



A three phase, 4 pole, 60 Hz, wye-connected generator has a synchronous reactance negligible stator reactance. The generator is connected to a bus of constant voltage magnitude and frequency of 415 V and 60 Hz.

Find the excitation voltage, E_a when the machine is delivering 25 kW at lagging PF.

$$E_a = V_t - j I_a X_s$$

$$415 = 239.6V$$

$$\sqrt{3}$$

PF = 0.8 lagging, $\theta = \cos^{-1}(0.8) = 36.87^\circ$
 $= \frac{25000}{415 \cdot \sqrt{3}} = 34.78A \angle 143.13^\circ$

$$E_a = 239.6 - j(34.78 \angle 143.13^\circ)(1.5)$$

$$270.90 + j141.74$$

$$274.098V \angle 8.76^\circ$$

If the excitation current I_f is increased by 20% without changing the power input from the prime mover, find the stator current, power factor and reactive power Q applied by the machine.

$$20\% \text{ increase} = 1 + 0.2 = 1.2$$

$$\delta = 8.76^\circ$$

$$E_a' = 1.2 \times 274.098 = 328.92V$$

$$V_t X_s \sin \delta = \frac{V_t E_a' \sin \delta'}{X_s} \therefore \sin \delta' = \frac{E_a \sin \delta}{E_a'} = \frac{274.098}{328.92} = 0.833$$

$$\delta \sin \delta' = 0.1269 \therefore \delta' = \sin^{-1}(0.1269)$$

$$\delta' = 7.29^\circ$$

$$I_a' = \frac{E_a' - V_t}{X_s} = \frac{328.92 \angle 7.29^\circ - 239.6 \angle 0^\circ}{1.5} = 27.82 - j57.77$$

SEPTEMBER						
M	T	W	T	F	S	S
30						1
2	3	4	5	6	7	8
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29

$$I_A' = 64.13A \angle -64.28^\circ$$

ii) Power factor = $\cos(-64.28^\circ) = 0.434$ (lagging)

iii) $Q = 3V_L I_A \sin \theta = 3 \times 239.6 \times 64.13 \times \sin(64.28) = 415 \text{ VAR}$

c) With the field excitation current I_f as in part (a), the input power from the prime mover is increased very slowly. What is the steady state limit. Determine the stator current I_A , power factor and reactive power Q .

At max power $\delta = 90^\circ$.

$$P_{max} = 3 S_A V_t = 3 \times 274.098 \times 239.6 = 131347.7 \text{ W} = 131.347 \text{ kW}$$

$$I_{max} = S_A - V_t = 277.698 \angle 90^\circ - 239.6 \angle 0^\circ = 292.71 \text{ A}$$

Power factor = $\cos(41.16^\circ) = 0.7529$ leading.

$$Q_{max} = 3V_L I_A^{max} \sin(41.16^\circ) = 3 \times 239.6 \times 292.71 \times 0.6582 = 114829.54 \text{ VAR} = 114.829 \text{ kVAR}$$