$L = 20 \text{ m}$$

$$d = 3 \text{ mm} = 0.003 \text{ m}$$

$$A = \pi/4 (d^2) = \pi/4 \times (0.003)^2 = 7.0695 \times 10^{-6} \text{ m}^2$$

$$\text{Molar mass, } M = 17 \text{ kg/mol}$$

$$R = 8315 \text{ J/kgmol K}$$

$$D = 0.28 \times 10^{-4} \text{ m}^2/\text{s}$$

Using the equimolar counter diffusion equation

$$\frac{M_a}{A} = \frac{D}{R_T} \cdot \frac{P_{a_1} - P_{a_2}}{L}$$

$$\frac{M_a}{A} = \frac{\Delta A}{R_T} \cdot \frac{P_{a_1} - P_{a_2}}{L}$$

Recall $\frac{1}{T} = \frac{1}{T_1} + \frac{1}{T_2}$

$$\frac{M_a}{A} = \frac{\Delta A}{R_T} \cdot \frac{P_{a_1} - P_{a_2}}{L}$$

$$\text{Substituting Eq 1}$$

$$\frac{M_a}{m} = \frac{\Delta A}{R} \cdot \frac{P_{a_1} - P_{a_2}}{L}$$

$$M_a = \frac{\Delta A}{R} \cdot \frac{P_{a_1} - P_{a_2}}{L} \cdot M$$

where M_a is the mass of gas diffusing out in kg/s to convert

$$M_a = \frac{\Delta A}{R} \cdot \frac{P_{a_1} - P_{a_2}}{L} \cdot m(3000) \dots \text{kg/hr}$$

$$M_a = \frac{(0.28 \times 10^{-4}) \times (7.0693 \times 10^{-6})}{8315} \cdot \frac{(1.013 \times 10^5 - 0) \times 7 \times 3000}{20}$$

$$= 7.38 \times 10^{-6} \text{ kg/hr}$$

b) Mass of air diffusing in, M_{air}

$$\frac{N_a}{A} = -\frac{N_b}{A}$$

$$\therefore N_a = -N_b$$

$$N_b = -N_a$$

$$= -7.38 \times 10^{-6}$$

$$\text{mole of air} = \frac{-7.38 \times 10^{-6}}{17}$$

$$= -4.34 \times 10^{-7}$$

$$\text{Mass of Air} = -4.34 \times 10^{-7} \times 28.97$$

$$= -1.26 \times 10^{-5} \text{ kg/hr.}$$