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CHEM 102 PHY 102

SECTION A

DEPT. MBB8

2. Distinguish between the terms: electric field and electric field intensity

Electric field is a vector, a quantity which has both magnitude and a direction. The electric field intensity is the magnitude of the vector.

The electric field is a region of space in which an electric charge experiences an electric force while electric field intensity is the force per unit charge.

b $Q_1 = 8 \mu C$ $Q_2 = 12 \mu C$ $r = 4m$

i Find the net electric field at a point P on the x-axis at $x = 7m$

$$E_1 = \frac{kq_1}{r^2} = \frac{(9 \times 10^9) \times (8 \times 10^{-9})}{7^2} = 1469387755 \frac{N}{C^2} \frac{N}{C}$$

$$E_2 = \frac{kq_2}{r^2} = \frac{(9 \times 10^9) \times (12 \times 10^{-9})}{3^2} = 12000 \frac{N}{C} \quad 12.0 \frac{N}{C}$$

Vector	Angle	x-component	y-components
$E_1 = 1469387755 \frac{N}{C}$	180°	$1469387755 \times \cos 180$	$1469387755 \times \sin 180$
$E_2 = 12000 \frac{N}{C}$	0°	$12000 \times \cos 0$	$12000 \times \sin 0$
		$E_x = -1346938776$	$E_y = 0$

$$E_{net} = \sqrt{(E_x)^2 + (E_y)^2}$$

$$E_{net} = \sqrt{(-1346938776)^2 + (0)^2}$$

$$E_{net} = 1346938776$$

$$E_{net} \approx 13469 \frac{N}{C}$$

$$E_{net} \approx 13.5 \frac{N}{C}$$

ii) The electric field at a point Q on the y axis at $y = 3\text{m}$ due to the charges

$$E_1 = \frac{kq_1}{r^2} = \frac{(9 \times 10^9) \times (8 \times 10^{-9})}{3^2} = \frac{8000}{9} \text{ N/C} \approx 888.89 \text{ N/C}$$

$$E_2 = \frac{kq_2}{r^2} = \frac{(9 \times 10^9) \times (12 \times 10^{-6})}{5^2} = 4320 \text{ N/C}$$

Vector	Angle	X comp	Y comp
$E_1 = 888.89 \text{ N/C}$	90°	$888.89 \times \cos 90$	$888.89 \times \sin 90$
$E_2 = 4320 \text{ N/C}$	36.9	$4320 \times \cos 36.9$	$4320 \times \sin 36.9$
		$E_x = 3454.637725$	$E_y = 10593.81537$

$$E_{\text{net}} = \sqrt{(E_x)^2 + (E_y)^2}$$

$$E_{\text{net}} = \sqrt{(3454.637725)^2 + (10593.81537)^2}$$

$$= 11142.86525 \text{ N/C}$$

$$\approx 11.1 \text{ N/C}$$

3 Volume Charge Density

This is the measure of quantity of charge per unit volume

$$\rho = \frac{dQ}{dv}$$

$$dQ = \rho \cdot dv$$

Surface Charge Density

This is the measure of how much electric charge is accumulated over a surface

$$\sigma = \frac{dQ}{dA}$$

$$\therefore dQ = \sigma dA$$

Linear Charge Density

This is the measure of a quantity of any characteristic value per unit of length. In other words it is the amount of electric charge per unit length.

$$\therefore \lambda = \frac{dQ}{dl}$$

$$\therefore dQ = \lambda dl$$

II Electric Potential Difference

This is the work done per unit charge against electrical forces, when a charge is transported from one point to another.

$$dW = F dl$$

The force is external

$$\therefore F = -qE$$

$$\therefore dW = -qE \cdot dl$$

The total work done in moving the test charge from

A to B

$$W_{(A \rightarrow B)} = -q_0 \int_A^B E dl$$

$$Q_1 = 10 \mu C$$

$$Q_2 = -2 \mu C$$

$$x = 0$$

$$x = 4m$$

$$V = 9 \times 10^9 \left(\frac{10 \times 10^{-6}}{r_1} + \frac{-2 \times 10^{-6}}{r_2} \right)$$

When $V = 0$

$$0 = \frac{90,000}{r_1} - \frac{18,000}{r_2}$$

$$\frac{90,000}{r_1} = \frac{18,000}{r_2}$$

$$\frac{r_1}{r_2} = \frac{90,000}{18,000}$$

$$\frac{r_1}{r_2} = \frac{5}{1}$$

$$r_1 = 5 \quad r_2 = 1$$

$$\therefore v = 0 \text{ at } x = 5 \text{ m}$$

Section B

4. Magnetic flux can be defined as the strength of magnetic field represented by lines of force

b. $M = 9.11 \times 10^{-31} \text{ kg}$
 $r = 1.4 \times 10^{-7} \text{ m}$

$B = 3.5 \times 10^{-1} \text{ T}$
 $\omega = ?$

$$\omega = \frac{v}{r} = \frac{qB}{m}$$

$$= \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$= 6.147 \times 10^{10} \text{ rad/s}$$

c. Electron moves in a circular orbit with a radius of $1.4 \times 10^{-7} \text{ m}$ with uniform magnetic field of $3.5 \times 10^{-1} \text{ tesla}$ and a perpendicular speed of light to the magnetic field.

The cyclotron frequency of the moving electron can be found by multiplying the charge (1.6×10^{-19}) and the magnetic field ($3.5 \times 10^{-1} \text{ T}$) divided by the mass of the electron ($9.11 \times 10^{-31} \text{ kg}$)

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It is a statement in electromagnetism, the magnetic intensity at any point due to a steady ~~movement~~ current in an infinitely long straight wire is directly proportional to the current and inversely proportional to the distance from point to wire.

$$dB = \frac{\mu_0 I dl}{4\pi r^2}$$

$$dB = \frac{\mu_0 I dl}{4\pi r^2}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \sin \theta$$

$$\sin(\pi - \theta) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int \frac{dl \sin(\pi - \theta)}{r^2}$$

From ~~the~~ Pythagoras's theorem:

$$r^2 = x^2 + y^2$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{x^2 + y^2} \quad \text{--- equ (i)}$$

$$\text{But } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{\frac{1}{2}}} \quad \text{--- equ (ii)}$$

Substitute equ (ii) into equ (i)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{\frac{1}{2}} (x^2 + y^2)^{\frac{1}{2}}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{\frac{3}{2}}}$$

Recall

$$dl = dy$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- eqn (ii)}$$

Using special integrals

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x} - \frac{y}{(x^2 + y^2)^{1/2}}$$

Eqn (ii) therefore becomes

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I x}{4\pi} \left(\frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right)$$

$$B = \frac{\mu_0 I}{4\pi x} \left(\frac{2a}{(x^2 + a^2)^{1/2}} \right)$$

$$(x^2 + a^2)^{1/2} \cong a, \text{ as } a \Rightarrow \infty$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$