

Ebitu, Ukpono Friday 18/ENG04/027

Fluid Mechanics Assignment

Elect Elect Engineering

1. Length of conical tube = 2.0m

$$V_1 = 5 \text{ m/s}$$

$$V_2 = 2 \text{ m/s}$$

Pressure head of smaller end = 2.5m

$$\text{Loss of head} = \frac{0.35(V_1 - V_2)^2}{2g}$$

$$\text{Loss of head} = \frac{0.35 \times (5-2)^2}{2 \times 9.81} = \frac{0.35(3)^2}{19.62}$$

$$h_L = 0.160 \text{ m}$$

The pressure at larger end = P/w

Using Bernoulli's equation

$$\frac{P_1}{w} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{w} + \frac{V_2^2}{2g} + Z_2 + h_L$$

$$Z_1 = 2 \text{ m}, Z_2 = 0$$

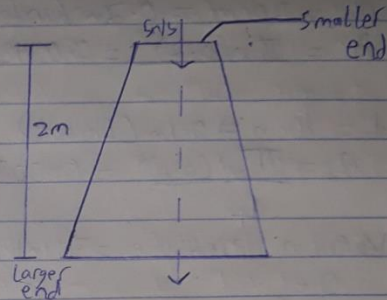
$$2.5 + \frac{5^2}{2 \times 9.81} + 2 = \frac{P_2}{w} + \frac{2^2}{2 \times 9.81} + 0 + 0.160$$

$$2.5 + 1.27 + 2 = \frac{P_2}{w} + 0.203 + 0.160$$

$$5.77 = \frac{P_2}{w} + 0.363$$

$$\frac{P_2}{w} = 5.77 - 0.363$$

$$\text{head at larger end} = \frac{P_2}{w} \Rightarrow 5.41 \text{ m}$$



$$2: \quad d_1 = 20\text{cm} = 0.2\text{m (inlet)}$$

$$A_1 = \frac{\pi \times (0.2)^2}{4} = 0.03142\text{m}^2$$

$$C_d = 0.98$$

$$P_1 = 17.658\text{N/cm}^2 = \frac{17.658}{10^{-4}}$$

$$= 176580\text{N/m}^2$$

$$d_2 = 10\text{cm} \Rightarrow 0.1\text{m (throat)}$$

$$A_2 = \frac{\pi \times (0.1)^2}{4} = 0.00785\text{m}^2$$

$$\text{Vacuum pressure} = 30\text{cmHg} \Rightarrow 0.3\text{mHg}$$

$$Q = ?$$

$$h_1 = \frac{P_1}{\rho g} = \frac{176580}{9.81 \times 1000}$$

$$\Rightarrow 18\text{m}$$

$$h_2 = \frac{P_2}{\rho} = -0.3\text{m of mercury}$$

$$\Rightarrow -0.3 \times 13.6 = -4.08\text{m of water}$$

$$h = \frac{P_1}{\rho} - \frac{P_2}{\rho} \Rightarrow 18 - (-4.08) = 22.08\text{m}$$

$$Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.98 \times 0.03142 \times 0.00785 \times \sqrt{2 \times 9.81 \times 22.08}}{\sqrt{0.03142^2 - 0.00785^2}}$$

$$Q = \frac{2.42 \times 10^{-4} \times \sqrt{433.21}}{\sqrt{9.26 \times 10^{-4}}}$$

$$Q = \frac{5.04 \times 10^{-3}}{0.0304} = 0.1658\text{m}^3/\text{s}$$

$$d_o = 15 \text{ cm} \Rightarrow 0.15 \text{ m}$$

$$d_i = 30 \text{ cm} \Rightarrow 0.30 \text{ m}$$

$$A_o = \frac{\pi \times (0.15)^2}{4} = 0.0177 \text{ m}^2$$

$$A_i = \frac{\pi \times (0.3)^2}{4} = 0.07 \text{ m}^2$$

$$h = y \left(\frac{\text{S.g. of mercury}}{\text{S.g. of oil}} - 1 \right) = 0.5 \left(\frac{13.6}{0.9} - 1 \right)$$

$$h = 7.05 \text{ m}$$

$$Q = \frac{C_d A_o \times A_i \sqrt{2gh}}{\sqrt{A_i^2 - A_o^2}}$$

$$Q = \frac{0.64 \times 0.0177 \times 0.07 \times \sqrt{2 \times 9.81 \times 7.05}}{\sqrt{0.07^2 - 0.0177^2}}$$

$$Q \Rightarrow \frac{7.9296 \times 10^{-4} \times \sqrt{138.32}}{\sqrt{4.59 \times 10^{-3}}}$$

$$Q = \frac{9.326 \times 10^{-3}}{0.068} = 0.137 \text{ m}^3/\text{s}$$

4: Reading from differential manometer = 170 mmHg = 0.17 mHg

Specific gravity of mercury = 13.6

" " " " Sea water = 1.026

$$h = y \left(\frac{\rho_m}{\rho_f} - 1 \right)$$

$$h = 0.17 \left(\frac{13.6}{1.026} - 1 \right)$$

$$h = 0.17 (12.26)$$

$$h = 2.084 \text{ m}$$

$$V = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.084} = \sqrt{40.89} \\ = 6.39 \text{ m/s}$$

$$5. \text{ Actual flow rate} = 5 \text{ dm}^3/\text{min} = 5 \text{ L}/\text{min}$$

$$\textcircled{a} \quad P = 15 \text{ bar} \quad \text{Speed} = 1700 \text{ rpm} \quad \text{Displacement} = 10 \text{ cc}/\text{rev}$$
$$\text{Torque} = 15 \text{ Nm}, \quad \text{Volumetric Efficiency} = \frac{\text{Theoretical flow}}{\text{Actual flow}} \times 100$$

$$\text{Theoretical flow} \Rightarrow \text{Displacement} \times \text{Speed}$$

$$\text{But } 10 \text{ cm}^3/\text{rev} = 10 \times 10^{-3} \Rightarrow 0.01 \text{ L}/\text{rev}$$

$$\text{Theoretical flow} = 0.01 \times 1700 \Rightarrow 17 \text{ L}/\text{min}$$

$$\text{Volumetric efficiency} = \frac{5}{17} \times 100 = 0.294 \times 100$$
$$= 29.4\%$$

$$b \quad \text{fluid power} \Rightarrow \text{pressure} \times \text{Actual flow}$$

$$= \frac{15 \times 5}{600} = 0.125 \text{ kW} \Rightarrow 1.25 \text{ W}$$

$$c \quad \text{Shaft power} = \frac{\text{fluid power}}{\text{efficiency of pump}} = \frac{1.25}{0.294} = 4.2517 \text{ W}$$

General / overall Efficiency

$$= \text{Volumetric eff.} \times \text{hydraulic / mechanical eff.}$$

$$\text{Hydraulic efficiency} = \frac{\text{Theoretical torque}}{\text{Actual torque}}$$

$$\text{Theoretical torque} = \frac{\text{Displacement} \times \text{pressure}}{20\pi} = \frac{10 \times 15}{20 \times 3.142}$$

$$= 2.39 \text{ Nm}$$
$$\text{Hydraulic / mechanical efficiency} = \frac{2.39}{15} = 0.16$$

$$\text{Overall efficiency} = 0.294 \times 0.16 \times 100 = 4.7\%$$