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19/MHSE/134

Phy 102 Assignment:

SECTION B

4a. Magnetic flux is defined as the number of magnetic field lines passing through a given surface area.

4b. $m = 9.1 \times 10^{-31} \text{ kg}$ $r = 1.4 \times 10^{-7} \text{ m}$ $\vec{B} = 3.5 \times 10^{-1} \text{ Weber/m}^2$ $q = 1.6 \times 10^{-19} \text{ C}$

$$v = \frac{q r B}{m}$$

$\omega = \text{angular speed} = \text{cyclotron frequency}$

$$\omega = \frac{q B}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.1 \times 10^{-31}}$$

$$\omega = 6.15 \times 10^{10} \text{ rad/s}$$

4c. The cyclotron frequency is $6.15 \times 10^{10} \text{ rad/s}$. It is also known as the same as angular speed. This is because the electron circulates at angular frequency in the type of accelerator called the cyclotron.

[5]

5a. Biot Savart law: ^{a statement:} as the magⁿ in electromagnetism: the magnetic intensity at any point due to a steady current in an infinitely long straight wire is directly proportional to the current and inversely proportional to the distance from point to wire.

5b.
$$B = \frac{\mu_0 I}{4\pi r^2} \int_a^{\pi-a} d\ell \sin \theta$$

$$\sin(\pi - \theta) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{r^2}$$

$$r^2 = x^2 + y^2$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{x^2 + y^2}$$

$$\sin(\pi - \phi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}}$$

Substituting

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

$$dl = dy$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy$$

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right]$$

$$B = \frac{\mu_0 I}{4\pi x} \left(\frac{2a}{(x^2 + a^2)^{1/2}} \right)$$

$(x^2 + a^2)^{1/2} \cong a$ as a approaches infinity

$$B = \frac{\mu_0 I}{2\pi x}$$

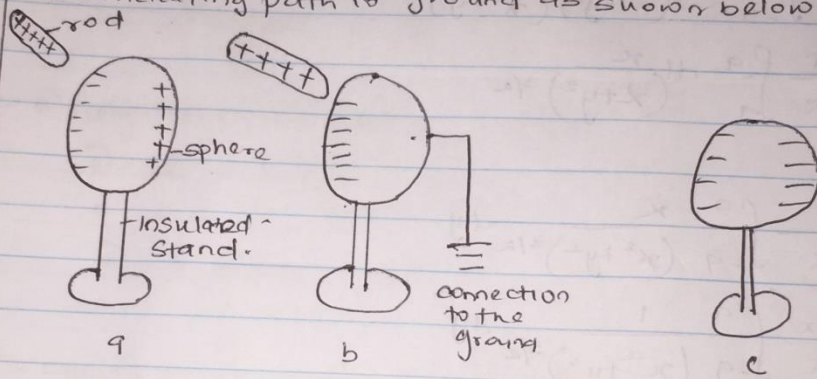
In physical situation, there is axial symmetry on the y -axis. Thus all points in a circle of radius a around the conductor, the

magnitude is $B = \frac{\mu_0 I}{2\pi r}$

∴ It defines the magnitude of the magnetic field of flux density B near along straight carrying conductor.

SECTION A.

1a To produce a negative charged sphere, you have to bring a positively charged rubber rod near a neutral conducting sphere that is insulated so that there is no conducting path to ground as shown below.



1b $q_1 + q_2 = 5.0 \times 10^{-5} \text{ C}$

$F = 1 \text{ N}$ $K = 9.0 \times 10^9$

$r = 2 \text{ m}$

$F = \frac{Kq_1q_2}{r^2}$

~~$1 = \frac{9.0 \times 10^9 \times (q_1q_2)}{2^2}$~~

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$1 = \frac{9.0 \times 10^9 \times (q_1q_2)}{2^2}$

