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17/ENG04/070

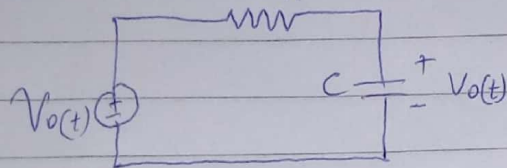
ELECTRICAL/ELECTRONICS

CIRCUIT THEORY II (EFE 320)

Assignment 1

Determine the type of filter shown below, and show that its cut-off frequency is:

$$\omega_c = 1/RC$$



Answer

This is a low-pass filter. A typical low-pass filter is formed when the output of an RC circuit is taken off the capacitor.

The transfer function is

$$H(s) = \frac{V_o}{V_i} = \frac{1/j\omega C}{R + 1/j\omega C}$$

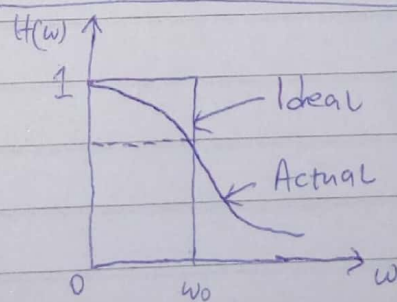
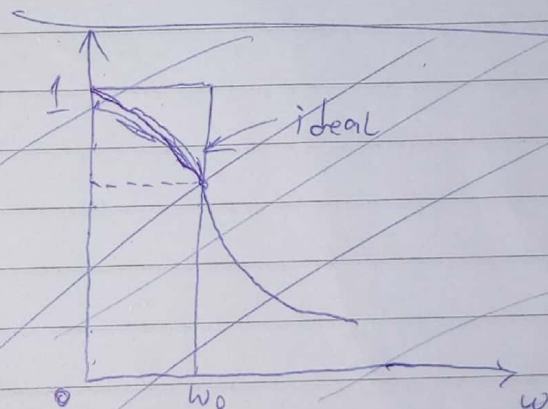
$$H(s) = \frac{1}{1 + j\omega C R}$$

Note that $H(0) = 1$, $H(\infty) = 0$

The half-power frequency, which is equivalent to the corner frequency on the Bode plots but in the context of filters is usually known as the cut-off frequency ω_c , is obtained by setting the magnitude of $H(\omega)$ equal to $1/\sqrt{2}$ thus

$$|H(\omega)| = \frac{1}{\sqrt{1 + \omega^2 R^2 C^2}} = \frac{1}{\sqrt{2}}$$

$$\omega_c = 1/RC$$



Ideal and actual frequency response of lowpass filter.

The cut-off frequency is also called the roll off frequency.