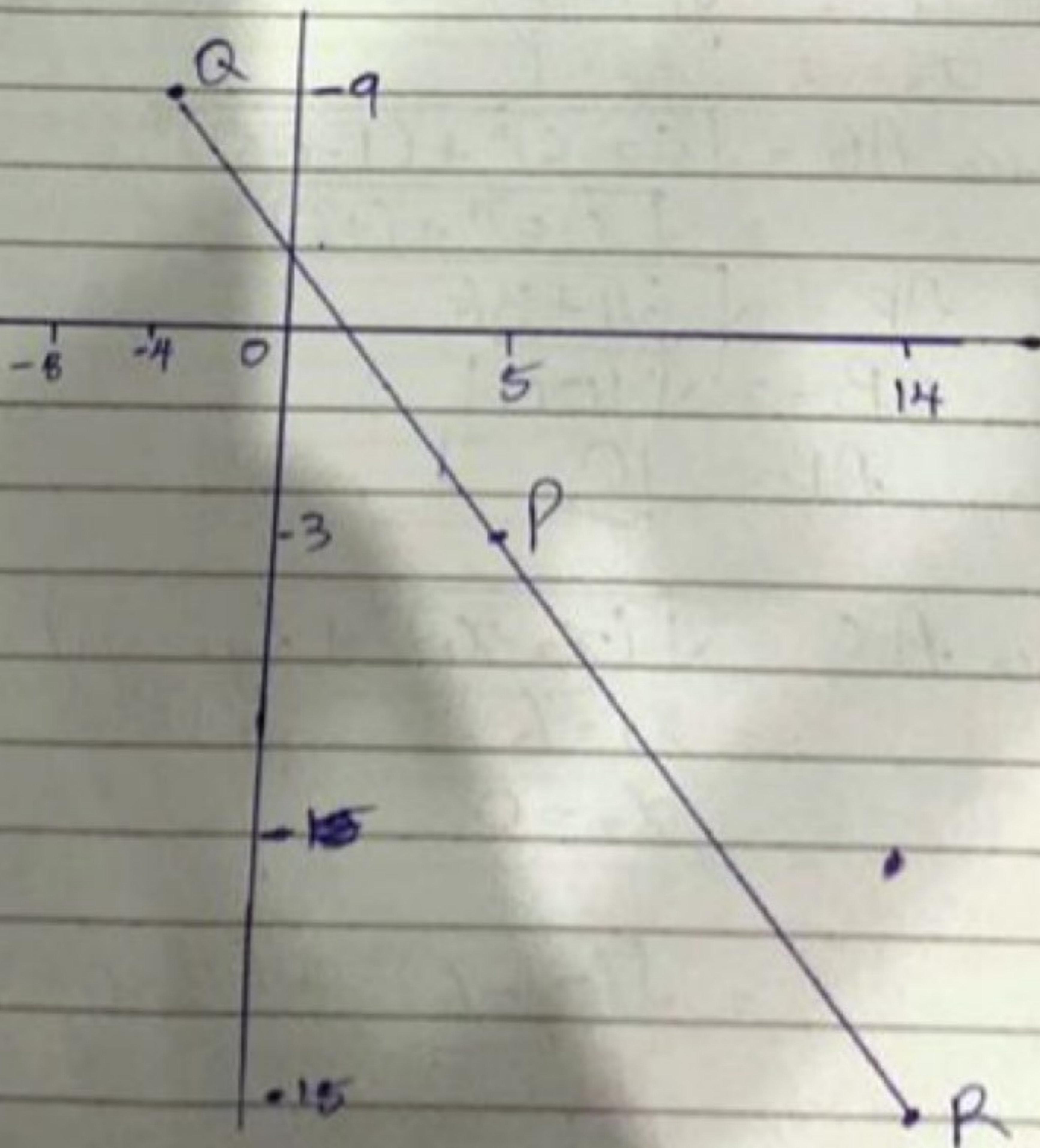


$$\begin{aligned} \text{Distance } BC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= x_1 = -2 \quad y_1 = 1 \\ &\quad x_2 = 0 \quad y_2 = 3 \end{aligned}$$

$$\begin{aligned} &= \sqrt{(0 - (-2))^2 + (3 - 1)^2} \\ &= \sqrt{(2)^2 + (2)^2} \\ &= \sqrt{4 + 4} \\ &= \sqrt{8} \end{aligned}$$

∴ Since $AB = AC$, therefore the triangle is an isosceles triangle.

