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DEPT: MBBS

COLLEGE: MHS

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COURSE CODE: MAT 104

Assignment

1. $y - 3x - 2 = 0$ and $3y + 2x + 9 = 0$

$$\text{let } A = y - 3x - 2 = 0$$

$$= \frac{dy}{dx} = 3 - 0 = 0$$

$$= \frac{dy}{dx} = 3 = 0$$

$$= \frac{dy}{dx} = 3$$

$$\text{let } B = 3y + 2x + 9 = 0$$

$$3 \frac{dy}{dx} + 1 + 0 = 0$$

$$3 \frac{dy}{dx} + 1 = 0$$

$$\frac{dy}{dx} = -\frac{1}{3}$$

A + B

ie $y - 2x - 2 = 0$ is perpendicular to $3y + 2x + 9 = 0$

2. $3y - 4 = 2x + 3$ and $y - 5 = x + 6$

let $A = 3y - 4 = 2x + 3$

$$3 \frac{dy}{dx} - 0 = 2 + 0$$

$$\frac{dy}{dx} = 2$$

$$\frac{dy}{dx} = \frac{2}{3}$$

let $B = y - 5 = x + 6$

$$\frac{dy}{dx} - 0 = 1 + 0$$

$$\frac{dy}{dx} = 1$$

$\therefore A \neq B$

i.e. $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ is not perpendicular

3. $x^2 + y^2 + 3y = 11 = 0$ at point $(1, 2)$

$$2x + 2y \frac{dy}{dx} + 3 \left(2x \frac{dy}{dx} + y \cdot 1 \right) - 0 = 0$$

$$2x + 2y \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y = 0$$

$$2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$m = \frac{dy}{dx} = \frac{-(2x + 3y)}{2y + 3x}$$

when $x = 1$ and $y = 2$

$$m = \frac{-(2(1) + 3(2))}{2(2) + 3(1)}$$

$$= \frac{-(2 + 6)}{4 + 3} = \frac{-8}{7}$$

$$m = \frac{-8}{7}$$

Equation of the tangent to a curve

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-8}{7}(x - 1)$$

$$y - 2 = \frac{-8x}{7} + \frac{8}{7}$$

$$7y - 14 = -8x + 8$$

$$8x + 7y - 14 - 8 = 0$$

$$8x + 7y - 22 = 0$$

b. Equation of the normal to a curve

$$y - y_1 = \frac{1}{m}(x - x_1)$$

$$y - 2 = \frac{1}{-8/7}(x - 1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$y - 2 = \frac{7x}{8} - \frac{7}{8}$$

$$8y - 16 = 7x - 7$$

$$8y = 7x - 7 + 16$$

$$7x - 8y + 9 = 0$$