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Course: fluid mechanics

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Assignment

1) pressure head at smaller end = 2.5m P₁/w

length of tube = 2.0m

Velocity of flow at higher lower end = 5ms⁻¹ V₁

Velocity of flow at higher end = 2ms⁻¹ V₂

$$\text{loss of head} = \frac{0.35(V_1 - V_2)^2}{2g} h_c$$

$$\text{loss of head} = \frac{0.35(5-2)^2}{2 \times 9.81} = 0.16\text{m}$$

Pressure head at higher end, $\frac{P_2}{w}$

$$\frac{P_1}{w} + V_1^2 + Z_1 = \frac{P_2}{w} + \frac{V_2^2}{2g} + Z_2 + h_c$$

$$Z_2 = 0, Z_1 = 2.0\text{m}$$

$$2.5 + \frac{5^2}{2 \times 9.8} + 2 = \frac{P_2}{w} + \frac{2^2}{2 \times 9.8} + 0.16$$

$$5.775 = \frac{P_2}{w} + 0.364$$

$$\frac{P_2}{w} = 5.775 - 0.364 = 5.411\text{m of liquid pressure head at higher end} = 5.411\text{m}$$

Vacuum pressure at the throat

$$P_2 = -300 \text{ mm} = -0.3 \times 13.6 = -4.08 \text{ m of water}$$

$$\text{Differential head, } h = \frac{P_1}{w} - \frac{P_2}{w} = 18.01 - (-4.08) = 22.09 \text{ m}$$

Rate of flow, Q

$$\text{Using the relation } = Q = \frac{C_d \times A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$Q = \frac{0.98 \times 0.0314 \times 0.00785}{\sqrt{(0.0314)^2 - (0.00785)^2}} \times \sqrt{2 \times 9.81 \times 22.09}$$
$$= \frac{0.000241 \times 20.92}{0.0304}$$

$$Q = 0.165 \text{ m}^3/\text{s}$$

Discharge of water through Venturimeter = $0.165 \text{ m}^3/\text{s}$

3) Orifice diameter $d_o = 15 \text{ cm} = 0.15 \text{ m}$

Pipe diameter = $30 \text{ cm} = 0.3 \text{ m}$

Manometer reading = 0.5 m of mercury

S.g of oil = 0.9 C.d = 0.64

Solution

$$\text{Area of Orifice, } \frac{\pi \times 0.15^2}{4} = 0.0177 \text{ m}^2$$

$$\text{Area of pipe, } \frac{\pi}{4} \times 0.30^2 = 0.0707 \text{ m}^2 = A_1$$

$$\text{Theoretical head, } h = y \left[\frac{S_L}{S_1} - 1 \right]$$

$$= 0.5 \left[\frac{13.6 - 1}{0.9} \right] = 7.06 \text{ m of oil}$$

Discharge Q:

$$\text{Using the relation, } Q = C_d \times A_0 \times \frac{A_1 \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}}$$

$$Q = \frac{0.64 \times 0.0707 \times 0.0707 \times \sqrt{2 \times 9.8 \times 7.06}}{\sqrt{(0.0707)^2 - (0.0177)^2}}$$

$$= \frac{0.0942}{0.707} = 0.133 \text{ m}^3/\text{s}$$

$$\text{Rate of oil discharge} = 0.133 \text{ m}^3/\text{s}$$

4) Reading of manometry $y = 170 \text{ mm} = 0.17 \text{ m}$ Mercury

Sp. gravity of mercury, $S_L = 13.6$

Sp. gravity of water, $S_1 = 1.026$

To find the head, (h) using the relation

$$h = y \left[\frac{S_L}{S_1} - 1 \right]$$

$$L = 0.17 \left[\frac{13.6 - 1}{1.026} \right] = 2.08$$

∴ Speed of the Submarine

$$V = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.08} = 6.38 \text{ m/s}$$

$$5) \text{ Actual flow rate} = 0.05 \text{ m}^3/\text{s} = 0.05/60 = 8.3 \times 10^{-4} \text{ m}^3/\text{s}$$

$$\text{Pressure charge} = 15 \times 10^5 \text{ N/m}^2$$

$$\text{Speed of rotation} = 1700 \text{ rev/min} = \frac{1700}{60} = 28.3 \text{ rev}^3$$

$$\text{Normal displacement} = 1 \times 10^{-5} \text{ m/rev}$$

$$\text{Torque input} = 15 \text{ Nm}$$

$$\begin{aligned} \text{Ideal flow rate} &= \text{normal} \times \text{speed displacement} \\ &= 28.3 \times 1 \times 10^{-5} \\ &= 2.83 \times 10^{-4} \text{ m}^3/\text{sec} \end{aligned}$$

$$\begin{aligned} \text{i) Volumetric efficiency} &= \frac{\text{Actual flow rate}}{\text{Ideal flow rate}} \times 100 \\ &= \frac{8.3 \times 10^{-4} \times 100}{2.83 \times 10^{-4}} \\ &= 296.82\% \end{aligned}$$

$$\begin{aligned} \text{ii) Fluid power} &= Q \cdot dp \\ &= 8.3 \times 10^{-4} \times 15 \times 10^5 \\ &= 1245 \text{ watts} \end{aligned}$$

$$\text{iii) Shaft Power} = T \cdot \omega$$

$T = \text{torque input}$

$\omega = \text{angular speed}$

$$T = 15 \text{ Nm}$$

$$\omega = 2\pi N \text{ rev rps}$$

$$\omega = \frac{2\pi N}{60}$$

$$\omega = \frac{2 \times 22 \times 28.3}{7} = 177.89 \text{ rev/s}$$

$$\text{Shaft Power} = 15 \times 177.89$$

$$= 2668.35 \text{ W}$$

$$\text{iv) Overall efficiency} = \frac{\text{fluid power}}{\text{shaft power}} \times 100\%$$

$$= \frac{1245}{2668.35} \times 100$$

$$= 46.66\%$$

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