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19/MHS07/003

Pharmacology Dept.

Math 104 Assignment.

1. The function is defined for all real numbers except $x = 2$.

The set of all real numbers except $x = 2$ (Domain). The Codomain is the set of all real number except $y = 0$.

2. If $K = \ln V$ differentiate K .

$$K = \ln V$$

$$\text{Let } K = y \quad \& \quad V = x.$$

$$y = \ln x.$$

Recall in log form

$$y = \ln x$$

$$y = \log_e x.$$

$$e^y = x.$$

$$\frac{d}{dx} (e^y) = e^y \frac{dy}{dx} = x.$$

where x is differentiated gives 1

$$e^y \frac{dy}{dx} = 1$$

$$\text{Recall } e^y = x.$$

$$x \frac{dy}{dx} = 1$$

$$\frac{dy}{dx} = 1/x.$$

3. Express y as an explicit function of x in the following

(a) $2x - 3y - 2 = 0$

(b) $x^2 + y^2 = 4$

$$-3y = 2 - 2x$$

~~$$y = \frac{2 - 2x}{-3}$$~~

$$-3y = 2(1 - x)$$

$$y = \frac{2(1 - x)}{-3}$$

$$y = \frac{-2(1 - x)}{3}$$

(b). $x^2 + y^2 = 4$

$$y^2 = 4 - x^2$$

$$y = \sqrt{4 - x^2}$$

$$y = 2 - x$$

4. If $p = \sin^{-1} A$, find the derivative of p

$$p = \sin^{-1} A$$

Let $p = y$ & $A = x$

$$y = \sin^{-1} x = \arcsin(x)$$

$$y = \sin^{-1} x$$

$$y = \frac{x}{\sin}$$

$$x = \sin y$$

$$\frac{dx}{dy} = \cos y \quad \frac{dy}{dx} = \frac{1}{\cos y}$$

$$\cos^2 y + \sin^2 y = 1$$

$$\cos^2 y = 1 - \sin^2 y$$

$$\sin^2 y = x^2$$

$$\cos y = \sqrt{1 - x^2}$$

but $y = p$ and $A = x$

$$\frac{dy}{dx} = \frac{1}{\cos p} = \frac{1}{\sqrt{1 - x^2}}$$

Hence; $\frac{dy}{dx} = \frac{1}{\cos y} = \frac{1}{\sqrt{1 - x^2}}$

$$5. \text{ If } f(x) = 2x^2 - 5.$$

$$g(x) = 4x - 2.$$

Find $f \circ g(x)$ and $g \circ f(x)$.

$$f \circ g(x) = f(g(x))$$

$$2(4x - 2)^2 - 5.$$

$$2[(4x - 2)(4x - 2)] - 5.$$

$$2[(16x^2 - 8x - 8x + 4)] - 5.$$

$$2[16x^2 + 4] - 5.$$

$$2[16x^2 - 16x + 4] - 5.$$

$$32x^2 - 32x + 8 - 5.$$

$$32x^2 - 32x + 3.$$

$$b. \text{ } g \circ f(x) = g(f(x)).$$

$$4(2x^2 - 5) - 2.$$

$$8x^2 - 20 - 2.$$

$$8x^2 - 22.$$

$$6. \text{ If } f(x) = 3x^2 + 2x + 1 = 0$$

$$f_e(x) = \frac{f(x) + f(-x)}{2}$$

2.

