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Matric no: 16/ENG04/066

Course Title: Introduction to Biomedical Engineering (EEE 578)

Assignment Title: Analysis of “ERG scheme for closed-loop Anesthesia”.

**1. Title of paper**

An Explicit Reference Governor Scheme for Closed-Loop Anesthesia

**2. Authors and affiliation**

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**3. Structure of Paper**

Abstract

Introduction

Modeling of the system

Fig 1: PKPD model block diagram

Control Architecture

Pre-stabilizing the Propofol Delivery System

Fig 2: The iControl closed-loop anesthesia system

Fig 3: Block diagram of the propofol control system

Enforcing Constraints Handling Capability

Fig 4: Approximation error for different hypnosis levels.

Results and Discussion

Fig 5: The unconstrained simulated responses of the 44 patients

Table 1: COMPARISON OF THE OBTAINED INDUCTION TIME.

Conclusion

Fig 6: The simulated responses of the 44 patients with the ERG scheme

References

**4. Abbreviations**

ECE - European Control Conference

IEEE – Institute of Electrical and Electronics Engineers

FNRS MIS – Fond de la Recherche Scientifique Mandat d’impulsion scientifique

SAAS - Service d’Automatiseet d’Analyse des Syst`emes

ERG – Explicit Reference Governor

PK – PharmacoKinetic

PD – PharmacoDynamic

PKPD – PharmacoKinetic PharmacoDynamic

DOH – Depth of hypnosis  
PID – Proportional Integral Derivative  
LBM – Lean Body Mass  
DSM – Dynamic Safety Margin  
NF – Navigational Field  
KF – Kalman Filter

## 5. Remarks

- a. By defining approximation error as  $e(t) = y(t) - \hat{y}(t)$ , the value of  $\delta_0$  can be determined as  $\delta_0 = \max_{v \in [0, 0.5]} \sup_t |e(t)|$ .
- b. Since the states of the system are not directly measured during the experiments, to determine the Lyapunov function  $V_i(\cdot)$ ,  $i = 1, \dots, 7$  an estimator is needed.
- c. To make sure that obtained matrix  $P_i$  is valid Lyapunov matrix for all patients, one possible way is to use Kharitonov theory, and replace the constraint  $A^T P_i + P_i A \leq 0$  with the resulting four Kharitonov's based constraints.

## 6. Abstract

A constrained control scheme for the control of depth of hypnosis in clinical anesthesia while obeying all imposed clinical constraints.

## 7. Introduction

- a. Meaning of anesthesia and why it is used on people undergoing surgery, and manual feedback control is the current practice.
- b. The components of anesthesia, and the proposal of a propofol delivery system to control the depth of hypnosis.
- c. The phases of propofol hypnosis and the challenge of safely administering the drug during the induction phase and the proposed solutions.
- d. The overdosing problem as well as other safety issues can be solved by defining some suitable safety constraints.
- e. The use of Explicit Reference Governor (ERG) framework because it requires very limited computational capability.
- f. The organization of the rest of the paper as broken down into sections.

## 8. Differences between figure 5 and 6

Figure 5	Figure 6
The DOH% goes below 40% during the first 10 mins of the DOH   time plot	The DOH% does not go below 40% during the entire plot
The $I(t)$ [ml/h] value is above 200 for most patients, reaching 400 at the initial time of 0 – 10 min	Most patients have an $I(t)$ [ml/h] approximately equal to 200 between 0- 10 min
In the $C_p$ [ug/m] plot, the transient region last for a short period (less than 5 min)	The transient period lasts for about 10 min for most patients.
In the $C_e$ [ug/m] plot, the transient region is very steep lasting for a time approximately less than 5 min.	The transient period less steep lasts for about 10 min.
Induction Time mean $\pm$ STD <sup>2</sup> [min, max] = 3.11 $\pm$ 0.38 [2.53, 4.46]	Induction Time mean $\pm$ STD <sup>2</sup> [min, max] = 6.24 $\pm$ 7.51 [4.98, 8.96]

Table 1: comparison of Figure 5 & 6

### Key results

- The proposed ERG scheme provides results that guarantee constraint satisfaction.
- A DOH of 50% was achieved for all patients.
- The ERG scheme gives a slower induction time mean.
- The ERG scheme automatically converges to the desired level of hypnosis using the auxiliary reference.

## 9. Conclusion

- I see the organization of the conclusion section.
- Yes, I understand the conclusion.

