

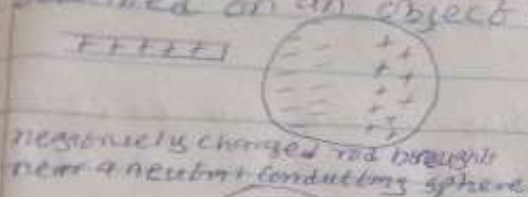
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MATRIC NO: 19/MHS01/010

MBS

COVID-19 Assignments

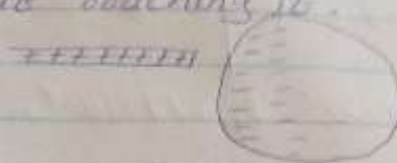
4. Charging by Induction is when electric charges are obtained on an object without touching it.



negatively charged rod brought near a neutral conducting sphere



some of electrons leave the sphere and travel to the sphere



when the rod is removed, the negativity of the sphere induced negative charge remains.

b. $q_1 + q_2 = 5.0 \times 10^{-5} \text{ C}$ $F = 1.0 \text{ N}$ $d = 2 \text{ m}$

$q_2 = 5.0 \times 10^{-5} - q_1$

$F = \frac{k q_1 q_2}{r^2}$

$1 = \frac{9.0 \times 10^9 \times q_1 \times (5.0 \times 10^{-5} - q_1)}{2^2}$

$4 = 4.5 \times 10^{-5} q_1 - 9.0 \times 10^9 q_1^2$

$9.0 \times 10^9 q_1^2 - 4.5 \times 10^{-5} q_1 + 4 = 0$

$q_1 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$= \frac{-(-4.5 \times 10^{-5}) \pm \sqrt{(4.5 \times 10^{-5})^2 - 4 \times 9.0 \times 10^9 \times 4}}{2 \times 9.0 \times 10^9}$

$= \frac{4.5 \times 10^{-5} \pm \sqrt{5.85 \times 10^{10}}}{1.8 \times 10^{10}}$

$= \frac{4.5 \times 10^{-5} \pm 241867.7}{1.8 \times 10^{10}}$ or

$\frac{4.5 \times 10^{-5} - 241867.7}{1.8 \times 10^{10}}$

$q_1 = 3.84 \times 10^{-5} \text{ C}$ or $1.156 \times 10^{-5} \text{ C}$

c. $Q_1 = Q_2 = 8.0 \times 10^{-6} \text{ C}$ $d = 0.5 \text{ m}$ $l = ?$

$l = E = ?$ $x^2 = l^2 + 0.5^2$

$\sqrt{x^2} = \sqrt{1.25}$

$x = 1.12$



$\tan \theta = \frac{1}{0.5}$
 $\theta = \tan^{-1} 2$
 $\theta = 63.4^\circ$

$E_1 = \frac{k q_1}{r^2} = \frac{9.0 \times 10^9 \times 8.0 \times 10^{-6}}{(1.12)^2} = 57397.96 \text{ N/C}$

$E_2 = \frac{k q_2}{r^2} = \frac{9.0 \times 10^9 \times 8.0 \times 10^{-6}}{(1.12)^2} = 57397.96 \text{ N/C}$

$E_y = \frac{k q}{r^2} = 9.0 \times 10^9 \times 8.0 \times 10^{-6} = 9.0 \times 10^4 \text{ N/C}$

vector	θ°	x-component	y-component
E_1	63.4	$E_1 \cos 63.4 = -25700.46$	$E_1 \sin 63.4 = 51322.63$
E_2	63.4	$E_2 \cos 63.4 = 25700.46$	$E_2 \sin 63.4 = 51322.63$
E_y	90	$E_y \cos 90 = 0$	$E_y \sin 90 = 9.0 \times 10^4$
		$\Sigma_x = 0$	$\Sigma_y = 102645.26 + 9.0 \times 10^4$

Magnitude = $\sqrt{(\Sigma_x)^2 + (\Sigma_y)^2}$

$E = \sqrt{0^2 + (102645.26 + 9.0 \times 10^4)^2}$
 since $E = 0$
 $0 = 102645.26 + 9.0 \times 10^4$

$q = \frac{-102645.26}{9.0 \times 10^9}$
 $= -1.14 \times 10^{-5}$

$q = -11.4 \text{ nC}$

2) Electric Field

Electric field intensity

It is a region of space in which an electric charge will experience electric force.

