

Electric charges can be obtained without touching it, by a process called electrostatic induction.

Consider a negatively charged rubber rod brought near a conducting sphere that is insulated so that the charges are shown below. The charges migrate to the side of the sphere nearest the rod. The migration is complete when the rod is removed. The sphere is now positively charged.

Assignment

15/11/20

$$1. \int \frac{2xc}{\sqrt{4x^2-1}} dx = \int \frac{2xc}{(4x^2-1)^{1/2}}$$

$$= 2 \int \frac{u}{(4x^2-1)^{1/2}} dx$$

$$u = (4x^2-1)^{1/2}$$
$$u^2 = 4x^2-1 \implies u^2+1 = 4x^2$$

$$x = \frac{\sqrt{u^2+1}}{2} \implies dx = \frac{u}{2\sqrt{u^2+1}}$$

$$\frac{dx}{du} = \frac{1}{2} \left(\frac{u^2+1}{4} \right)^{-1/2} \times \frac{u}{2}$$

$$dx = \frac{u du}{4} \left(\frac{u^2+1}{4} \right)^{-1/2}$$

$$2 \int \left(\frac{u^2+1}{4} \right)^{1/2} \times \frac{1}{4} \times \frac{u du}{4} \left(\frac{u^2+1}{4} \right)^{-1/2}$$

$$\frac{2}{4} \int \frac{u}{u} du$$

$$\frac{2}{4} \int du = \frac{1}{2} [u] + c$$

$$= \frac{\sqrt{4x^2-1}}{2} + c$$

$$2. \int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx$$

$$\int \sin^{-1} x \times \frac{\text{soln}}{(\sqrt{1-x^2})^{-1}} dx$$

$$u = \sin^{-1} x$$

$$\frac{du}{dx} = \frac{1}{\sqrt{1-x^2}}$$

$$du = \frac{dx}{\sqrt{1-x^2}}$$

$$du = (\sqrt{1-x^2})^{-1} dx$$

$$\int u du$$

$$\frac{u^2}{2} + c$$

$$= \frac{(\sin^{-1} x)^2}{2} dx$$

on an object without touching it, by a process called

rubber rod brought near a neutral (uncharged) and so that there is no conducting path to ground as between the

n^{-1}) and the

$$3. \int (\tan x)^6 \sec^2 x \, dx$$

soln

$$u = \tan x$$

$$\frac{du}{dx} = \sec^2 x$$

$$du = \sec^2 x \, dx$$

$$= \int u^6 \, du$$

$$= \left[\frac{u^7}{7} \right] + c$$

$$= \left(\frac{\tan x}{7} \right)^7 + c$$