## 10. Section II

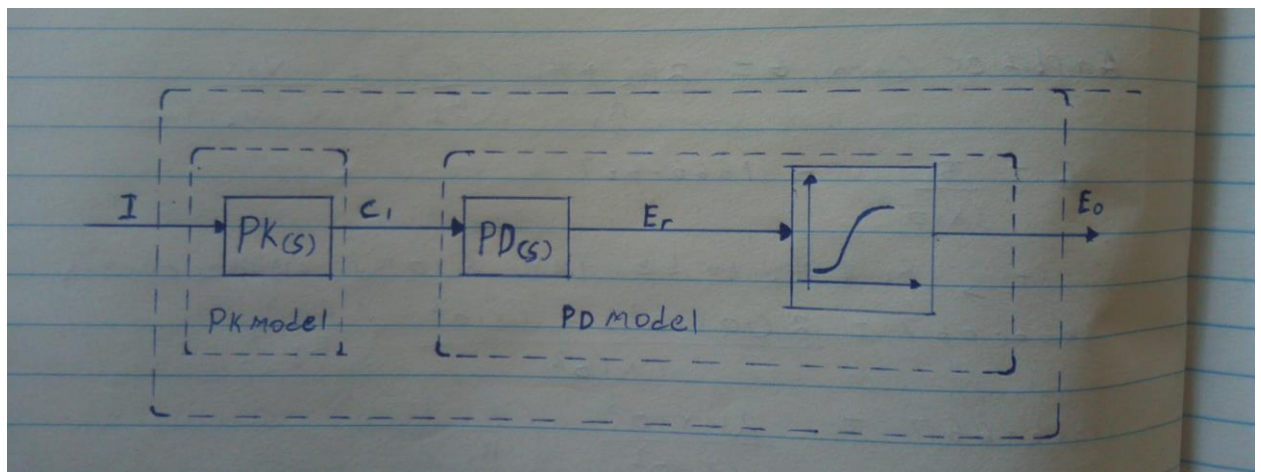


Figure 1: PKPD Model

- PK model: It relates the drug plasma concentration with the administered dose. It considers three compartments: plasma compartment, shallow peripheral compartment and the deep peripheral compartment.

Input variable:  $I(t)$  (in [mg/s]) is the infusion rate.

Output variable:  $C_1$  (in [mg/l]) is the propofol concentration.

- PD model: It relates the plasma concentration with the pharmacological end-effect.

Input variable:  $C_1$  is the propofol concentration.

Output variable:  $E_o(t)$  is the clinical hypnotic effect.

- PKPD model: It gives a drug-response relationship of the propofol.

Input variable:  $I(t)$  (in [mg/s]) is the infusion rate.

Output variable:  $E_o(t)$  is the clinical hypnotic effect.

PK Model equation.

$$\begin{bmatrix} \dot{C}_1 \\ \dot{C}_2 \\ \dot{C}_3 \end{bmatrix} = \begin{bmatrix} -k_{10} + k_{12} + k_{13} & k_{12} & k_{13} \\ k_{21} & -k_{21} & 0 \\ k_{31} & 0 & -k_{31} \end{bmatrix} \begin{bmatrix} C_1 \\ C_2 \\ C_3 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} I$$

$$k_{10} = \frac{Cl_1}{V_1}, k_{12} = \frac{Cl_2}{V_1}, k_{21} = \frac{Cl_2}{V_2}, k_{13} = \frac{Cl_3}{V_1}, k_{31} = \frac{Cl_3}{V_3}$$

$C_1, C_2$  and  $C_3$  are the propofol concentration in the plasma, fast peripheral compartment, and slow peripheral compartments respectively.  $V_1, V_2,$  and  $V_3$  are the volumes for each compartment respectively.  $Cl_1$  is the elimination clearance,  $Cl_2$  and  $Cl_3$  are inter-compartmental clearance respectively.

PD Model equation.

$$PD(s) = \frac{C_e(s)}{C_p(s)} = e^{-T_d s} \frac{k_d}{s + k_d}$$

Where  $C_p(t) = C_1(t)$ , and  $T_d$  (in [s]) and  $k_d$  (in [s<sup>-1</sup>]) are transport delay and rate of propofol distribution between the plasma concentration and the brain.