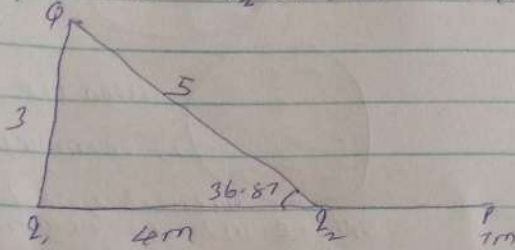
It is force per charge. It is the magnitude of the electric field.

cyclotron frequency $(\omega) = \frac{qB}{m}$

$= \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$

$= 6.147 \times 10^{10} \text{ rad/s}$

b) $q_1 = 8 \times 10^{-7} \text{ C}$ $q_2 = 12 \times 10^{-7} \text{ C}$ $ac = 4 \text{ m}$



$E_1 = \frac{kq_1}{r^2} = \frac{9.0 \times 10^9 \times 8.0 \times 10^{-7}}{3^2} = 1.469 \text{ N/C}$

$E_2 = \frac{kq_2}{r^2} = \frac{9.0 \times 10^9 \times 12 \times 10^{-7}}{4^2} = 12 \text{ N/C}$

net electric field = $12 + 1.469 = 13.47 \text{ N/C}$

H. $E_1 = \frac{kq_1}{r^2} = \frac{9.0 \times 10^9 \times 8.0 \times 10^{-7}}{3^2} = 8 \text{ N/C}$

$E_2 = \frac{kq_2}{r^2} = \frac{9.0 \times 10^9 \times 12 \times 10^{-7}}{4^2} = 10.59 \text{ N/C}$

vector	angle	x-component	y-component
E_1	90°	$E_1 \cos 90 = 0$	$E_1 \sin 90 = 8$
E_2	36.87°	$E_2 \cos 36.87 = 3.456$	$E_2 \sin 36.87 = 2.57$
		$\Sigma x = 3.456$	$\Sigma y = 10.59$

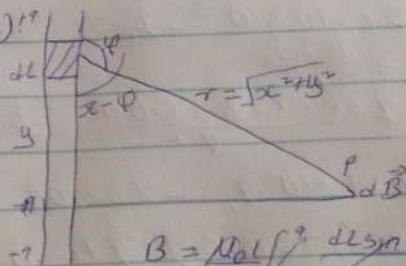
$|E| = \sqrt{3.456^2 + 10.59^2} = 11.14 \text{ N/C}$
 $E = 11.14 \text{ N/C}$
 $\theta = \tan^{-1} \frac{y}{x} = 71.93^\circ$

4.) Magnetic flux is defined as the strength of magnetic field represented by lines of force. It is represented by the symbol Φ

b) $m = 9.11 \times 10^{-31} \text{ kg}$ $r = 1.4 \times 10^{-7} \text{ m}$

$B = 3.5 \times 10^{-1} \text{ T}$ $\theta = 90^\circ$

5a) Bloch-Square 190 states that the magnetic field is directly proportional to the product permeability to free space (μ_0), the current (I), the change in length, the radius and inversely proportional to square of radius (r^2). It can be represented mathematically by $B = \frac{\mu_0 I}{2\pi r}$



$B = \frac{\mu_0 I}{4\pi r} \int_{-\pi/2}^{\pi/2} \frac{dl \sin \theta}{r^2}$

$B = \frac{\mu_0 I}{4\pi r^2} \int_{-\pi/2}^{\pi/2} dl \sin \theta$

$\sin(\pi - \theta) = \sin \theta$

$\therefore B = \frac{\mu_0 I}{4\pi r^2} \int_{-\pi/2}^{\pi/2} dl \sin(\pi - \theta)$

from diagram, $r^2 = x^2 + y^2$ (Pythagoras)

$B = \frac{\mu_0 I}{4\pi r^2} \int_{-\pi/2}^{\pi/2} \frac{dl \sin(\pi - \theta)}{x^2 + y^2}$ --- (K)

But $\sin(\pi - \theta) = \frac{y}{r} = \frac{y}{\sqrt{x^2 + y^2}}$

substituting (K) into (K), we have
 $B = \frac{\mu_0 I}{4\pi} \int_{-\pi/2}^{\pi/2} \frac{dl}{(x^2 + y^2)^{3/2}}$

$B = \frac{\mu_0 I}{4\pi} \int_{-\pi/2}^{\pi/2} dl \frac{y}{(x^2 + y^2)^{3/2}}$

recall $dl = dy$

$B = \frac{\mu_0 I}{4\pi} \int_{-\pi/2}^{\pi/2} \frac{y}{(x^2 + y^2)^{3/2}} dy$ --- (K)

$B = \frac{\mu_0 I}{4\pi} \int_{-\pi/2}^{\pi/2} \frac{1}{(x^2 + y^2)^{3/2}} dy$ --- (K)

using special integral.

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$$\int \frac{dy}{(x^2+y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2+y^2)^{1/2}}$$

Eg 6 (~~xxxx~~) \therefore becomes

$$B = \frac{\mu_0 I c}{450} \left[\frac{y}{x^2(x^2+y^2)^{1/2}} \right]_9^{-9}$$

$$B = \frac{\mu_0 I c}{450} \left(\frac{29}{x^2(x^2+9^2)^{1/2}} \right)$$

$$B = \frac{\mu_0 I}{4500c} \left(\frac{29}{(x^2+9^2)^{1/2}} \right)$$

$$(x^2+9^2)^{1/2} \approx 9,959 \rightarrow \infty$$

$$\therefore B = \frac{\mu_0 I}{2500c}$$