

Examine whether / not these pair of lines are perpendicular to each other

1 $y - 3x - 2 = 0$ and $3y + x + 9 = 0$

2 $3y - 4 = 2x + 3$ and $y - 5 = x + 6$

3 Find the equations of the tangent & normal to the curve $x^2 + y^2 + 3xy - 11 = 0$ @ pt $(1, 2)$

∴ $y - 3x - 2 = 0$ and $3y + x + 9 = 0$

$$y = 3x + 2$$

$$3y = -x - 9$$

$$y = -\frac{1}{3}x - 3$$

$$m_1 = 3$$

$$m_2 = -\frac{1}{3}$$

m_1, m_2 is perpendicular to m_2
when their product equals -1

$$3 \times -\frac{1}{3} = -1$$

The pair of lines are perpendicular to each other

2 $3y - 4 = 2x + 3$ and $y - 5 = x + 6$

$$3y = 2x + 3 + 4$$

$$y = x + 6 + 5$$

$$3y = 2x + 7$$

$$y = x + 11$$

$$y = \frac{2}{3}x + \frac{7}{3}$$

$$m_1 = \frac{2}{3}$$

$$m_2 = 1$$

The lines are perpendicular when $m_1 m_2 = -1$
 $\frac{2}{3} \times 1 = \frac{2}{3}$

The pair of lines are not perpendicular to each other

$$3) \quad x^2 + y^2 + 3xy - 11 = 0 \quad \text{at pt } (1, 2)$$

$$2x + 2y \frac{dy}{dx} + 3y + 3x \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} (2y + 3x) = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

$$m = \left. \frac{dy}{dx} \right|_{x=1, y=2} = \frac{-2(1) - 3(2)}{2(2) + 3(1)} = \frac{-2 - 6}{4 + 3} = \frac{-8}{7}$$

Equation of tangent

$$y - 2 = -\frac{8}{7}(x - 1)$$

$$7y - 14 = -8x + 8$$

$$7y + 8x - 22 = 0$$

$$7y = -8x + 22$$

For the normal

$$m = -1 \div -\frac{8}{7} = \frac{7}{8}$$

Equation of the normal

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y - 7x - 9 = 0$$

$$8y = 7x + 9$$