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COURSE: FLUID MECHANICS

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Assignment

* Question 1

Solution

pressure head at smaller end = 2.5m P_1/ρ

Length of tube = 2.0m h_L

velocity of flow at lower end = 5ms^{-1} v_1

velocity of flow at higher end = 2ms^{-1} v_2

$$\text{loss of head} = \frac{0.35 (v_1 - v_2)^2}{2g} h_L$$

$$\text{loss of head} = \frac{0.35 (5 - 2)^2}{2 \times 9.81} = 0.16\text{m}$$

Pressure head head at higher end, $\frac{P_2}{\rho}$

$$\frac{P_1}{\rho} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{v_2^2}{2g} + z_2 + h_L$$

$$z_2 = 0, \quad z_1 = 2.0\text{m}$$

$$2.5 + \frac{5^2}{2 \times 9.8} + 2 = \frac{P_2}{\rho} + \frac{2^2}{2 \times 9.8} + 0.16$$

$$\therefore 5.775 = \frac{P_2}{\rho} + 0.364$$

$$\frac{P_2}{\rho} = 5.775 - 0.364 = 5.411\text{m of liquid}$$

Pressure head at higher end = 5.411m

Q. Inlet diameter = 20cm = 0.2 m
 throat diameter = 10cm = 0.1 m
 Pressure at inlet = 17.658 N/cm² = 176.58 kN/m²
 30cm of mercury
 $C_d = 0.98$ coefficient of discharge = 0.98

Solution

$$\text{Area of inlet } A_1 = \frac{\pi}{4} \times 0.2^2 = 0.0314 \text{ m}^2$$

$$\text{Area of throat } A_2 = \frac{\pi}{4} \times 0.1^2 = 0.00785 \text{ m}^2$$

$$\frac{P_1}{\rho} = \frac{176.58}{9.8} = 18.01 \text{ m}$$

Vacuum pressure at the throat,

$$\frac{P_2}{\rho} = -300 \text{ mm} = -300 - 0.3 \times 13.6 = -4.08 \text{ m of water}$$

$$\text{Differential head, } h = \frac{P_1}{\rho} - \frac{P_2}{\rho} = 18.01 - (-4.08) = 22.09 \text{ m}$$

Rate of flow, Q:

Using the relation, $Q = C_d \times A_1 A_2$

$$\sqrt{A_1^2 - A_2^2} \times \sqrt{2gh}$$

= ~~0.98~~

$$Q = 0.98 \times 0.0314 \times 0.00785 \times \sqrt{2 \times 9.81 \times 22.09}$$

$$\sqrt{(0.0314)^2 - (0.00785)^2}$$

$$= \frac{0.000241 \times 20.82}{0.5304}$$

$$0.5304$$

$$Q = 0.165 \text{ m}^3/\text{s}$$

Discharge of water through venturimeter = 0.165 m³/s

3. Orifice diameter $A_0 = 1.5 \text{ cm} = 0.015 \text{ m}$
 Pipe diameter = $30 \text{ cm} = 0.3 \text{ m}$
 Manometer reading = 0.5 m of mercury
 S.g of oil = 0.9 $C_d = 0.64$

Solution

Area of orifice, $\frac{\pi}{4} \times 0.015^2 = 0.000177 \text{ m}^2 = A_0$

Area of pipe, $\frac{\pi}{4} \times 0.3^2 = 0.0707 \text{ m}^2 = A_1$

Differential head, $h = y \left[\frac{S_m}{S_o} - 1 \right]$

$= 0.5 \left[\frac{13.6}{0.9} - 1 \right] = 7.06 \text{ m of oil}$

Discharge Q :

Using the relation, $Q = C_d \times \frac{A_0 \cdot A_1 \cdot \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}}$

$Q = \frac{0.64 \times 0.0707 \times 0.000177 \times \sqrt{2 \times 9.8 \times 7.06}}{\sqrt{(0.0707)^2 - (0.000177)^2}}$

$= \frac{0.0942}{0.0707} = 0.133 \text{ m}^3/\text{s}$

Rate of oil discharge = $0.133 \text{ m}^3/\text{s}$

4. Reading of manometer, $y = 170\text{mm} = 0.17\text{m}$ of mercury
Sp. gravity of mercury, $S_{H_2O} = 13.6$
Sp. gravity of sea water, $S_s = 1.026$

To find the head, (h), using the relation;

$$h = y \left[\frac{S_{H_2O}}{S_s} - 1 \right] \text{ we have:}$$

$$h = 0.17 \left[\frac{13.6}{1.026} - 1 \right] = 2.08$$

\therefore Velocity Speed of the submarine,

$$v = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.08} = 6.38\text{m/s}$$

Solution

$$5. \text{ Actual flow rate} = 0.05 \text{ m}^3/\text{min} = 0.05/60 = \overset{8.3 \times 10^{-4} \text{ m}^3/\text{sec}}{\cancel{8.33}}$$

$$\text{Pressure charge} = 15 \text{ bar} = 15 \times 10^5 \text{ N/m}^2$$

$$\text{Speed of rotation} = 1700 \text{ rev/min} = 1700/60 = 28.3 \text{ rps}$$

$$\text{Normal displacement} = 10 \text{ cm}^3/\text{rev} = 1 \times 10^{-5} \text{ m}^3/\text{rev}$$

$$\text{Torque input} = 15 \text{ Nm}$$

$$\text{Ideal flow rate} = \text{normal} \times \text{speed displacement}$$

$$= 28.3 \times 1 \times 10^{-5}$$

$$= 2.83 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$i) \text{ Volumetric efficiency} = \frac{\text{Actual flow rate} \times 100\%}{\text{Ideal flow rate}}$$

$$= \frac{8.3 \times 10^{-4} \times 100}{2.83 \times 10^{-4}}$$

$$= \cancel{34.096\%} \approx 296\%$$

$$ii) \text{ Fluid Power} = Q \cdot \Delta P$$

$$= 8.3 \times 10^{-4} \times 15 \times 10^5$$

$$= 1245 \text{ Watts or Nm/sec}$$

$$iii) \text{ Shaft power} = T \cdot \omega$$

where T = Torque input

ω = angular speed =

$$T = 15 \text{ Nm}$$

$$\omega = 2\pi N \text{ for rps}$$

$$\omega = \frac{2\pi N}{60} \text{ for rpm}$$

$$\omega = \frac{2 \times 3.14 \times 28.3}{7} = 177.89 \text{ rad/sec}$$

Shaft po

$$\text{Shaft power} = 15 \times 177.89$$

$$= 2668.35 \text{ Watts}$$

$$\begin{aligned} \text{ii) Overall efficiency} &= \frac{\text{Fluid power}}{\text{Shaft power}} \times 100 \\ &= \frac{1245}{2668.35} \times 100 \\ &= 46.66\% \end{aligned}$$