

NAME: ODOGWU PAUL CHIDOZIE

MATRIC NO.: 15/ENG04/039

EEE 552 ASSIGNMENT

(a)(i) Recall $E = \frac{I}{r^2} = \frac{I}{\pi}$

Therefore,

$$L = \frac{E}{\pi}$$

Considering reflection factor,

$$L = \frac{E}{\pi} \times \text{reflection factor}$$

$$L = \frac{44000}{\pi} \times \frac{85}{100}$$

$$L = 11.905 \times 10^3 \text{ cd/m}^2 \quad \text{or} \quad 1.19 \times 10^4 \text{ cd/m}^2$$

(ii) $L = \frac{0.22}{\pi} \times \frac{85}{100}$

$$L = 59.52 \times 10^{-3} \text{ cd/m}^2$$

(b)(i) Flux emitted by source

$$\phi = I \times \omega = 120 \times 4\pi = 480\pi \text{ lumen}$$

Flux emitted by globe (30% is absorbed)

$$480\pi \times \frac{30}{100} = 144\pi \text{ lumen}$$

$$\therefore \text{Flux emitted by globe} = 480\pi - 144\pi = 336\pi \text{ lumen}$$

$$\text{Luminance} = \frac{\text{Flux emitted}}{\text{Area}} = \frac{336\pi}{\pi \times 0.22^2} = 6942 \text{ lumen/m}^2$$

$$\begin{aligned}
 \text{(ii) Candle Power (CP)} &= \frac{\text{Lumen}}{W} \\
 &= \frac{336\pi}{4\pi} \\
 &= 84 \text{ cd} //
 \end{aligned}$$

$$\begin{aligned}
 \text{(c) } A &= 75 \times 10^{-4} \text{ m}^2 \stackrel{\sim}{=} 75 \text{ cm}^2 \\
 t &= 2 \times 10^{-2} \text{ m} \stackrel{\sim}{=} 2 \text{ cm}
 \end{aligned}$$

$$\text{Heat required} = mC\Delta\theta$$

$$\text{Density} = \frac{m}{V} \quad [\text{Recall } V = A \times t]$$

$$m = \text{Density} \times V$$

$$m = 0.55 \frac{\text{g}}{\text{cm}^3} \times (75 \times 2) \text{ cm}^3$$

$$m = 82.5 \text{ g}$$

$$C = \frac{\epsilon_0 \epsilon_r A}{t} = \frac{8.85 \times 10^{-12} \times 6.5 \times 75 \times 10^{-4}}{2 \times 10^{-2}}$$

$$C = 21.57 \times 10^{-12} \text{ F}$$

$$\omega = 2\pi f = 2\pi \times 20 \times 10^6 = 125.664 \times 10^6 \text{ rad/s}$$

$$\text{Power factor} = \cos \phi = 0.04$$

$$\phi = \cos^{-1}(0.04) = 87.7^\circ$$

$$\delta = 90^\circ - \phi = 90^\circ - 87.7^\circ = 2.3^\circ$$

$$\text{Heat required} = mC\Delta\theta$$

$$= 82.5 \times 0.255 \times (80 - 30)$$

$$= 1051.88 \text{ cal}$$

$$\text{Total heat required} = 1051.88 \times \frac{85}{100} = 894.098 \text{ cal}$$

$$1 \text{ cal} = 4.186 \text{ (W-3) J}$$

$$894.098 \text{ cal} = x$$

$$\text{Power input} = \frac{x}{8 \times 60} = 894.098 \times 4.186 = 3742.7 \text{ (W-3)}$$

$$P = \frac{\text{Energy}}{\text{time}} = \frac{3742.7}{8 \times 60} = 7.797 \text{ W}$$

$$P_d = V^2 WC \tan \delta$$

$$7.797 = V^2 \times 125.664 \times 10^6 \times 21.57 \times 10^{-12} \times \tan 2.3^\circ$$

$$V^2 = \frac{7.797}{1.08868 \times 10^{-4}}$$

$$V = 267.62 \text{ V} //$$

$$P = IV \cos \phi$$

$$I = \frac{7.797}{267.62 \times 0.04}$$

$$I = 0.7284 \text{ A} //$$