

ENG

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Mechanical Engineering

Assignment

1)  $Z_1 = 0$

$V_1 = 5 \text{ m/s}$

$Z_2 = 2.0 \text{ m}$

$V_2 = 2 \text{ m/s}$

The pressure,  $h + \frac{P_1}{\rho} = 2.5 \text{ m}$

$\frac{P_2}{\rho} = ?$

$$h_f = 0.35 \frac{(V_1 - V_2)^2}{2g}$$
$$= \frac{0.35(5-2)^2}{2 \times 9.81} = \frac{0.35 \times 9}{2 \times 9.81}$$

$= 0.1606 \text{ m}$

Applying Bernoulli's Equation

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + Z_2 + h_f$$

$$\frac{P_2}{\rho} = \frac{P_1}{\rho} + \frac{V_1^2}{2g} + Z_1 - \frac{V_2^2}{2g} - Z_2 - h_f$$

$$= 2.5 + \frac{5^2}{2 \times 9.81} + 0 - \frac{2^2}{2 \times 9.81} - 2 - 0.1606$$

$$= 2.5 + 1.274 - 0.204 - 0.1606 - 2.0$$

$= 1.4094 \text{ m}$

$= 1.41 \text{ m}$

$\therefore h_2, \frac{P_2}{\rho} = 1.41 \text{ m}$

$= 1.41 \text{ m}$

2)  $d_1 = 20 \text{ cm} = \frac{20}{100} = 0.2 \text{ m}$ ,  $A_1 = \frac{\pi d^2}{4} = \frac{\pi (0.2)^2}{4} = 0.0314 \text{ m}^2$

$d_2 = 10 \text{ cm} = \frac{10}{100} = 0.1 \text{ m}$ ,  $A_2 = \frac{\pi d^2}{4} = \frac{\pi (0.1)^2}{4} = 0.00785 \text{ m}^2$

$$P_1 = 17.658 \text{ N/cm}^2 = 17.658 \times 10^4$$

$$= 176580 \text{ N/m}^2$$

$$P_2 = 30 \text{ cm of Mercury}$$

$$h_2 = -0.3 \text{ m of Hg}$$

$$= -0.3 \times 13.6$$

$$h_2 = -4.08$$

$$h_1 = \frac{P_1}{\rho g} = \frac{176580}{1000 \times 9.81}$$

$$= 18 \text{ m}$$

$$\therefore h = h_1 - h_2$$

$$h = 18 - (-4.08) = 18 + 4.08$$

$$h = 22.08$$

$$\therefore Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$= \frac{0.98 \times 0.0314 \times 0.00785 \times \sqrt{2 \times 9.81 \times 22.08}}{\sqrt{(0.0314)^2 - (0.00785)^2}}$$

$$Q = \frac{0.00503}{0.0304}$$

$$\therefore Q = 0.1654 \text{ m}^3/\text{s}$$

3) Orifice diameter,  $d_o = 15 \text{ cm} = 0.15 \text{ m}$

Pipe diameter,  $d_i = 30 \text{ cm} = 0.3 \text{ m}$

$$A_o = \frac{\pi d_o^2}{4} = \frac{\pi (0.15)^2}{4}$$

$$= 0.01767 \text{ m}^2$$

$$C_d = 0.64$$

$$A_i = \frac{\pi d_i^2}{4} = \frac{\pi (0.30)^2}{4}$$

$$= 0.070686 \text{ m}^2$$

Differential head:

$$y = 50 \text{ cm}$$

$$= 0.5 \text{ m}$$

$$h = \frac{p}{w} = y \left( \frac{\text{S.G. of mercury}}{\text{S.G. of oil}} - 1 \right)$$

$$= 0.5 \left( \frac{13.6}{0.9} - 1 \right)$$

$$= 0.5 (14.11) = 7.06 \text{ m}$$

$$\therefore h = 7.06 \text{ m}$$

$$\therefore Q = \frac{C_d \times A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$= \frac{0.64 \times 0.01767 \times 0.07068}{\sqrt{(0.07068)^2 - (0.01767)^2}} \times \sqrt{2 \times 9.81 \times 7.06}$$

$$= \frac{0.009407}{0.66844}$$

$$Q = 0.1374 \text{ m}^3/\text{s}$$

$$Q = 0.137 \text{ m}^3/\text{s}$$

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14) Difference of Hg (Cy)

$$y = 170 \text{ mm}$$

$$y = \frac{170}{1000} = 0.17 \text{ m}$$

$$\text{S.G. of mercury} = 13.6$$

$$\text{S.G. of Sea Water} = 1.026$$

$$\therefore h = y \left( \frac{\text{S.G. of Hg}}{\text{S.G. of seawater}} - 1 \right)$$

$$= y \left( \frac{13.6}{1.026} - 1 \right)$$

$$= 0.17 (12.255)$$

$$= 2.08 \text{ m}$$

$$\text{Velocity} = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.08}$$

$$V = 6.39 \text{ m/s}$$

$$\therefore \text{Velocity} = 6.39 \text{ m/s}$$

$$5) \text{ Actual flow rate} = 5 \text{ dm}^3/\text{min} \\ = \frac{5 \times 10^{-3} \text{ m}^3/\text{sec}}{60} \\ =$$

$$\text{Change in pressure, } \delta p = 15 \text{ bar} \\ = 15 \times 10^5 \text{ N/m}^2$$

$$\text{Speed of rotation, } N = 1700 \text{ rev/min} \\ = \frac{1700}{60} = 28.33 \text{ rev/secs}$$

$$\text{Nominal Displacement} = 10 \text{ cm}^3/\text{rev} \\ = \frac{10}{10^6} \text{ m}^3/\text{rev} \\ = 1 \times 10^{-5} \text{ m}^3/\text{rev}$$

$$\text{Torque Input, } T = 15 \text{ Nm}$$

$$i) \text{ Volumetric Efficiency} \\ = \frac{\text{Actual flow rate}}{\text{Ideal flow rate}} \times 100\%$$

$$\text{Actual flow rate} = 8.33 \times 10^{-5} \text{ m}^3/\text{sec}$$

$$\text{Ideal flow rate} = \text{speed of rotation} \times \text{nominal displacement} \\ = 28.33 \times 1 \times 10^{-5} \\ = 2.833 \times 10^{-4}$$

$$\therefore \text{ Volumetric efficiency} \\ = \frac{8.33 \times 10^{-5}}{2.833 \times 10^{-4}} \times 100\% \\ = 29.40\%$$

$$ii) \text{ Fluid Power, } P_f = Q \times \delta p \\ = 8.33 \times 10^{-5} \times 15 \times 10^5 \\ = 12495 \text{ watts}$$

iii) Shaft Power =  $T \cdot \omega$

$$T = 15 \text{ Nm}$$

$$\omega = 2\pi N \text{ rad/s}$$

$$= 2 \times \frac{22}{7} \times 28.33$$

$$= 178.07 \text{ rad/s}$$

$$\text{Shaft Power} = 15 \times 178.07$$

$$= 2671.11 \text{ watts}$$

$\therefore$  Overall efficiency

$$= \frac{\text{Fluid Power}}{\text{Shaft Power}} \times 100\%$$

$$= \frac{124.95}{2671.11} \times 100$$

$$= 4.678\%$$

$\therefore$  The Overall efficiency is 4.68% //