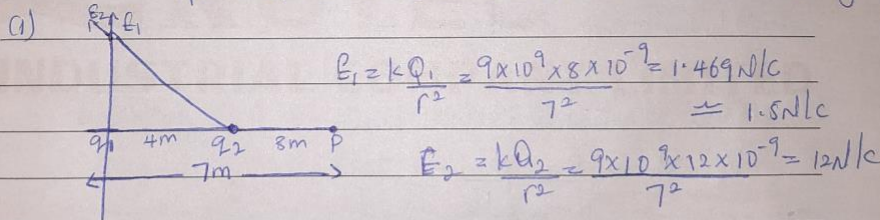


Memo

electric field	electric field intensity
A region of space around the electric charge in which electric force acts on	The measure of the strength of an electric field at any point also a force per unit charge.

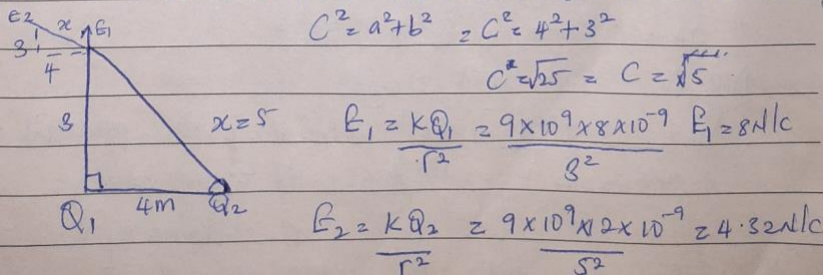
- (2b)  $q_1 = 8\text{nc}$  at origin  
 $q_2 = 12\text{nc}$  on axis at  $x = 4\text{m}$ .

i) net electric field at point P on the axis at  $x = 7\text{m}$  while on point Q on the Y axis at  $y = 3\text{m}$  due to the charges.



$$E_{\text{net}} = E_1 + E_2 = 1.5 + 12 \text{N/C} = 13.5 \text{N/C}$$

(ii) E at Point Q on the Y axis at  $y = 3\text{m}$  due to charge.



Memo

Vector	angle	x-comp	y-comp
$E_1 = 8 \text{ N/C}$	$90^\circ$	$0 \text{ N/C}$	$8 \text{ N/C}$
$E_2 = 4.32$	$36.87^\circ$	$-3.45 \text{ N/C}$	$2.59 \text{ N/C}$
$E_{\text{net}} = \sqrt{E_{fx}^2 + E_{fy}^2}$		$\Sigma x = -3.45 \text{ N/C}$	$\Sigma y = 10.59 \text{ N/C}$
$E_{\text{net}} = 11.12 \text{ N/C}$			

(3) Formulation of densities of charge.

a) Volume charge density  $\rho = \frac{dq}{dv} = dQ = \rho dv$ .

ii) Surface charge density  $\sigma = \frac{dq}{dA} = dQ = \sigma dA$

iii) Linear charge density  $\lambda = \frac{dq}{dL} = dQ = \lambda dL$ .

(6) Electric potential difference equation.

$$V_B - V_A = \frac{Q}{4\pi\epsilon_0} \left[ \frac{1}{r_B} - \frac{1}{r_A} \right]$$

where  $Q = \text{point charge}$ .

$r_B = \text{distance of } Q \text{ to point B}$

$r_A = \text{distance of } Q \text{ to point A}$

Due to Several point charges.

$$V_p = \frac{1}{4\pi\epsilon_0} \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right] \text{ where } V = \text{electric potential.}$$

$Q = \text{point charge}$

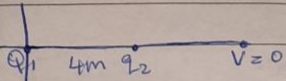
$r = \text{distance of } Q$ .

(7) Point charge  $Q_1 = 10 \mu\text{C}$   $Q_2 = -2 \mu\text{C}$  along x-axis  $x = 0$ .

$x = 4 \text{ m}$  find its position along the x-axis where  $V = 0$ .

