

RAJI UMMAI-SALMA ONIZE

18ENG08P020

BIOMEDICAL ENGINEERING

ANSWER

$$1] V_1 = 5 \text{ ms}^{-1}, V_2 = 2 \text{ ms}^{-1}$$

$$\text{Smaller end} = 2.5 \text{ m}, L = 2.0 \text{ m}$$

$$h_f = \frac{0.35 (V_1 - V_2)^2}{2g}$$

Lower end =

$$L = z_1 - z_2 = z_h$$

$$\frac{P_1}{w} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{w} + \frac{V_2^2}{2g} + z_2 + h_f$$

$$P_2 = P_1 + \frac{w}{2g} (V_1^2 - V_2^2) + (z_1 - z_2) h_f$$

$$= 2.5 + \frac{5^2 - 2^2}{2 \times 9.81} + 2 - \frac{0.35 (5 - 2)^2}{2 \times 9.81}$$

$$2.5 + 1.07 + 2 - 0.16055$$

$$P_2 = 5.4096 \text{ bar}$$

$$2] Q = C_d A_1 A_2 \sqrt{2gh} \\ \sqrt{A_1^2 - A_2^2}$$

$$d_2 = 20 \text{ cm} = 0.2 \text{ m}$$

$$A_1 = \frac{3.142 \times (0.2)^2}{4} = 0.03142 \text{ m}^2$$

$$d_2 = 10 \text{ cm} = 0.1 \text{ m}$$

$$A_2 = \frac{3.142 \times (0.1)^2}{4} = 7.855 \times 10^{-3} \text{ m}^2$$

$$P_1 = 17.658 \text{ cm} = 176580 \text{ N/m}^2$$

Specific gravity of mercury = 13.6

$$P_1 - P_2 = 176580$$

$$\frac{W}{P_2} = \frac{1000 \times 9.81}{18 \text{ m}}$$

$$\text{Vacuum Pressure} = P_2 = 300 \text{ mmHg}$$

$$W = 0.30 \times 13.6$$

$$P_2 = -4.08 \text{ m}$$

$$h = \frac{P_1 - P_2}{W} = \frac{176580 - (-4.08)}{1000 \times 9.81}$$

$$= 18 + 4.08 = 22.08 \text{ m}$$

$$Q = 0.98 \times 0.03142 \times 7.855 \times 10^{-3} \times \sqrt{2 \times 9.81 \times 22.08}$$

$$\sqrt{0.03142^2 - (7.855 \times 10^{-3})^2}$$

$$Q = 0.165 \approx 0.17 \text{ m}^3/\text{s}$$

3.] $D_1 = 15 \text{ cm} = 0.15 \text{ m}$
 $D_2 = 30 \text{ cm} = 0.3 \text{ m}$
 $50 \text{ cmHg} = 500 \text{ mmHg} = 0.5 \text{ m}$
 $Q = ?$ S.G. = 0.9, $C_d = 0.64$

$$A_1 = \frac{\pi d_1^2}{4} = \frac{3.142 \times (0.15)^2}{4}$$

$$= 0.0177 \text{ m}^2$$

$$= 0.0176 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{3.142 \times (0.3)^2}{4}$$

$$= 0.0706 \text{ m}^2$$

$$h = 0.5 \left[\frac{13.6 - 1}{1.026} \right]$$

$$= 7.05 \text{ m}$$

$$Q = C_d A_1 A_2 \sqrt{2gh}$$

$$\sqrt{A_1^2 - A_2^2}$$

$$Q = 0.64 \times 0.0176 \times 0.0706 \times \sqrt{2 \times 9.81 \times 7.05}$$

$$\sqrt{(0.0176)^2 - (0.0706)^2}$$

$$Q = 9.35 \times 10^{-2} \times 40.12$$

$$Q = 2.33 \times 10^{-3} \text{ m}^3/\text{s}$$

4.] Axis = 15 m
 $170 \text{ mmHg} = 0.17 \text{ m}$
S.G. of mercury = 13.6
S.G. of sea water = 1.026
 $h = 0.17 \left[\frac{13.6 - 1}{1.026} \right]$
 $h = 2.08 \text{ m}$
 $V = \sqrt{2gh}$
 $V = \sqrt{2 \times 9.81 \times 2.08}$
 $V = 6.39 \text{ m/s}$

5.] Actual flowrate = $0.05 \text{ m}^3/\text{min}$
 m^3/min to m^3/sec
 $60 \text{ sec} = 1 \text{ min}$
 $= \frac{0.05}{60}$

$$Q = 8.33 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$\text{Speed} = 1700 \text{ rev/min}$$

$$= \frac{1700}{60} = 28.33 \text{ rev/sec}$$

$$= 28.33 \text{ rps}$$

$$\text{Pressure } \delta P = 15 \text{ bars}$$

$$1 \text{ bar} = 1 \times 10^5 \text{ N/m}^2$$

$$15 \text{ bar} = \alpha$$

$$\alpha = 15 \times 10^5 \text{ N/m}^2$$

$$\delta P = 15 \times 10^5 \text{ N/m}^2$$

$$\text{Nominal displacement} = 10 \text{ cm}^3/\text{rev}$$

$$100 \text{ cm} = 1 \text{ m}$$

$$100^3 \text{ cm}^3 = 1 \text{ m}^3$$

$$10 \text{ cm}^3 = \alpha$$

$$\alpha = 10 = 1 \times 10^{-5} \text{ m}^3/\text{rev}$$

$$\frac{1000000}{1000000}$$

$$\text{Ideal flowrate} = \text{nominal} \times \text{speed}$$

$$= 1 \times 10^{-5} \times 28.33$$

$$= 2.833 \times 10^{-4} \text{ m}^3/\text{sec}$$

a) Volumetric Efficiency
 $\frac{\text{Actual flowrate}}{\text{Ideal flowrate}} \times 100\%$
 $= \frac{8.33 \times 10^{-4}}{2.833 \times 10^{-4}} \times 100\%$
 $= 2.94\%$

b) Fluid power $P_f = Q \cdot \delta P$

$$8.33 \times 10^{-4} \times 15 \times 10^5$$

$$= 1.2495 \times 10^{-7} \text{ Watts}$$

c) Shaft Power
 $T \cdot \omega$
 $T = 15 \text{ Nm}$
 $\omega = 2\pi N$
 $\omega = 2 \times 22 \times 28.33$
 $= 178.07 \text{ rad/sec}$
Shaft power = 15×178.07
 $= 2.67 \times 10^3$

d) Overall Efficiency
 $\frac{\text{Fluid power} \times 100\%}{\text{Shaft power}}$
 $\frac{1.2495 \times 10^{-7} \times 100\%}{2.67 \times 10^3}$
 $= 4.67 \times 10^{-11} \%$

4.] Axis = 15 m, $170 \text{ mmHg} = 0.17 \text{ m}$
S.G. of Hg = 13.6, S.G. of sea water = 1.026
 $= 1.026$
 $h = 0.17 \left[\frac{13.6 - 1}{1.026} \right] = 2.08 \text{ m}$
 $V = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.08}$
 $V = 6.39 \text{ m/s}$
 $6.39 \times 60 \times 6 = \frac{23009}{100}$
 $= 23.009$
Speed of submarine = 23.004 km/hr