

$$1 \quad x = 7t^2, \quad y = 6t^2 - 4t \quad \text{and} \quad z = t - 5$$

$$r = xi + yj + zk$$

$$r = (7t^2)i + (6t^2 - 4t)j + (t - 5)k$$

$$\text{velocity} = \frac{dr}{dt}$$

$$\frac{dr}{dt} = 14ti + (12t - 4)j + \frac{k}{1}$$

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$$A = i + 3j - 4k$$

$$B = 2i - 3j + k$$

$$C = 4j - 3k$$

$$(B \times C) = \begin{vmatrix} i & j & k \\ 2 & -3 & 1 \\ 0 & 4 & -3 \end{vmatrix}$$

$$(B \times C) = i \begin{vmatrix} -3 & 1 \\ 4 & -3 \end{vmatrix} - j \begin{vmatrix} 2 & 1 \\ 0 & -3 \end{vmatrix} + k \begin{vmatrix} 2 & -3 \\ 0 & 4 \end{vmatrix}$$
$$= i(9 - 4) - j(-6 - 0) + k(8 - 0)$$
$$= 5i + 6j + 8k$$

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$$A \times (B \times C) = \begin{vmatrix} i & j & k \\ 1 & 2 & -4 \\ 5 & 6 & 8 \end{vmatrix}$$

$$\begin{aligned} A \times (B \times C) &= i \begin{vmatrix} 2 & -4 \\ 6 & 8 \end{vmatrix} - j \begin{vmatrix} 1 & -4 \\ 5 & 8 \end{vmatrix} + k \begin{vmatrix} 1 & 2 \\ 5 & 6 \end{vmatrix} \\ &= i(16 + 24) - j(8 + 20) + k(6 - 10) \\ &= 40i - 28j + 4k \end{aligned}$$

3. $R = 4 \sin 3t i + 4e^{3t} j + 7t^3 k$

$$\begin{aligned} \int R &= \int 4 \sin 3t i + \int 4e^{3t} j + \int 7t^3 k \\ &= 4i \int \sin 3t + 4j \int e^{3t} + 7k \int t^3 \\ &= \frac{4i}{3} (-\cos(3t)) + \frac{4j e^{3t}}{3} + \frac{7k t^4}{4} \\ &= -\frac{4 \cos(3t)}{3} i + \frac{4 e^{3t}}{3} j + \frac{7 t^4}{4} k \end{aligned}$$

4. $A = 7i + 2j - k$

$B = 2i + j + 4k$

$C = i + j + k$

$$\begin{aligned} (A+C) \cdot (B-A) &= [(7i+2j-k) + (i+j+k)] \cdot [(2i+j+4k) - (7i+2j-k)] \\ &= [8i+3j+0k] \cdot [-5i-j+5k] \\ &= -40 - 3 + 0 \\ &= -43 // \end{aligned}$$

$$T = \frac{\frac{dr}{dt}}{\left| \frac{dr}{dt} \right|}$$

$$r = xi + yj + zk$$

$$r = ti + t^2j + t^3k$$

$$\frac{dr}{dt} = i + 2tj + 3t^2k$$

$$\begin{aligned} \text{at } t=1, \frac{dr}{dt} &= i + 2(1)j + 3(1)^2k \\ &= i + 2(1)j + 3(1)k \\ &= i + 2j + 3k \\ &= \sqrt{1^2 + 2^2 + 3^2} \end{aligned}$$

$$= \sqrt{1+4+9}$$

$$= \sqrt{14} = 3.74$$

$$\text{Hence } T = \frac{i + 2j + 3k}{3.74}$$