If P, Q and R are the points $(5, -3)$, $(-4, 9)$ and $(14, -15)$ respectively. Find the ratio in which
 P divides QR
 R divides PQ



∴ P divides QR

$$\frac{L}{2} = K$$

$$\therefore \frac{L}{2} = \frac{K}{L}$$

The ratio R divided P Q
 $= 2:1$

$$S = \frac{L(-4) + K(14)}{L+K}$$

$$5(L+K) = -4L + 14K$$

$$5L + 5K = -4L + 14K$$

Collect like terms

$$5L + 4L = 14K - 5K$$

$$\frac{9L}{9} = \frac{9K}{9}$$

$$L = K$$

$$\therefore \frac{K}{L} = \frac{1}{1}$$

\therefore The ratio is 1:1

$$y = \frac{Ly_1 + Ky_2}{L+K}$$

$$\begin{cases} y = -3, y_2 = -15 \\ y_1 = 9, L = ?, K = ? \end{cases}$$

$$-3 = \frac{L(9) + K(-15)}{L+K}$$

$$-3(L+K) = 9L - 15K$$

$$-3L - 3K = 9L - 15K$$

$$-3L - 9L = -15K + 3K$$

$$\frac{-12L}{-12} = \frac{-12K}{-12}$$

$$K = L$$

$$\therefore \frac{K}{L} = \frac{1}{1}$$

The P divides QR

i) R divides PQ
R divides PQ externally

$$x = \frac{Lx_1 - Kx_2}{L - K}$$

$$\begin{cases} x_1 = 5, x_2 = -4, x = 14 \\ L = ?, K = ? \end{cases}$$

$$\therefore \frac{14 = L(5) - K(-4)}{L - K}$$

$$14 = \frac{5L + 4K}{L - K}$$

$$14(L - K) = 5L + 4K$$

$$14L - 14K = 5L + 4K$$

collect like terms

$$14L - 5L = 4K + 14K$$

$$9L = 18K$$