## 11. Section III

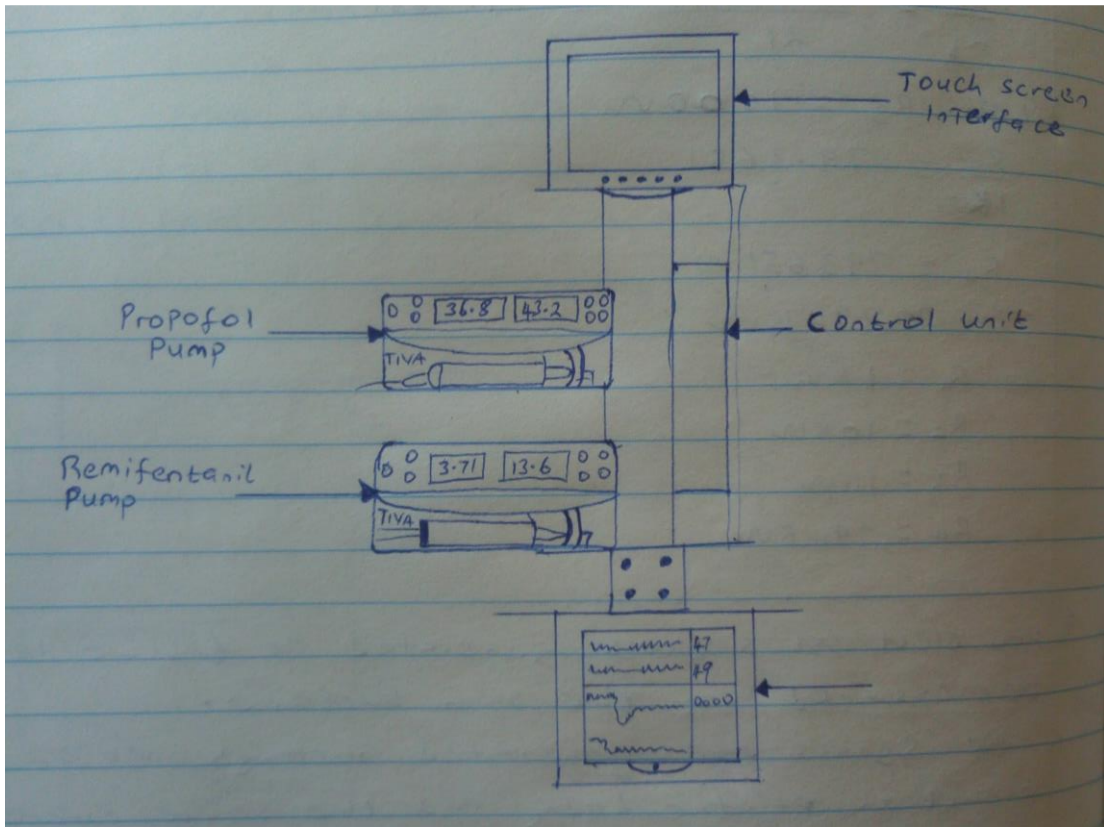


Figure 2: The iControl closed-loop anesthesia system

I have read the PID section of the 'experience controls' app.

Design of a PID controller

$$G_{ff}(s) = k + \frac{k_i}{s}$$

$$G_c(s) = \frac{k_d N s}{s + N}$$

$$LBM = 0.3281 \cdot W + 0.33929 \cdot H - 29.5336 \text{ - for male}$$

$$LBM = 0.29569 \cdot W + 0.41813 \cdot H - 43.2933 \text{ - for female}$$

Using  $W = 69\text{Kg}$  and  $H = 188\text{cm}$  for male LBM

$$LBM = (0.3281 \times 69) + (0.33929 \times 188) - 29.5336$$

$$LBM = 56.89182$$

$$k = 0.0243LBM, k_1 = 0.000165LBM, k_d = 1.35LBM$$

$$k = 1.382471226$$

$$k_i = 0.0093871503$$

$$k_d = 76.803957$$

- The iControl system is used for the clinical evaluation of the controller design. It stabilizes the propofol delivery system using a robust PID controller.
- Integrator windup refers to a scenario in a PID feedback controller where a large change in setpoint occurs and the integral term accumulates a significant error during the rise.
- Equation (13) represents a non-linear system.
- Constraints satisfaction prevents integral windup which in the case is overdose.
- The aim of the ERG framework is to determine an invariant set (in particular, a Lyapunov level set) that would contain the state trajectory if the currently auxiliary reference were to remain constant.
- The ERG generates a signal which is used as a reference signal to the system.