

Example Amosaku Kim

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Sheet 12let
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1 $y = t^3 - \frac{t^2}{2} - 2t + 4$

at stationary point, $\frac{dy}{dt} = 0$

$$\frac{dy}{dt} = 3t^2 - \frac{2t}{2} - 2$$

$$3t^2 - t - 2 = 0$$

$$(3t^2 - 3t) \quad (t - 2)$$

$$3t(t - 1) \quad 2(t - 2)$$

$$(t - 1) \quad (3t - 2)$$

$$t = 1 \quad \text{or} \quad t = \frac{2}{3}$$

ii $\frac{d^2y}{dt^2}$ of stationary point

$$t = 1 \quad \text{or} \quad t = \frac{2}{3}$$

$$y = (1)^3 - \frac{1^2}{2} - 2(1) + 4$$
$$= 1 - \frac{1}{2} - 2 + 4$$

$$= 2.5$$

$$t = \frac{2}{3}$$

$$\left(\frac{2}{3}\right)^3 - \frac{\left(\frac{2}{3}\right)^2}{2} - \frac{4}{3} + 4$$

$$\frac{8}{27} - \frac{4}{9} - \frac{4}{3} + 4$$

$$= \frac{43}{27} \approx 2.51$$

III value of the stationary point

$$\frac{dy}{dx} = 6x - 1$$

$$\begin{aligned} \text{at } x = 1/6 \\ &= 6(1/6) - 1 \\ &= 6 - 1 \\ &= 5 \end{aligned}$$

$$\begin{aligned} \text{at } x = 7/6 \\ &= 6(7/6) - 1 \\ &= 4 - 1 \\ &= 3 \end{aligned}$$

$$2 \quad 2y^2 - 5x^4 - 2 - 7y^3 = 0$$

$$y \frac{d}{dx} (2y^2) + \frac{d}{dx} (-5x^4) - \frac{d}{dx} (2) - \frac{d}{dx} (7y^3)$$

$$4y \frac{dy}{dx} + 20x^3 - 0 - 21y^2 \frac{dy}{dx}$$

$$4y \frac{dy}{dx} + 20x^3 - 0 - 21y^2 \frac{dy}{dx}$$

$$y = 4y \frac{dy}{dx} + 20x^3 - 21y^2 \frac{dy}{dx}$$

$$3 \quad 4x^2 + 2xy^3 - 5y^2 = 0$$

$$\frac{dy}{dx} (4x^2 + 1 \frac{d}{dx} 2xy^3 - \frac{d}{dx} 5y^2) = 0$$

$$8x + 2xy \frac{dy}{dx} + 2y^3 - 10y \frac{dy}{dx} = 0$$

$$2x^3y \frac{dy}{dx} - 10y \frac{dy}{dx} + 8x + 2y^3$$

$$\frac{dy}{dx} (2x^3y - 10y) + 8x + 2y^3 = 0$$

$$\frac{dy}{dx} (2x^3y - 10y) = \frac{-8x - 2y}{(2x^3y - 10y)}$$

$$y' = 1 = \frac{-8(1) - 2(2)}{2(1)^3(2) - 10(2)}$$

$$= \frac{-8 - 4}{12 - 20}$$

$$\frac{-12}{-8} = \frac{3}{2}$$