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 181ENG01/008
 CHEMICAL ENGINEERING
 FLUID MECHANICS

1) $L = 2.0\text{m}$

V_1 (smaller end) $= 5\text{m/s}$

V_2 (lower end) $= 2\text{m/s}$

$h = \frac{0.35 (V_1 - V_2)^2}{2g}$

Ph at smaller head $= 2.5\text{m}$

$\frac{P_2}{w} = \frac{P_1}{w} + \frac{(V_1^2 + V_2^2)}{2g} + (z_1 - z_2)h$

$= 2.5 + \frac{5^2 - 2^2}{2 \times 9.81} + 2 - \frac{0.5 (5 - 2)^2}{2 \times 9.81}$

$= 2.5 + 1.07 + 2 - 0.16055$

Pressure at lower head $= 5.409\text{bar} \approx 5.41\text{bar}$

2) Inlet diameter $= 0.2\text{m}$

Throat diameter $= 0.1\text{m}$

$C_d = 0.98$

$A_1 = \frac{\pi d^2}{4} = \frac{\pi \times 0.2^2}{4} = 0.314\text{m}^2$

$A_2 = \frac{\pi d^2}{4} = \frac{\pi \times 0.1^2}{4} = 7.85 \times 10^{-3}\text{m}^2$

$h = \frac{P_1}{w} - \frac{P_2}{w}$

$\frac{P_1}{w} = \frac{1.765 \times 10^{-2} \text{Nm}}{9.81}$

$= 1.799 \times 10^{-3}$

$$\frac{P_2}{\rho} = 0.8 \times 13.6 = -4.08$$

$$h = \frac{P_1}{\rho} = \frac{P_2}{\rho} = 1.799 \times 10^{-5} - (-4.08)$$

$$= 4.082 \text{ m}$$

$$\therefore Q = 0.98 \times 0.0314 \times 7.85 \times 10^{-3} \times \sqrt{(0.0314)^2 - (7.85 \times 10^{-3})^2} \times \sqrt{2 \times 9.81 \times 4.082}$$

$$Q = 0.0002415 \times 8.949$$

$$Q = \frac{0.00216}{0.0303}$$

$$= 0.0713 \text{ m}^3/\text{s}$$

$$3) D_1 = 0.15 \text{ m}$$

$$D_2 = 0.3 \text{ m}$$

$$S.G. = 0.9$$

$$C_d = 0.64$$

$$A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.0176 \text{ m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.07069 \text{ m}^2$$

$$h = 0.5 \left[\frac{13.6}{0.9} - 1 \right]$$

$$= 7.05 \text{ m}$$

$$Q = \frac{C_d A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$= \frac{0.64 \times 0.0176 \times 0.07069}{\sqrt{(0.0176)^2 - (0.07069)^2}} \times \sqrt{2 \times 9.81}$$

$$= \frac{0.0007996 \times 11.7609}{\sqrt{0.000309 - 0.00499}}$$

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4) Axis = 15m

170mm of mercury (0.17m)

5g of mercury 13.6

5g of sea water = 1.026

$$h = 0.19 \left[\frac{13.6}{1.026} - 1 \right]$$

$$h = 2.083m$$

$$V = \sqrt{2gh}$$

$$V = \sqrt{2 \times 9.81 \times 2.083}$$

$$V = 6.39m/s$$

5) $Q = 0.5 dm^3/min = 8.33 \times 10^{-5} m^3/sec$

Speed of rotation = 1700 Rev/min = 28.3 Rev/sec

Normal displacement = 10 cm³/rev = 10⁻⁵ m³/rev

Torque Input = 15 Nm

Pressure change = 15 bar = 15 × 10⁵ N/m²

Ideal flow rate = Nominal displacement × Speed rotation
 $= 10^{-5} \times 28.3 = 2.83 \times 10^{-4} m^3/sec$

a) Volumetric Efficiency = $\frac{\text{Actual flow rate}}{\text{Ideal flow rate}} \times 100$
 $= \frac{8.33 \times 10^{-5} \times 100}{2.83 \times 10^{-4}}$
 $= 29.45\%$

b) Fluid power, $PF = Q \times \Delta P$
 $= 3.33 \times 10^{-5} \times 15 \times 10^5 = 124.95 \text{ watts}$

c) Shaft power $P = T \times \omega$

$\omega = 2 \times \pi \times \text{Speed of Rotation}$

$\omega = 2 \times \pi \times 28.3$

$\omega = 177.81 \text{ rad/sec}$

$\therefore \text{Shaft Power} = 15 \times 177.81 = 2667.2 \text{ watts}$

d) Overall efficiency = $\frac{\text{Fluid Power} \times 100}{\text{Shaft Power}}$
 $= \frac{124.95}{2667.2} \times 100$
 $= 4.68\%$