

6a

Application of Faraday's law in the production of sound in electric guitar

- The coil in this case called the pickup coil is placed near the vibrating string which is made of a metal that can be magnetized. A permanent magnet inside the coil magnetizes the portion of the string nearest the coil. When the string vibrates at some frequency, the magnetized segment produces a changing magnetic flux through the coil. The changing flux induces an emf in the coil that is fed to an amplifier. The output of the amplifier is sent to the loudspeakers, which produces the sound waves we hear.

6b

The magnetic flux through the coil at  $t=0$  is 0 because  $B=0$  at the time

$$|\mathcal{E}_1| = N \frac{d\Phi_B}{dt}$$

$$|\mathcal{E}_1| = N \Delta \Phi_B / \Delta t$$

$$|\mathcal{E}_1| = N \frac{\Delta \Phi_B}{\Delta t} = N \frac{(\Phi_B)_{t_2} - (\Phi_B)_{t_1}}{t_2 - t_1}$$

6c

(4)

The magnetic flux through a surface is the surface integral of the normal component of the magnetic field with flux density  $B$  passing through the medium. Or Magnetic flux is the integral of magnetic field represented by lines of force.

45 By deduction  ~~$F = \frac{qB}{2\pi m}$~~   $F = \frac{qB}{2\pi m}$

$$\therefore q = 1.6 \times 10^{-19}$$

$$B = 8.5 \times 10^{-1}$$

$$m = 9.11 \times 10^{-31}$$

$$F = \frac{1.6 \times 10^{-19} \times 8.5 \times 10^{-1}}{2(\pi)(9.11 \times 10^{-31})}$$

$$= \frac{1.6 \times 10^{-19} \times 8.5 \times 10^{-1}}{2(3.142)(9.11 \times 10^{-31})}$$

$$= \frac{1.6 \times 10^{-19} \times 8.5 \times 10^{-1}}{(6.284)(9.11 \times 10^{-31})}$$

$$= \frac{1.36 \times 10^{-18}}{5.724 \times 10^{-30}}$$

$$= 2.37 \times 10^{11} \text{ Hz}$$

$$F = 9.7 \times 10^{11} \text{ Hz}$$

2

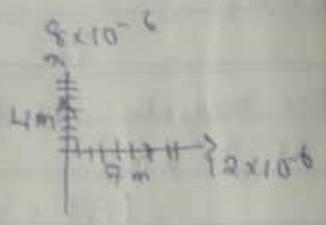
- Distinguish between the terms: electric field and electric field intensity
- 5) A positive charge  $Q_1 = 8 \mu\text{C}$  is at the origin and a second positive charge  $Q_2 = 12 \mu\text{C}$  is on the x-axis at  $x = 4\text{m}$ .
- the net electric field at a point P on the x-axis at  $x = 7\text{m}$
  - the electric field at a point Q on the y-axis at  $y = 3\text{m}$  due to the charges

Definition  
 Electric field is a region of space in which electric charge is felt  
 where electric field intensity is the force per unit charge  
 mathematically:

$$E = \frac{F(\text{N})}{q(\text{C})}$$

26)  $Q_1 = 8 \times 10^{-6}$   
 $Q_2 = 12 \times 10^{-6}$   
 $r_1 = 4\text{m}$

$$E = \frac{kq}{r^2}$$



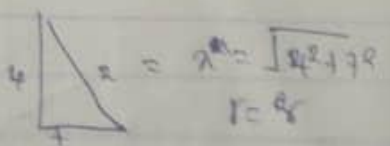
Note: Point P is a vector sum where  $E_{\text{net}} = E_1 + E_2$   
 $E_{\text{net}} = \sqrt{E_{x2}^2 + E_{y2}^2}$

Obtaining the electric fields

$$E_1 = \frac{kq}{r^2} = \frac{9.0 \times 10^9 \times 8 \times 10^{-6}}{4^2} = 1467.75 = 1.47 \times 10^3 \text{ N/C}$$

$E_2 = ?$  from the diagram

$$E_2 = \frac{kq}{r^2}$$



$$= \frac{9 \times 10^9 \times 12 \times 10^{-6}}{5^2} = 4.49 \times 10^3 \text{ N/C} \quad \therefore E_2 = 2.219 \text{ N/C}$$

Calculating angle  $\theta = \tan^{-1}(y/x)$

$$\theta = \tan^{-1}(4/4) = \tan^{-1}(1) = 29.7 \approx 30$$

$$E_y = 147.000 + 2.1435 = 147004.435$$

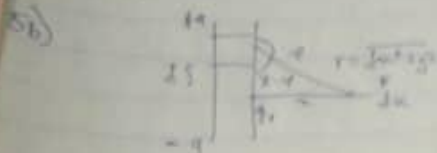
$$E_{\text{net}} = \sqrt{E_x^2 + E_y^2} = \sqrt{(2.219)^2 + (147004.435)^2} = 1.47 \times 10^5 \text{ N/C}$$

$$\therefore (E_x)_2 = 4.49 \times \cos 29.7 = 2.219$$

$$(E_y)_2 = 4.49 \times \sin 29.7 = 2.219$$

$\Sigma 4.438$

2) Biot-Savart law is an equation that describes the magnetic field created by a current carrying wire and allows one to calculate its strength.



$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \theta}{r^2}$$

$$\sin(\alpha - \theta) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\alpha - \theta)}{r^2}$$

From diagram  $r^2 = x^2 + y^2$  (Pythagorean)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\alpha - \theta)}{x^2 + y^2} \quad \text{--- (1)}$$

$$\text{But } \sin(\alpha - \theta) = \frac{x}{\sqrt{x^2 + y^2}} \quad \text{--- (2)}$$

$$= \frac{x}{(x^2 + y^2)^{3/2}} \quad \text{--- (1)}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

$$= B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl x}{(x^2 + y^2)^{3/2}}$$

Recall  $dl = dy$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)} dy \quad \text{--- (1)}$$

Using integration

$$\int \frac{dy}{x^2 + y^2} = \frac{1}{x^2} \cdot \frac{y}{(x^2 + y^2)^{1/2}}$$

Equation (1) becomes

$$B = \frac{\mu_0 I}{4\pi} \left[ \frac{y}{(x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I}{4\pi} \left[ \frac{2a}{x^2 + a^2} \right]^{1/2}$$

$$B = \frac{\mu_0 I}{4\pi x} \left[ \frac{2a}{(x^2 + a^2)^{1/2}} \right]$$

When the length  $2a$  of the conductor is very great in comparison to its distance  $x$  from point P, we consider it infinitely long. That is when

$a$  is much larger than  $x$   
 $(x^2 + a^2)^{1/2} = a$ , as  $a \rightarrow \infty$

$$B = \frac{\mu_0 I}{2\pi x}$$