20 YEARS  
OF ACCOMPLISHMENT

Memo



$$V_p = k \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$V_p = 9 \times 10^9 \times \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = 9 \times 10^9 \times \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4+x} = \frac{2 \times 10^{-6}}{x}$$

$$10 \times 10^{-6} x = (4+x) (2 \times 10^{-6})$$

$$10 \times 10^{-6} x = 8 \times 10^{-6} + 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 10 \times 10^{-6} x - 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 8 \times 10^{-6} x$$

$$x = \frac{8 \times 10^{-6}}{8 \times 10^{-6}} = 1$$

Position along the x-axis is 1m.

where  $V=0$ .

$$V = k \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$0 = \left[ \frac{10 \times 10^{-6}}{4-x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$\frac{2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4-x}$$

Memo

$$[4-x][2 \times 10^6] = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} - 2 \times 10^{-6} x = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} = 10 \times 10^{-6} x + 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 12 \times 10^{-6} x$$

$$x = \frac{8 \times 10^6}{12 \times 10^{-6}}$$

$$x = 0.67 \text{ m}$$

$$\text{Position of } \sqrt{2} \text{ is } 0.67 \text{ m}$$

4a) Magnetic flux is defined as the strength of the magnetic field which can be represented by line of forces. It is denoted as  $\phi$ .

$$\phi = B \cdot dA$$

4b)  $m_e = 9.11 \times 10^{-31} \text{ kg}$ ,  $r = 1.4 \times 10^{-7} \text{ m}$ ,  $B = 3.5 \times 10^{-1} \text{ W/m}^2$

Cyclotron frequency = angular speed  $\therefore \omega = 1.6 \times 10^{-19}$

$$F_B = qvB = \frac{m_e v^2}{r}$$

$$m_e v = qBr$$

$$v = \frac{qBr}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1} \times 1.4 \times 10^{-7}}{9.11 \times 10^{-31}}$$

$$v = 8.61 \times 10^{-3} \text{ m/s}$$

$$\omega = \frac{v}{r} = \frac{qB}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\omega = 6.14 \times 10^{10} \text{ s}^{-1}$$

4c) Mass of electron =  $9.11 \times 10^{-31} \text{ kg}$

Memo

$r_{\text{radius}} = 1.4 \times 10^{-7} \text{ m}$

$B = 3.5 \times 10^{-10} \text{ T/m}^2$

and we were asked to find the Cyclotron frequency which is the same thing as angular speed. It is called cyclotron frequency because it is a frequency of an accelerator called cyclotron.

Recall  $\omega = \text{angular speed}$

$\omega = qB$ . Since Cyclotron frequency = angular speed.

So the Cyclotron frequency =  $6.14 \times 10^{10} \text{ s}^{-1}$

having a unit of  $\frac{1}{\text{T}}$  which is the unit of frequency dimensionally.

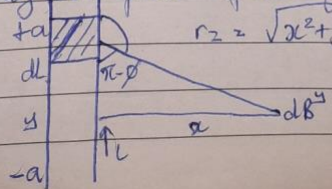
(5a) Biot-Savart law states that the magnetic field is directly proportional to the product permeability of free space ( $\mu_0$ ) the current ( $I$ ), the change in length, the radius - and inversely proportional to square of radius ( $r^2$ ). Mathematically:

$$dB = \frac{\mu_0 I dl \times \hat{r}}{4\pi r^2}$$

where  $\mu_0$  permeability of free space =  $4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$ ,  
 $r$  = radius.  $I$  = steady current

$dB$  = magnetic field  $dl$  = length of wire unit is  $\text{colm}^2$

(5b) Magnetic field of a straight current carrying conductor.



$r = \sqrt{x^2 + y^2}$

A section of a straight current carrying conductor.

Memo

Applying Bio - Savart law, we find magnitude of the field

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \phi}{r^2}$$

$$\sin(\pi - \phi) = \sin \phi$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{r^2}$$

From the diagram  $r^2 = x^2 + y^2$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{x^2 + y^2} \quad \text{--- (i)}$$

$$\text{But } \sin(\pi - \phi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- (ii)}$$

Substitute (ii) into (i)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cdot x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cdot x}{(x^2 + y^2)^{3/2}} \quad dy \leftarrow +1 \rightarrow (iii)$$

$$dl = dy ; B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} \quad \text{--- (iii)}$$

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi x} \left[ \frac{2a}{(x^2 + a^2)^{1/2}} \right] ; (x^2 + a^2)^{1/2} = a = \infty$$

$$B = \frac{\mu_0 I}{2\pi x} = \frac{\mu_0 I}{2\pi r}$$

14 Apr 2020