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 500L.

1) Linear programming is an optimization technique for a system of linear constraints and a linear objective function. An objective function defines the quantity to be optimized, and the goal of linear programming is to find the values of the variables that maximize or minimize the objective function.

2)
$$\begin{array}{cccc|c} 2 & 0 & 0 & 1 & 4 & 51 \\ 2 & 0 & 1 & 0 & 3 & -99 \\ 2 & 1 & 1 & 1 & 2 & 351 \\ \hline 0 & -20 & 0 & 0 & 30 & 10500 \end{array}$$

$R_4 \rightarrow 20R_3 + R_4$

x_1	x_2	s_1	s_2	s_3	Constant
2	0	0	1	4	51
2	0	1	0	3	-99
2	1	1	1	2	351
40	0	20	20	70	17520

Since we have no,

$$\begin{array}{cccc|c} 1 & \frac{1}{2} & \frac{1}{2} & 0 & 500 \\ 0 & \frac{1}{2} & -\frac{1}{2} & 1 & 300 \\ 0 & -5 & 15 & 0 & 15000 \end{array}$$

$$R_2 - 2R_1$$

$$\begin{array}{cccc|c} 1 & \frac{1}{2} & \frac{1}{2} & 0 & 500 \\ 0 & 1 & -1 & 2 & 600 \\ 0 & -5 & 15 & 0 & 15000 \end{array}$$

$$R_1 = -\frac{1}{2}R_2 + R_1$$

$$R_3 = 5R_2 + R_3$$

$$\begin{array}{cccc|c} 1 & 0 & 1 & -1 & 200 \\ 0 & 1 & -1 & 2 & 600 \\ 0 & -5 & 15 & 0 & 15000 \end{array}$$

$$\begin{array}{cccc|c} 1 & 0 & 1 & -1 & 200 \\ 0 & 1 & -1 & 2 & 600 \\ 0 & 0 & 10 & 10 & 18000 \end{array}$$

$$x_1 = 200, x_2 = 600, z = 18,000$$

Objective function

$$\text{Max } z = 30x_1 + 20x_2$$

Subtract -10

$$2x_1 + x_2 \leq 1000$$

$$x_1 + x_2 = 500$$

$$x_1, x_2 \geq 0$$

$$Z + 30x_1 - 20x_2 = 0$$

x_1	x_2	s_1	s_2	Z
2	1	1	0	1000
1	1	0	1	500
-30	-20	0	0	0

$$R_1 = \text{Row } 1/2, \quad R_3 \rightarrow 30R_1 + R_3$$

$$R_2 = -R_1 + R_2$$

x_1	x_2	s_1	s_2	Z
1	$1/2$	$1/2$	0	500
1	1	0	1	800
-30	-30	0	0	0

1	$1/2$	$1/2$	0	500
0	$1/2$	$-1/2$	1	300
0	-5	15	0	15000