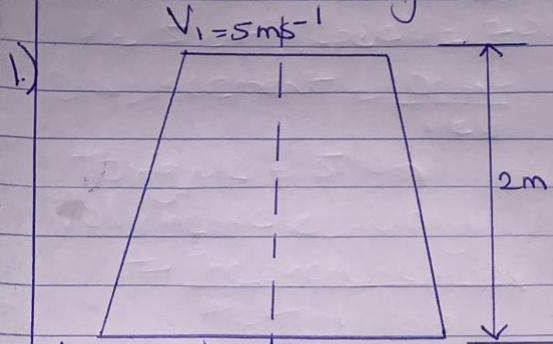


UGBECHIE VALENTINA CHINONSO
18/ENG08/023
BIOMEDICAL ENGINEERING
ENG235
FLUID MECHANICS

UGBECHIE VALENTINA
18/ENG081023

Biomedical Engineering
ENG 235 Assignment



$$V_2 = 2 \text{ ms}^{-1}$$

$$z_1 = 2 \text{ m}$$

$$V_1 = 5 \text{ ms}^{-1}$$

$$V_2 = 2 \text{ ms}^{-1}$$

$$P_1 = 2.5 \text{ m}$$

$$\text{Loss of head } (h_2) = \frac{0.35 (V_1 - V_2)^2}{2g}$$

$$= \frac{0.35 (5 - 2)^2}{2(9.8)}$$

$$h_2 = \frac{3.05}{19.6}$$

$$h_2 = 0.16 \text{ m}$$

Applying Bernoulli's equation for conical tube

$$\frac{P_1}{w} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{w} + \frac{V_2^2}{2g} + z_2 + h_2$$

$$z_1 = 2 \text{ m}$$

$$z_2 = 0 \text{ m}$$

$$\frac{2.5}{2(9.8)} + \frac{5^2}{2(9.8)} + 2 = \frac{P_2}{w} + \frac{2^2}{2(9.8)} + 0 + 0.16$$

$$2.5 + 1.27 + 2 = \frac{P_2}{w} + 0.203 + 0.16$$

$$5.77 = \frac{P_2}{w} + 0.363$$

$$\frac{P_2}{w} = 5.41 - 0.363$$

$$= 5.04 \text{ m}$$

$$\text{head at larger opening} = 5.04 \text{ m}$$

$$2) d_1 = 20 \text{ cm} = 0.2 \text{ m (inlet)}$$

$$A_1 = \frac{\pi d_1^2}{4} = \frac{3.14 \times (0.2)^2}{4}$$

$$= 0.0314 \text{ m}^2$$

$$= 0.03142 \text{ m}^2$$

$$d_2 = 10 \text{ cm} = 0.1 \text{ m (throat)}$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{3.14 (0.1)^2}{4}$$

$$= 0.00785 \text{ m}^2$$

$$C_d = 0.98$$

$$P_1 = 17.658 \text{ N cm}^{-2}$$

$$= 17658 \text{ Nm}^{-2}$$

Vacuum Pressure

$$= 30 \text{ cm Hg} = 0.3 \text{ m Hg}$$

$$Q = ?$$

$$h_1 = \frac{P_1}{\rho g} = \frac{176580}{9.81 \times 1000}$$

$$h_2 = \frac{P_2}{w} = -0.3 \text{ m Hg}$$

$$= (-0.3 \times 13.6) \text{ m H}_2\text{O}$$

$$= -4.08 \text{ H}_2\text{O}$$

$$h = \frac{P_1}{w} - \frac{P_2}{w} = 18 - (-4.08)$$

$$= 22.08 \text{ m}$$

$$Q = C_d A_1 A_2 \sqrt{2gh}$$

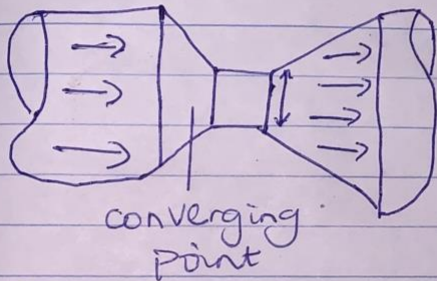
$$Q = \frac{0.98 - 0.03142 - 0.00785}{\sqrt{2 \times 9.81 \times 22.08}}$$

$$\sqrt{0.03142^2 - 0.00785^2}$$

$$Q = \frac{2.42 \times 10^{-9} \times \sqrt{435.2}}{\sqrt{9.26 \times 10^{-9}}}$$

