

Yahaya Fawaz Olawole

EEE 326

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ELECT/ELECT

A 25MVA, 415, three phase, 4-pole 60Hz, wye-connected synchronous generator has a synchronous reactance of  $1.5 \Omega$ /phase and negligible stator resistance. The generator is connected to an infinite bus (of constant voltage magnitude and constant frequency) of 415V and 60Hz.

7) Determine the excitation voltage,  $E_a$  when the machine is delivering rated kVA at 0.8 PF lagging.

$$E_a = V_t - j I_a X_s ; V_t = 415V, S = 25000VA = 25000VA$$

$$V_t = \frac{V_l}{\sqrt{3}} = \frac{415}{\sqrt{3}} = 239.6V$$

$$X_s = 1.5 \Omega ; PF = 0.8 \text{ lagging} ; \therefore \theta = \cos^{-1}(0.8) = 36.87^\circ$$

$$I_a = \frac{S}{V_t \sqrt{3}} = \frac{25000}{415 \sqrt{3}} = 34.78A \angle 143.13^\circ$$

$$\therefore E_a = 239.6 - j [34.78 \angle 143.13^\circ] (1.5)$$

$$\Rightarrow E_a = 270.90 + j41.74$$

$$E_a = 274.098 \angle 8.76^\circ$$

8) The field excitation current  $I_f$  is increased by 20% without changing the power input from the prime mover. Find the stator current  $I_a$ , power factor and reactive power  $Q$  applied by the machines.

$$\therefore 20\% \text{ increase} = 1 + 0.2 = 1.2$$

$$\Rightarrow S = 8.76^\circ$$

$$E_a' = 1.2 \times 274.098 = 328.92V$$

$$\therefore \frac{V_t E_a \sin \delta}{X_s} = \frac{V_t E_a' \sin \delta'}{X_s} \quad \therefore \sin \delta' = \frac{E_a \sin \delta}{E_a'}$$

$$\Rightarrow \frac{274.098 \sin 8.76^\circ}{328.92V}$$

$$\sin \delta' = 0.1269 \quad \therefore \delta = \sin^{-1}(0.1269)$$

$$\delta' = 7.29^\circ$$

$$i) \underline{I_A'} = \frac{E_a' - V_t}{jX_s} = \frac{328.92 \angle 7.29^\circ - 239.6 \angle 0^\circ}{j1.5}$$

$$= \frac{328.92 \angle 7.29^\circ - 239.6 \angle 0^\circ}{j1.5} = \frac{27.42 - j57.77}{j1.5}$$

$$ii) \text{ Power factor} = \cos(64.28^\circ) = 0.434 \text{ lagging}$$

$$iii) Q = 3 V_t I_2 \sin \theta = 3 \times 239.6 \times 64.13 \sqrt{\sin(64.28^\circ)} = 41529.65 \text{ VAR}$$

c) With the field excitation current  $I_f$  as in part (a), the input power from the prime mover is increased very slowly. What is the steady state limit? Determine stator current  $I_A$ , power factor and reactive power  $Q$ .

$$\text{At max power } \delta = 90^\circ$$

$$P_{max} = \frac{3 E_a V_t}{X_s} = \frac{3 \times 274.098 \times 239.6}{1.5} = 131347.76 \text{ kW} = 131.347 \text{ MW}$$

$$\underline{I_{Amax}} = \frac{E_a - V_t}{jX_s} = \frac{274.098 \angle 90^\circ - 239.6 \angle 0^\circ}{j1.5} = 249.71 \angle 41.16^\circ$$

$$\text{Power factor} = \cos(41.16^\circ) = 0.7529 \text{ (leading)}$$

$$Q_{max} = 3 V_t I_{Amax} \sin(41.16^\circ) = 3 \times 239.6 \times 242.71 \times 0.6582 = 114929.54 \text{ VAR}$$

$$\underline{\underline{114.829 \text{ kVAR}}}$$