

MAT 102

$A = 2i - j, B = 3i + j - 11k$  and  $C = 4i + 4j - 5k$

1)  $-3A + 7B - 8C$

$$\Rightarrow -3A = -3(2i - j) \\ = -6i + 3j$$

$$7B = 7(3i + j - 11k)$$

$$21i + 7j - 77k$$

$$+ 8C = +8(4i + 4j - 5k)$$

$$= +32i + 32j - 40k$$

$$\therefore -3A + 7B - 8C = (-6i + 3j) + (21i + 7j - 77k) - (32i + 32j - 40k) \\ (15i + 10j - 77k) - (32i + 32j - 40k) \\ = (-17i - 22j - 37k)$$

2) if  $k = 2A + 4B - C$ , find the direction cosine of  $k$

$$\Rightarrow 2A = 2(2i - j) \\ = (4i - 2j)$$

$$4B = 4(3i + j - 11k) \\ = (12i + 4j - 44k)$$

$$\therefore 2A + 4B - C = (4i - 2j) + (12i + 4j - 44k) - (4i + 4j - 5k) \\ = (16i + 2j - 44k) - (4i + 4j - 5k)$$

$$k = (12i - 2j - 39k)$$

$$\text{Magnitude of } k = \sqrt{12^2 + (-2)^2 + (-39)^2} \\ = \sqrt{1539} \approx 39$$

$$\cos \alpha = \frac{12}{39}$$

$$\cos \beta = \frac{-2}{39}$$

$$\cos \gamma = \frac{-39}{39}$$

3)  $A \times (B \times C)$

$$\therefore (2i - j) \times ((3i + j - 11k) \times (4i + 4j - 5k)) \\ = 9i - 15j + 13k$$