$$Q = \frac{5.037 \times 10^{-3}}{0.0309}$$

$$Q = 0.166 \text{ m}^3 \text{ s}^{-1}$$



$$C_d = 0.69 \quad y = 0.5 \text{ m Hg}$$

$$\Rightarrow d_0 = 15 \text{ cm} = 0.15 \text{ m}$$

$$d_1 = 30 \text{ cm} = 0.3 \text{ m}$$

$$A_0 = \frac{\pi (0.15)^2}{4} = 0.0177 \text{ m}^2$$

$$A_1 = \frac{\pi (0.3)^2}{4} = 0.07 \text{ m}^2$$

$$h = y \left(\frac{\rho_{\text{Hg}}}{\rho_{\text{water}}} - 1 \right)$$

$$= 0.5 \left(\frac{13.6}{1.026} - 1 \right)$$

$$h = 7.65 \text{ m}$$

$$Q = \frac{C_d A_0 \times A_1 \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}}$$

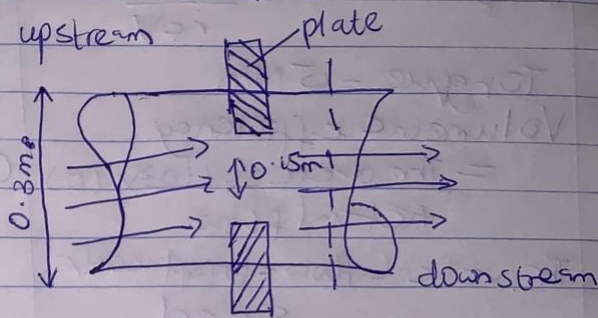
$$Q = \frac{0.69 \times 0.0177 \times 0.07 \times \sqrt{2 \times 9.81 \times 7.65}}{\sqrt{0.07^2 - 0.0177^2}}$$

$$\sqrt{0.07^2 - 0.0177^2}$$

$$Q = \frac{7.9296 \times 10^{-4} \times \sqrt{138.32}}{\sqrt{4.59 \times 10^{-3}}}$$

$$Q = \frac{9.326 \times 10^{-3}}{0.069}$$

$$= 0.137 \text{ m}^3 \text{ s}^{-1}$$



4) Reading from manometer
 $= 170 \text{ mm Hg}$
 $= 0.17 \text{ m Hg}$

Specific gravity of Hg = 13.6

Specific gravity of water = 1.026

$$h = y \left(\frac{\rho_{\text{Hg}}}{\rho_{\text{water}}} - 1 \right)$$

$$h = 0.17 \left(\frac{13.6}{1.026} - 1 \right)$$

$$h = 0.17 (12.26)$$

$$h = 2.084 \text{ m}$$

$$V = \sqrt{2gh}$$

$$= \sqrt{2 \times 9.81 \times 2.084}$$

$$= \sqrt{40.89}$$

$$= 6.39 \text{ m s}^{-1}$$

5) Actual flow rate = $5 \frac{\text{dm}^3}{\text{min}}$
 $= 5 \text{ L/min}$

$P = 15 \text{ bar}$, Speed = 1700 rpm
 Displacement = $\frac{10 \text{ cm}^3}{\text{rev}}$

Torque = 15 Nm
 Volumetric efficiency
 $= \frac{\text{Theoretical flow}}{\text{Actual flow}} \times 100$

Theoretical flow = $\frac{\text{Displacement} \times \text{Speed}}{\text{rev}}$

but $\frac{10 \text{ cm}^3}{\text{rev}} = 0.01 \text{ L/rev}$

Theoretical flow = 0.01×1700
 $= 17 \text{ L/min}$

Volumetric efficiency = $\frac{5 \times 100}{17}$
 $= 29.4\%$

5) Fluid Power = $\frac{\text{Pressure} \times \text{Actual flow}}{600}$

$= \frac{15 \times 5}{600}$
 $= 12.5 \text{ W}$

© Shaft Power = $\frac{\text{Fluid Power}}{\text{Efficiency}}$

$= \text{Volumetric Efficiency} \times \text{Hydraulic Efficiency}$

Hydraulic Efficiency = $\frac{\text{Theoretical Torque}}{\text{Actual Torque}}$

Theoretical Torque

Hydraulic
 $= \frac{(10 \times 15)}{(20 \times 3.14 \times 2)}$
 $\approx 2.39 \text{ Nm}$

Hydraulic Efficiency
 $= \frac{2.39}{15}$

$= 0.16$

Overall Efficiency
 $= 0.294 \times 0.16 \times 100$
 $= 4.7\%$

