

Day Andrew Ho 18/EN407/013 Petroleum Eng 200 level

1) $V_1 = 5 \text{ m/s}$ $V_2 = 2 \text{ m/s}$

Smaller end = 2.5m

$h = 2.0$

$$h_1 = \frac{0.35(V_1 - V_2)^2}{2g}$$

$h = z_1 - z_2 = 2.0$

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + z_2$$

$$\frac{P_2}{\rho} = \frac{P_1}{\rho} + \frac{1}{2g} (V_1^2 + V_2^2) + (z_1 - z_2)h$$

$$= 2.5 + \frac{(5^2 - 2^2)}{2 \times 9.81} + 2 = \frac{(0.35(5-2)^2)}{2 \times 9.81}$$

$$= 2.5 + 1.07 + 2 = 5.6055$$

$P_2 = 5.609 \text{ bar}$

2) Inlet diameter = 20cm

Throat diameter = 10cm

$C_d = 0.98$

Inlet, $P_1 = 17.658 \text{ N/cm}^2$

$$A_1 = \frac{\pi d^2}{4} = \frac{1}{4} \times \left(\frac{20}{100}\right)^2 \times \pi$$

$$= 0.0314 \text{ m}^2$$

$$A_2 = \frac{\pi d^2}{4} = \frac{1}{4} \times \left(\frac{10}{100}\right)^2 \times \pi$$

$$= 7.85 \times 10^{-5} \text{ m}^2$$

If $y = 30 \text{ cm}$ (0.3m) of mercury

$$P_1 = \frac{17.658}{1000} = 1.7658 \times 10^{-3} \text{ N/m}^2$$

$$\frac{P_1}{\rho} = \frac{1.7658 \times 10^{-3}}{9.81} = 1.8 \times 10^{-4} \text{ m}$$

$$\frac{P_2}{\rho} = 0.3 \times 13.6 = 4.08$$

$$h = \frac{P_1}{\rho} - \frac{P_2}{\rho} = 1.8 \times 10^{-4} - (-4.08)$$

$$= 4.08018 \text{ m}$$

$$Q = C_d \times \frac{A_1 A_2}{\sqrt{A_1 A_2}} \times \sqrt{2gh}$$

$$Q = 0.98 \times \frac{0.0314 \times 7.85 \times 10^{-5}}{\sqrt{0.0314 \times 7.85 \times 10^{-5}}} \times \sqrt{2 \times 9.81 \times 4.08}$$

$$Q = 0.98 \times \frac{0.0314 \times 7.85 \times 10^{-3}}{\sqrt{0.0314 \times 7.85 \times 10^{-3}}} \times \sqrt{2 \times 9.81 \times 4.08}$$

$$= 0.070 \text{ m}^3/\text{s}$$

③ $D_1 = 15\text{cm}$
 $D_2 = 30\text{cm}$
 $h = 0.5\text{m}$ of mercury
 $S.G. = 13.6$
 $C_d = 0.64$

$$A_1 = \frac{\pi d^2}{4} = \frac{1}{4} \times \left(\frac{15}{100}\right)^2 \times \pi$$

$$= 0.0176\text{m}^2$$

$$A_2 = \frac{\pi d^2}{4} = \frac{1}{4} \times \left(\frac{30}{100}\right)^2 \times \pi$$

$$= 0.0706\text{m}^2$$

$$h = \frac{13.6 - 1}{13.6} \times 0.5$$

$$= 0.4706\text{m}$$

$$Q = C_d \times A_1 \times A_2 \times \sqrt{2gh}$$

$$= 0.64 \times 0.0176 \times 0.0706 \times \sqrt{2 \times 9.81 \times 0.4706}$$

$$= 2.83 \times 10^{-3}\text{m}^3/\text{s}$$

4) Orifice diameter = 15cm
 Pipe diameter = ?
 $h = 0.17\text{m}$ of mercury
 $S.G. \text{ of mercury} = 13.6$
 $S.G. \text{ of sea water} = 1.026$

$$h = \frac{S.G. \text{ of mercury} - 1}{S.G. \text{ of sea water}} \times 0.17$$

$$= \frac{13.6 - 1}{1.026} \times 0.17$$

$$= 2.083\text{m}$$

$$V = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.083}$$

$$= 6.39\text{m/s}$$

⑤ $Q = 0.05\text{dm}^3/\text{min}$
 $= 8.33 \times 10^{-5}\text{m}^3/\text{s}$
 Speed of rotation = 1700 rev/min
 $= 28.3\text{ rev/s}$
 Nominal displacement = $10\text{cm}^3/\text{rev}$
 $= 10^{-3}\text{m}^3/\text{rev}$
 Torque input = 15 Nm
 Pressure change = 15 bar = $15 \times 10^5\text{N/m}^2$

$$\text{Ideal flow rate} = \text{Nominal displacement} \times \text{speed of rotation}$$

$$= 10^{-3} \times 28.3$$

$$= 2.83 \times 10^{-2}\text{m}^3/\text{s}$$