

$$A = 2i - j, B = 3i + j - 11k, C = 4i + 4j - 5k$$

i)  $-3A + 7B - 8C$

$$\begin{aligned} &= -3(2i - j) + 7(3i + j - 11k) - 8(4i + 4j - 5k) \\ &= -6i - 3j + 21i + 7j - 77k - 24i + 24j - 40k \\ &= -9i + 28j - 117k \end{aligned}$$

iii)  $A \times (B \times C)$

$$\begin{aligned} &= (B \times C) = \begin{vmatrix} 3i + j - 11k \\ 4i + 4j - 5k \end{vmatrix} \begin{vmatrix} i & j & k \\ 3 & 1 & -11 \\ 4 & 4 & -5 \end{vmatrix} \\ &= i \begin{vmatrix} 1 & -11 \\ 4 & -5 \end{vmatrix} - j \begin{vmatrix} 3 & -11 \\ 4 & -5 \end{vmatrix} + k \begin{vmatrix} 3 & 1 \\ 4 & 4 \end{vmatrix} \\ &= i(-5 + 44) - j(-15 + 44) + k(12 - 4) \\ &= 39i - 29j + 8k \end{aligned}$$

$$\begin{aligned} A \times (B \times C) &= 2i - j + 2i - j \times 39i - 29j + 8k \begin{vmatrix} i & j & k \\ 2 & -1 & 0 \\ 39 & -29 & 8 \end{vmatrix} \\ &= 78i - 29j + 8k \\ &= 115i \begin{pmatrix} -1 & 0 \\ -29 & 8 \end{pmatrix} - j \begin{pmatrix} 2 & 0 \\ 39 & 8 \end{pmatrix} + k \begin{pmatrix} 2 & -1 \\ 39 & -29 \end{pmatrix} \\ &= i(-8 + 0) - j(16 - 0) + k(-58 + 39) \\ &= -8i - 16j - 19k \\ &= -27 \end{aligned}$$

iv)  $(3A \times B) \cdot (A \times 2B)$

$$3A = 6i - 3j$$

$$3A \times B = \begin{vmatrix} i & j & k \\ 6 & -3 & 0 \\ 3 & 1 & -11 \end{vmatrix}$$

$$\begin{aligned} &= i \begin{pmatrix} -3 & 0 \\ 1 & -11 \end{pmatrix} - j \begin{pmatrix} 6 & 0 \\ 3 & -11 \end{pmatrix} + k \begin{pmatrix} 6 & -3 \\ 3 & 1 \end{pmatrix} \\ &= i(33 - 0) - j(-66 - 0) + k(8 + 9) \\ &= 33i + 66j + 15k \end{aligned}$$

$$2B = 6i + 2j - 22k$$

$$A \times 2B = \begin{vmatrix} i & j & k \\ 2 & -1 & 0 \\ 6 & 2 & -22 \end{vmatrix}$$

$$\begin{aligned} &= i \begin{pmatrix} -10 & 0 \\ 2 & -22 \end{pmatrix} - j \begin{pmatrix} 2 & 0 \\ 6 & -22 \end{pmatrix} + k \begin{pmatrix} 2 & -1 \\ 6 & 2 \end{pmatrix} \\ &= i(22 - 0) - j(-44 - 0) + k(4 + 6) \\ &= 22i + 44j + 10k \end{aligned}$$

$\vec{6i}$

$$\begin{aligned} & (3A \times B) \cdot (A \times 2B) \\ &= (6\vec{i} + 2\vec{j} - 22\vec{k}) \cdot (22\vec{i} + 44\vec{j} + 10\vec{k}) \\ &= 132 + 88 - 220 \\ &= 0 \end{aligned}$$

v)  $A - 2B - C$

$$\begin{aligned} & 2\vec{i} - \vec{j} - (6\vec{i} + 2\vec{j} - 22\vec{k}) + 4\vec{i} + 4\vec{j} - 5\vec{k} \\ &= 5\vec{j} - 27\vec{k} \end{aligned}$$

2) Perpendicular vectors is a vector that forms a right angle

Coplanar vectors are the the vector which lie in the same plane formed by two axes in the coordinate geometry