

Oginni Oluwaseyi Michael

19/EN606/041

Mechanical Engineering

MAT 102

1) $A(6, -5)$, $B(-2, 1)$ and $C(0, 3)$

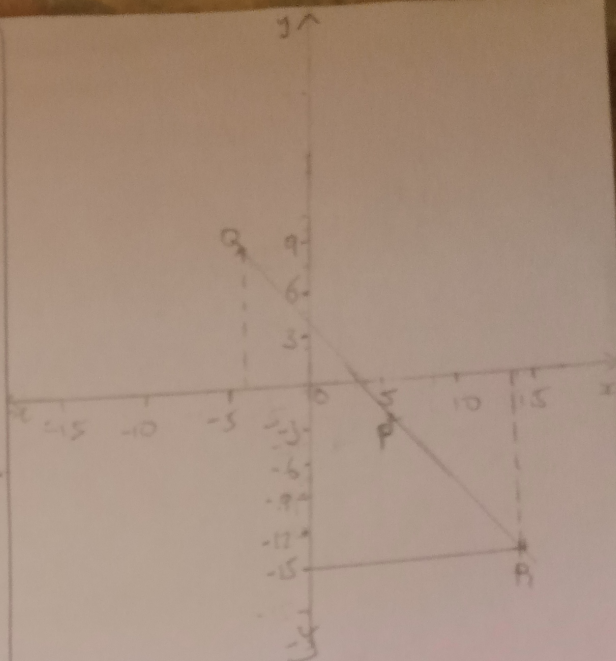
$$\begin{aligned}\overline{AB} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(-2 - 6)^2 + (1 + 5)^2} \\ &= \sqrt{64 + 36} \\ &= \sqrt{100} = 10\end{aligned}$$

$$\begin{aligned}\overline{BC} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(0 + 2)^2 + (3 - 1)^2} \\ &= \sqrt{4 + 4} \\ &= \sqrt{8} = 2\sqrt{2}\end{aligned}$$

$$\begin{aligned}\overline{AC} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(0 - 6)^2 + (3 + 5)^2} \\ &= \sqrt{36 + 64} \\ &= \sqrt{100} = 10\end{aligned}$$

Since $\overline{AB} = \overline{AC} \neq \overline{BC}$, \therefore its an isosceles triangle

2) $P(5, -3)$, $Q(-4, 9)$, $R(14, -15)$



a) P divides \overline{QR} internally

Using $x = \frac{l x_1 + k x_2}{l + k}$

$$5 = \frac{l(-4) + k(14)}{l + k}$$

$$5(l + k) = -4l + 14k$$

$$5l + 5k = -4l + 14k$$

$$5l + 4l = 14k - 5k$$

$$9l = 9k$$

$$\text{Ratio } k:l \Rightarrow 1:1$$

b) P divides \overline{PQ} externally

Using $x = \frac{l x_1 - k x_2}{l - k}$

$$14 = \frac{l(5) - k(-4)}{l - k}$$

$$14l - 14k = 5l + 4k$$

$$14l - 5l = 4k + 14k$$

$$9l = 18k$$

$$\text{Ratio } k:l \Rightarrow 2:1$$