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COURSE: MATHS 104

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2a) $\int \frac{2x}{\sqrt{4x^2-1}} dx$

let $u = \sqrt{4x^2-1} = (4x^2-1)^{1/2}$

$\frac{du}{dx} = (4x^2-1)^{-1/2}$

$du = 4x(4x^2-1)^{-1/2} dx$

$dx = \frac{du}{4x(4x^2-1)^{-1/2}} = \frac{(4x^2-1)^{1/2} dx}{4x}$

we have

$2 \int \frac{x}{u} dx = 2 \int \frac{x}{(4x^2-1)^{1/2}} \cdot \frac{(4x^2-1)^{1/2} dx}{4x} du$

$= \frac{1}{2} \int du$

$= \frac{1}{2} u + C = \frac{1}{2} \sqrt{4x^2-1} + C$

2) $\int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx$

$= \int \sin^{-1} x \cdot (1-x^2)^{-1/2} dx$

let $u = \sin^{-1} x$

$du = (1-x^2)^{-1/2} dx$

$\int u du = \frac{u^2}{2} + C$

$= \frac{(\sin^{-1} x)^2}{2} + C$

$$3) \int (\tan x)^b \sec^2 x \, dx$$

$$\text{let } u = \tan x$$

$$du = \sec^2 x \, dx$$

we have

$$\int u^b \, du = \frac{u^{b+1}}{b+1} + C \quad \text{or} \quad \frac{(\tan x)^{b+1}}{b+1} + C$$