$4 = \frac{9.0 \times 10^9 (q_1q_2)}{9.0 \times 10^9}$

$$4.44 \times 10^{-10} = q_1 q_2$$

$$5.0 \times 10^{-5} = q_1 + q_2$$

$$5.0 \times 10^{-5} = q_2 = q_1$$

Substitute

$$(5.0 \times 10^{-5} - q_2) \times q_2 = 4.44 \times 10^{-10}$$

$$5.0 \times 10^{-5} q_2 - q_2^2 = 4.44 \times 10^{-10}$$

$$q_2^2 - 5.0 \times 10^{-5} q_2 + 4.44 \times 10^{-10} = 0$$

$$q_2 = 3.85 \times 10^{-5} \text{ or } 1.15 \times 10^{-5} \text{ C}$$

$$\text{when } q_2 = 3.85 \times 10^{-5} \quad q_1 =$$

$$q_1 = 5.0 \times 10^{-5} - 3.85 \times 10^{-5}$$

$$q_1 = 1.15 \times 10^{-5} \text{ C}$$

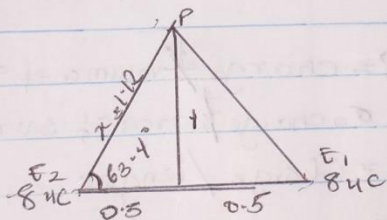
$$\text{when } q_2 = 1.15 \times 10^{-5}$$

$$q_1 = 5.0 \times 10^{-5} - 1.15 \times 10^{-5}$$

$$q_1 = 3.85 \times 10^{-5} \text{ C} //$$

1c. $q_1 = q_2 = 8 \mu\text{C}$

$$d = 0.5 \text{ m}$$



using Pythagoras theorem

$$x^2 = 0.5^2 + 1^2$$

$$x^2 = 0.25 + 1$$

$$x^2 = 1.25$$

$$x = \sqrt{1.25}$$

$$x = 1.12$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{1}{0.5}$$

$$\tan \theta = 2$$

$$\tan^{-1} 2 = \theta$$

$$\theta = 63.4^\circ$$

$$E_1 = E_2 = \frac{kq_1}{r^2} = \frac{9.0 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2}$$

$$E_1 = E_2 = 57397.96$$

$$E_q = \frac{kq_2}{r^2} = \frac{9.0 \times 10^9 \times q}{1} = 9.0 \times 10^9 q$$

Vector	angle	x-comp	y-comp
$E_1 = 57397.96$	63.4	-25200.5	51322.6
$E_2 = 57397.96$	63.4	25200.5	51322.6
$E_q = 9.0 \times 10^9 q$	90°	0	$9.0 \times 10^9 q$
		$\Sigma x = 0$	$\Sigma y = 102645.2 + 9.0 \times 10^9 q$

$$\text{Magnitude} = \sqrt{0^2 + (102645.2 + 9.0 \times 10^9 q)^2}$$

$$0 = 102645.2 + 9.0 \times 10^9 q$$

$$\frac{9.0 \times 10^9 q}{9.0 \times 10^9} = \frac{-102645.2}{9.0 \times 10^9}$$

$$q = 1.14 \times 10^{-5} \text{ C} //$$

3

- 3(a) Volume charge density $= \rho = \frac{\text{charge}}{\text{volume of distribution}} \quad \frac{q}{V}$
- (i) Surface charge density $= \sigma = \frac{\text{charge}}{\text{area of surface}} \quad \frac{q}{A}$
- (ii) Linear charge density $= \lambda = \frac{\text{charge}}{\text{length}} \quad \frac{q}{L}$

(3b) Electric potential difference can be defined as the work done per unit charge against electrical forces when a charge is transported from one place to another.

$$dW = F \cdot dl \quad (1)$$

$$F = -q \cdot E \quad (2)$$

Putting (2) in (1)

$$dW = -q_0 E dl$$

Total work done in moving a test charge from A to B

$$W(A \rightarrow B)_{q_0} = -q_0 \int_A^B E dl \dots (4)$$

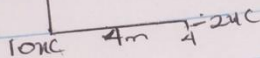
From the definition above

$$V_B - V_A = \frac{W(A \rightarrow B)_{q_0}}{q_0} \dots (5)$$

Putting Eq 4 in 5

$$V_B - V_A = \int_A^B E dl //$$

So $Q_1 = 10 \mu C$ $Q_2 = -2 \mu C$



$$V_p = \frac{1}{4\pi\epsilon_0} \left[\frac{Q_1 + Q_2}{r} \right]$$
$$0 = 9 \cdot 10^9 \left[\frac{10 \times 10^{-6} - 2 \times 10^{-6}}{r} \right]$$
$$0 = 9 \cdot 10^9 \left[\frac{8 \times 10^{-6}}{r} \right]$$

V
distribution
 q/A
 q/L

the
es
to