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$$\textcircled{1} \int \frac{2x}{\sqrt{4x^2-1}} dx = \frac{1}{2} \sqrt{4x^2-1} + c$$

$$\text{let } u = \sqrt{4x^2-1} = (4x^2-1)^{1/2}$$

$$\frac{du}{dx} = \frac{1}{2} (4x^2-1)^{-1/2} \cdot 8x$$

$$\frac{du}{dx} = 4x (4x^2-1)^{-1/2}$$

$$dx = \frac{du}{4x(4x^2-1)^{-1/2}} = \frac{(4x^2-1)^{1/2}}{4x} du$$

we have

$$2 \int \frac{x}{u} dx = 2 \int \frac{x}{(4x^2-1)^{1/2}} \cdot \frac{(4x^2-1)^{1/2}}{4x} du$$

$$= \frac{1}{2} \int du$$

$$= \frac{1}{2} u + c$$

$$= \frac{1}{2} \sqrt{4x^2-1} + c$$

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$$\textcircled{2} \int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx = \frac{(\sin^{-1} x)^2}{2} + C$$

where $\int \sin^{-1} x \cdot (1-x^2)^{-1/2} dx$

let $u = \sin^{-1} x$

$$du = (1-x^2)^{-1/2} dx$$

$$\int u du = \frac{u^2}{2} + C$$

$$= \frac{(\sin^{-1} x)^2}{2} + C$$

$$\textcircled{3} \int (\tan x)^6 \sec^2 x dx \Rightarrow \begin{aligned} u \tan x \\ du = \sec^2 x dx \\ u^6 du = \frac{u^7}{7} \end{aligned}$$

let $u = \tan x$

$$du = \sec^2 x dx$$

we have

$$\int u^6 du = \frac{u^7}{7} + C$$

$$= \frac{(\tan x)^7}{7} + C$$