$$f(-x) = 3(-x)^2 - 2(-x) + 1$$

$$= 3x^2 + 2x + 1$$

$$\frac{3x^2 + 2x + 1 + 3x^2 + 2x + 1}{2}$$

$$\frac{6x^2 + 2}{2} = 3x^2 + 1$$

$$f_o(x) = \frac{3x^2 - 2x + 1 - (3x^2 + 2x + 1)}{2}$$

$$f_o(x) = \frac{-4x}{2} = -2x.$$

$$f(x) = f_o(x) + f_e(x).$$

$$f(x) = 3x^2 + 1 - 2x$$

$$= 3x^2 - 2x + 1$$

7. Differentiate from first principle.

$$y = \cos x.$$

$$(y + \Delta y) = \cos(x + \Delta x).$$

$$\Delta y = \cos(x + \Delta x) - y$$

$$\Delta y = \cos(x + \Delta x) - \cos x. \quad \text{--- (i)}$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B.$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B.$$

$$\text{Let } A+B = x + \Delta x.$$

$$A-B = x.$$

$$2A = 2x + \Delta x.$$

$$A = \frac{2x + \Delta x}{2}.$$

$$A = x + \frac{\Delta x}{2}.$$

$$B = \frac{\Delta x}{2}.$$

$$\cos(x + \Delta x) - \cos x = 2 \sin\left(x + \frac{\Delta x}{2}\right) \sin\left(\frac{\Delta x}{2}\right).$$

$$\Delta y = 2 \sin\left(x + \frac{\Delta x}{2}\right) \sin\left(\frac{\Delta x}{2}\right)$$

$$\Delta y = 2 \sin\left(x + \frac{\Delta x}{2}\right) \sin\left(\frac{\Delta x}{2}\right).$$

$$\frac{dy}{dx} = \frac{\sin\left(x + \frac{\Delta x}{2}\right) \sin\left(\frac{\Delta x}{2}\right)}{\frac{\Delta x}{2}}.$$

Standard Limit

Limit $\Delta x \rightarrow 0$.

$$\frac{dy}{dx} = -\sin(x+0)$$

$$= -\sin x.$$

8 $y = 3t^2$ $y = \frac{3}{x}$

$$t^2 = \frac{1}{x}$$

$$y = \frac{3}{x}.$$

$$y = 3 \times \frac{1}{x}$$

$$\text{let } u = \frac{1}{x}$$

$$\frac{dy}{dx} = \frac{1}{x^2}$$

$$y = 3u$$

$$\frac{dy}{du} = 3$$

$$\frac{dy}{dx} = \frac{du}{dx} \times \frac{dy}{du}$$

$$3 \times \frac{-1}{x^2}$$

$$\frac{dy}{dx} = \frac{-3}{x^2}$$

9. Find $\frac{dy}{dx}$ If $y = x^2 \cos 2x e^{4x}$.

$$y = x^2 \cos 2x e^{4x}$$

$$\ln y = \ln (x^2 \cos 2x e^{4x})$$

$$\ln y = \ln (x^2) + \ln (\cos 2x) + \ln (e^{4x})$$

$$\frac{d}{dx} (\ln y) = \frac{d}{dx} (\ln x^2) + \frac{d}{dx} (\ln \cos 2x) + \frac{d}{dx} (\ln e^{4x})$$

$$\frac{1}{y} \frac{dy}{dx} = \frac{1}{x^2} (2x) + \frac{1}{\cos 2x} (-\sin 2x) + \frac{1}{e^{4x}} (4e^{4x})$$

$$\frac{1}{y} \frac{dy}{dx} = \frac{2x}{x^2} - \frac{\sin 2x}{\cos 2x} + \frac{4e^{4x}}{e^{4x}}$$

$$\frac{dy}{dx} = \frac{x}{2} + \cot 2x + 4$$

$$\frac{dy}{dx} = y \left(\frac{x}{2} + \cot 2x + 4 \right)$$

$$\frac{dy}{dx} = x^2 \cos 2x e^{4x} \left(\frac{x}{2} + \cot 2x + 4 \right)$$

10. Given that $y = \sin(3x^3 + 5)$ Find the derivative of y .

$$y = \sin(3x^3 + 5)$$

$$\text{Let } u = 3x^3 + 5 \quad \frac{du}{dx} = 9x^2$$

$$y = \sin u \quad \frac{dy}{du} = \cos u$$

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$= 9x^2 \times \cos u$$

~~$$9x^2 \cos u$$~~

$$9x^2 \cos(3x^3 + 5)$$