

INT. ASS.  
19/MHS01/090.

$$= 2 \int \frac{x}{(4x^2-1)^{3/2}} \cdot \frac{(4x^2-1)^{1/2} du}{4x}$$

$$= \frac{2}{4} \int du$$

$$= \frac{1}{2} \int du$$

$$= \frac{1}{2} u + c$$

$$\int \frac{2x}{\sqrt{4x^2-1}} dx = \frac{1}{2} (4x^2-1)^{1/2} + c$$

2.  $\int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx$

$$= \int \sin^{-1} x \cdot (1-x^2)^{-1/2} dx$$

let  $u = \sin^{-1} x$

$$du = (1-x^2)^{-1/2} dx$$

$$\int \sin^{-1} x \cdot (1-x^2)^{-1/2} dx = \int u du$$

$$= \frac{u^2}{2} + c$$

$$\int \sin^{-1} x \cdot (1-x^2)^{-1/2} dx = \frac{(\sin^{-1} x)^2}{2} + c$$

3  $\int (\tan x)^6 \sec^2 x dx$

$$\int (\tan x)^6 \sec^2 x dx = \int u^6 du$$
$$= \frac{u^7}{7} + c$$

$$\int (\tan x)^6 \sec^2 x dx = \frac{(\tan x)^7}{7} + c$$



$$\frac{-1}{4} + C = \frac{-1}{3(3x-5)^4} + C$$

$$\sqrt{2x+1} dx$$

$$\sqrt{2x+1}$$

$$2x+1$$

$$= 2dx$$

$$= u du$$

$$1$$

$$1$$

$$x^2-1$$

$$\int \sqrt{4x^2-1} dx$$

$$\text{Let } u = \sqrt{4x^2-1} = (4x^2-1)^{1/2}$$

$$\frac{du}{dx} = \frac{1}{2} (4x^2-1)^{-1/2} \cdot 8x$$

$$\frac{du}{dx} = (4x^2-1)^{1/2} \cdot 4x$$

$$\frac{du}{dx} = 4x (4x^2-1)^{-1/2}$$

$$dx = \frac{du}{4x (4x^2-1)^{-1/2}}$$

$$4x (4x^2-1)^{-1/2}$$

$$dx = \frac{(4x^2-1)^{1/2} du}{4x}$$