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$$1) \int \frac{2x}{\sqrt{4x^2-1}} dx.$$

Solution.

$$\int 2x \cdot (4x^2-1)^{-1/2} \cdot dx.$$

$$\text{Let } u = 4x^2 - 1$$

$$\frac{du}{dx} = 8x$$

$$du = 8x dx$$

$$dx = \frac{du}{8x}$$

$$\therefore = \int \frac{1}{\cancel{2x}} \cdot u^{-1/2} \cdot \frac{du}{\cancel{8x} \cdot 4}$$

$$= \frac{1}{4} \int u^{-1/2} \cdot du$$

$$= \frac{1}{4} \left[\frac{u^{1/2}}{1/2} \right] + C$$

$$= \frac{1}{\frac{4}{2}} \left[\frac{1}{2} u^{1/2} \right] + C$$

$$= \frac{1}{2} \sqrt{4x^2-1} + C$$

$$2) \int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx$$

Solution.

$$\int \sin^{-1} x \cdot \frac{1}{\sqrt{1-x^2}} dx$$

$$\text{Let } u = \sin^{-1} x \quad \therefore x = \sin u$$

$$\frac{dx}{du} = \cos u$$

$$\text{but } \sin^2 u + \cos^2 u = 1$$

$$\cos^2 u = 1 - \sin^2 u$$

$$\cos^2 u = 1 - x^2$$

$$\cos u = \sqrt{1-x^2}$$

$$\frac{dx}{du} = \sqrt{1-x^2}$$

$$dx = \sqrt{1-x^2} \, du$$

$$du = \frac{1}{\sqrt{1-x^2}} \cdot dx$$

$$= \int u \cdot du$$

$$= \frac{u^2}{2} + c$$

$$= \frac{(\sin^{-1} x)^2}{2} + c$$

$$3) \int (\tan x)^6 \sec^2 x \, dx$$

Solution

$$\int (\tan x)^6 \sec^2 x \, dx$$

$$\text{Let } u = \tan x$$

$$\frac{du}{dx} = \sec^2 x$$

$$du = \sec^2 x \, dx$$

$$dx = \frac{du}{\sec^2 x}$$

$$\therefore \int u^6 \cdot du$$

$$= \left[\frac{u^7}{7} \right] + c$$

$$= \frac{(\tan x)^7}{7} + c$$