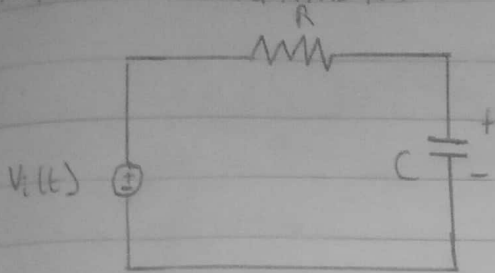


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17/ENG05/030

MECHATRONICS ENGINEERING

ENG 322 ASSIGNMENT



Determine the type of filter shown above and show that its cutoff frequency is  $\omega_c = \frac{1}{RC}$

Solution

Converting to frequency domain

$$R = R$$

$$C = \frac{1}{j\omega C}$$

$$H(\omega) = \frac{V_o}{V_i}$$

Using KVL (series connection)

$$H(\omega) = \frac{V_o}{V_i} = \frac{\frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} = \frac{\frac{1}{j\omega C}}{\frac{Rj\omega C + 1}{j\omega C}}$$

$$H(\omega) = \frac{1}{1 + j\omega RC}$$

When  $H(0) = 1$ ,  $H(\infty) = 0$

The half power frequency which is equivalent to the corner frequency on the BODE plots but in the context of filters is called CUT-OFF FREQUENCY.

$\omega_c$  is obtained by setting magnitude of  $H(\omega) = \frac{1}{\sqrt{2}}$

Substituting  $\omega_c$

$$H(\omega_c) = \frac{1}{\sqrt{1 + \omega_c^2 R^2 C^2}} = \frac{1}{\sqrt{2}}$$

Square both sides

$$\frac{1^2}{1 + \omega_c^2 R^2 C^2} = \frac{1}{2}$$

$$2 \cdot 1^2 = 1 + \omega_c^2 R^2 C^2$$

$$2 = 1 + \omega_c^2 R^2 C^2$$

$$2 - 1 = \omega_c^2 R^2 C^2$$

$$1 = \omega_c^2 R^2 C^2$$

Taking square root of both sides

$$\sqrt{1} = \sqrt{\omega_c^2 R^2 C^2}$$

$$1 = \omega_c RC$$

$$\therefore \omega_c = \frac{1}{RC}$$