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MATRIC: 121ENC05/004

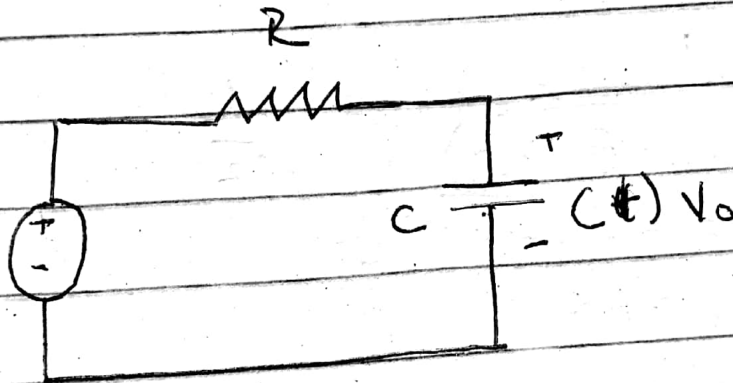
DEPT: MECHATRONICS ENGINEERING

Course: ENG322

①

Demonstrate the type of filter shown below and show that its cut off frequency

$$\omega_c = 1/RC$$



Soln

It's a low pass filter

$$H(\omega) = \frac{V_c}{V_i} = \frac{1/j\omega C}{R + 1/j\omega C}$$

$$\frac{1}{j\omega C} \times \frac{1}{R + 1/j\omega C}$$

$$= \frac{1}{1 + Rj\omega C}$$

$$H(0) = 1$$

$$H(\infty) = 0$$

(2)

The cut off frequency, ω_c

$$|H(\omega)| = \frac{1}{5RC + 1} = \frac{1}{\sqrt{3}}$$

$$= \frac{\sqrt{1^2}}{\sqrt{1^2 + (\omega_c RC)^2}} = \frac{1}{\sqrt{2}}$$

$$= \frac{1}{\sqrt{1 + (\omega_c^2 R^2 C^2)}} = \frac{1}{\sqrt{2}}$$
$$\sqrt{2} = \sqrt{1 + \omega_c^2 R^2 C^2}$$

$$2 = 1 + \omega_c^2 R^2 C^2$$

$$\omega_c^2 R^2 C^2 = 1$$

$$\Rightarrow \omega_c = \frac{1}{RC}$$