

when $x = 1$ and $y = 2$.

$$\frac{dy}{dx} = \frac{-8(1) - 2(2)^3}{6(1)(2)^2 - 10(2)} = \frac{-8 - 16}{24 - 20} = \frac{-24}{4}$$

$$\frac{dy}{dx} = -6$$

$$8x + (6xy^2 - 10y^2) \frac{dy}{dx} = -8x - 2y^2$$

$$6xy^2 \frac{dy}{dx} - 10y^2 \frac{dy}{dx} = -8x - 2y^2$$

$$\frac{dy}{dx} (6xy^2 - 10y^2) = -8x - 2y^2$$

$$\frac{dy}{dx} = \frac{-8x - 2y^2}{6xy^2 - 10y^2}$$

The nature of stationary point

$$\frac{d^2y}{dt^2} = \frac{8t^3 - 12t^2 + 216t - 72}{(6-2t)^3}$$

$$\text{at } t=0$$

$$\frac{d^2y}{dt^2} = \frac{-72}{216} = -\frac{1}{3}$$

at $t=0$, we have maximum point

$$\text{at } t = 4.3028$$

$$\frac{d^2y}{dt^2} = -9.14028$$

at $t = 4.3028$ we have maximum point

$$\text{at } t = 0.6972$$

$$\frac{d^2y}{dt^2} = 0.474$$

at $t = 0.6972$, we have minimum point



1. STATIONARY POINT $\Rightarrow t = 0, t = \frac{5 + \sqrt{13}}{2}$ or $t = \frac{5 - \sqrt{13}}{2}$

2. for the coordinates of stationary point.

At $t = 0$

$$y = \frac{(0)^3 - 0^2}{2 - 2(0)} + 4 = 0$$

At $t = \frac{5 + \sqrt{13}}{2}$

$$y = \frac{(4.3028)^3 - (4.3028)^2}{2 - 2(4.3028)} + 4 = 61.1483$$

$$y = 23.468$$

At $t = \frac{5 - \sqrt{13}}{2}, 0.6972$

$$y = \frac{(0.6972)^3 - (0.6972)^2}{2 - 2(0.6972)} + 4$$

$$y = -0.03196$$

$(0, 0)$

$(4.3028, 23.468)$

$(0.6972, -0.03196)$

Find a maximum point

$$y = t^3 - t^2$$

$$2 - 2t + 4$$

Find stationary point

ii. Coordinates of the stationary point.

iii. Nature of the stationary point of the curve.

$$\text{at stationary point } \frac{dy}{dt} = 0$$

$$\frac{dy}{dt} = \frac{1}{\sqrt{x}} \cdot \frac{dy}{dx} \quad \frac{dx}{dt} = 3t^2 - 2t \quad \frac{dy}{dx} = -2$$

$$\frac{dy}{dt} = \frac{2 - 2t + 4(8t^2 - 2t)}{(2 - 2t + 4)^2} - (3t^2 - 2t)(-2)$$

$$\frac{dy}{dt} = \frac{6t^2 - 6t^3 + 12t^2 - 4t + 14t^2 + 8t + 12t^3 + 2t^2}{(2 - 2t + 4)^2}$$

$$\frac{dy}{dt} = \frac{20t^2 - 4t^3 - 12t}{(6 - 2t)^2}$$

$$\frac{20t^2 - 4t^3 - 12t}{(6 - 2t)^2} = 0 \quad ; \quad \frac{20t^2 - 4t^3 - 12t}{36 - 24t + 4t^2} = 0 \quad ; \quad \frac{10t^2 - 2t^3 - 6t}{18 - 12t + 2t^2} = 0$$

$$\frac{5t^2 - t^3 - 3t}{(3 - t)^2} = 0$$

$$5t^2 - t^3 - 3t = 0 \quad ; \quad t \times (5t - t^2 - 3) = 0$$

$$t = 0$$

$$5t - t^2 - 3 = 0$$

$$t = 0, 1$$