$$\frac{9}{9} = \frac{18}{9} \frac{K}{L}$$

$$L = 2K$$

~~L = 1, K = 1/2~~

$$\frac{L}{K} = \frac{2K}{K}$$

$$\frac{L}{K} = \frac{1}{2}$$

$$\therefore -2 : 1$$

$$y = \frac{Ly_1 - Ky_2}{L - K}$$

$$\begin{cases} y_1 = -3, y_2 = 9, y = -15 \\ L = ?, K = ? \end{cases}$$

$$-15 = \frac{L(-3) - K(9)}{L - K}$$

$$-15(L - K) = -3L - 9K$$

$$-15L + 15K = -3L - 9K$$

$$-15L + 3L = -9K - 15K$$

$$-12L = -24K$$

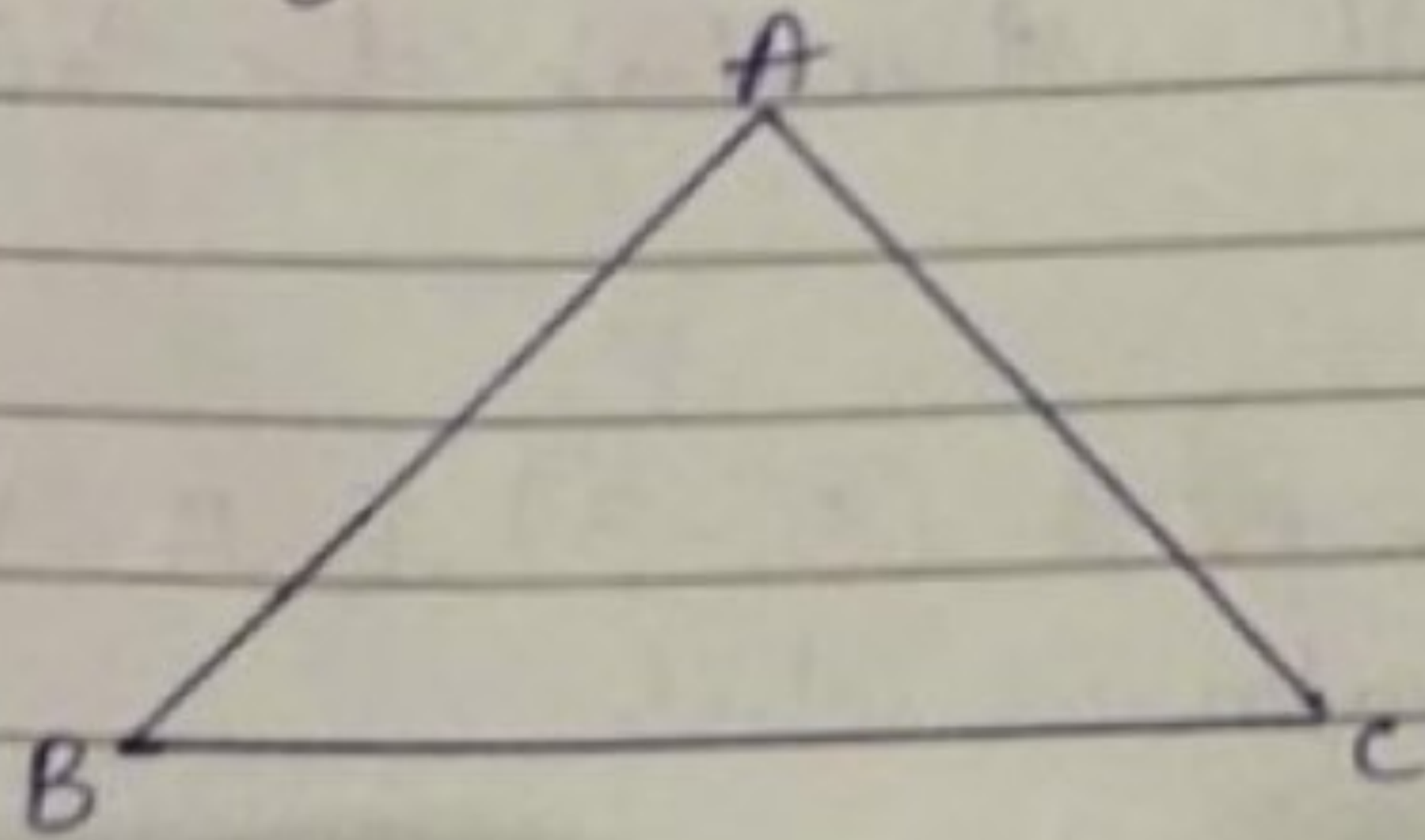
MATRIC NUMBER: 19/ENG07/009

COURSE CODE: MAT 102

DATE SUBMITTED: 8-04-2020

DEPARTMENT: PETROLEUM ENGINEERING

1. Show that points $A(6, 5)$, $B(-2, 1)$, $C(0, 3)$ form an isosceles triangle



$$\text{Distance } AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$x_1 = 6 \quad y_1 = 5$$

$$x_2 = -2 \quad y_2 = 1$$

$$\text{Distance } AB = \sqrt{(-2 - 6)^2 + (1 - 5)^2}$$

$$= \sqrt{(-8)^2 + (-4)^2}$$

$$AB = \sqrt{64 + 16}$$

$$AB = \sqrt{80}$$

$$AB = \underline{\underline{10}}$$

$$\text{Distance } AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$x_1 = 6 \quad y_1 = 5$$

$$x_2 = 0 \quad y_2 = 3$$

$$= \sqrt{(0 - 6)^2 + (3 - 5)^2}$$

$$= \sqrt{(-6)^2 + (-2)^2}$$

$$= \sqrt{36 + 4}$$

$$= \sqrt{40}$$

$$= \underline{\underline{10}}$$