

UNIVERSITY OF NIGERIA
COUNCIL OF STUDENTS

COMPUTER ENGINEERING

MATRIC NO: 19/ENG02/067

MAT 104

S.N: 32

$$1) \quad y = \frac{t^3 - t^2}{2} - 2t + 4$$

$$\frac{dy}{dt} = 3t^2 - t - 2$$

At stationary points, $\frac{dy}{dt} = 0$

$$3t^2 - t - 2 = 0$$

$$3t^2 - 3t + 2t - 2 = 0$$

$$3t(t-1) + 2(t-1) = 0$$

$$(3t+2)(t-1) = 0$$

$$3t = -2 \quad t = 1$$

$$t = -2/3$$

When $t = -2/3$

$$y = \frac{3(-2/3)^3 - (-2/3)^2}{2} - 2(-2/3) + 4$$

$$y = \frac{(-2/3)^3 - (-2/3)^2}{2} - 2(-2/3) + 4$$

$$y = \frac{130}{27}$$

When $t = 1$

$$y = \frac{(1)^3 - (1)^2}{2} - 2(1) + 4$$

$$y = \frac{5}{2}$$

The coordinates of the stationary points are $(-2/3, 130/27)$ and $(1, 5/2)$

$$\frac{d^2y}{dt^2} = 6t - 1$$

When $t = -2/3$

$$\frac{d^2y}{dt^2} = 6(-2/3) - 1 = -5$$

At $(-2/3, 130/27)$ we have a maximum point

When $t = 1$

$$\frac{d^2y}{dt^2} = 6(1) - 1 = 5$$

At $(1, \frac{5}{2})$ we have a minimum point.

$$2) \quad 2y^2 - 5x^4 - 2 - 7y^3 = 0$$

$$4y \cdot \frac{dy}{dx} - 20x^3 - 21y^2 \cdot \frac{dy}{dx} = 0$$

$$4y \cdot \frac{dy}{dx} - 21y^2 \cdot \frac{dy}{dx} = 20x^3$$

$$\frac{dy}{dx} (4y - 21y^2) = 20x^3$$

$$\frac{dy}{dx} = \frac{20x^3}{4y - 21y^2}$$

$$3) \quad 4x^2 + 2xy^3 - 5y^2 = 0$$

$$8x + 6xy^2 \cdot \frac{dy}{dx} + 2y^3 - 10y \cdot \frac{dy}{dx} = 0$$

$$6xy^2 \cdot \frac{dy}{dx} - 10y \cdot \frac{dy}{dx} = -8x - 2y^3$$

$$\frac{dy}{dx} (6xy^2 - 10y) = -8x - 2y^3$$

$$\frac{dy}{dx} = \frac{-8x - 2y^3}{6xy^2 - 10y}$$

When $x = 1$ and $y = 2$

$$\frac{dy}{dx} = \frac{-8(1) - 2(2)^3}{6(1)(2)^2 - 10(2)}$$

$$\frac{dy}{dx} = \frac{-8 - 16}{24 - 20}$$

$$\frac{dy}{dx} = -6$$