

$$= (3A \times B) \cdot (A \times 2B)$$

$$= (3 \times 22) + (66 \times 44) + (15 \times 10) = 3780$$

v) $A - 2B - C$

$$= (2i - j) - (6i + 2j - 22k) - (4i + 4j - 5k)$$

$$= -8i - 7j + 27k$$

2) Perpendicular

Coplanar

Two vectors A and B are perpendicular

if their scalar product is zero $(A \times B)$

Three vectors A, B and C are coplanar if their scalar

product is equal to 0 $(A \cdot (B \times C))$

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$$\text{if } A = 2i - j, B = 3i + j - 11k \text{ and } C = 4i + 4j + 5k$$

i) $3A + 7B - 8C$

$$-6i + 3j + 21i + 7j - 77k - 32i - 32j - 40k \\ = 17i - 22j - 77k$$

ii) $K = 2A + 4B - C$

$$2A = 2(2i - j) = 4i - 2j$$

$$+ 4B = 4(3i + j - 11k) = 12i + 4j - 44k$$

$$2A + 4B - C = 12i - 2j - 39k$$

$$|K| = \sqrt{(12)^2 + (-2)^2 + (-39)^2} = \sqrt{1669} = 40.85$$

The direction cosines of K are

$$\cos \alpha = \frac{12}{40.85} = 0.2938$$

$$\cos \beta = \frac{-2}{40.85} = 0.0490$$

$$\cos \gamma = \frac{-39}{40.85} = 0.9547$$

iii) $A \times B \times C = A \times B = \begin{vmatrix} i & j & k \\ 2 & -1 & 0 \\ 3 & 1 & -11 \end{vmatrix}$

$$= i(11-0) - j(-22-0) + k(2+3)$$

$$= 11i + 22j + 5k$$

$$A \times B \times C = \begin{vmatrix} i & j & k \\ 11 & 22 & 5 \\ 4 & 4 & -5 \end{vmatrix}$$

$$= i(-110-20) - j(-55-20) + k(44-88)$$

$$= -130i + 75j - 44k$$

$$iv) (3A \times B) - (A \times 2B)$$

$$3A = 3(2i - j) = 6i - 3j$$

$$2B = 2(3i + j - 11k) = 6i + 2j - 22k$$

$$3A \times B = \begin{vmatrix} i & j & k \\ 6 & -3 & 0 \\ 3 & 1 & -11 \end{vmatrix}$$

$$= i(33-0) - j(-66-0) + k(6+9)$$

$$= 33i + 66j + 15k$$

$$v) A \times 2B = \begin{vmatrix} i & j & k \\ 2 & -1 & 0 \\ 6 & 2 & -22 \end{vmatrix}$$

$$= i(22-0) - j(-44-0) + 4(k+6)$$

$$= 22i + 44j + 10k$$