

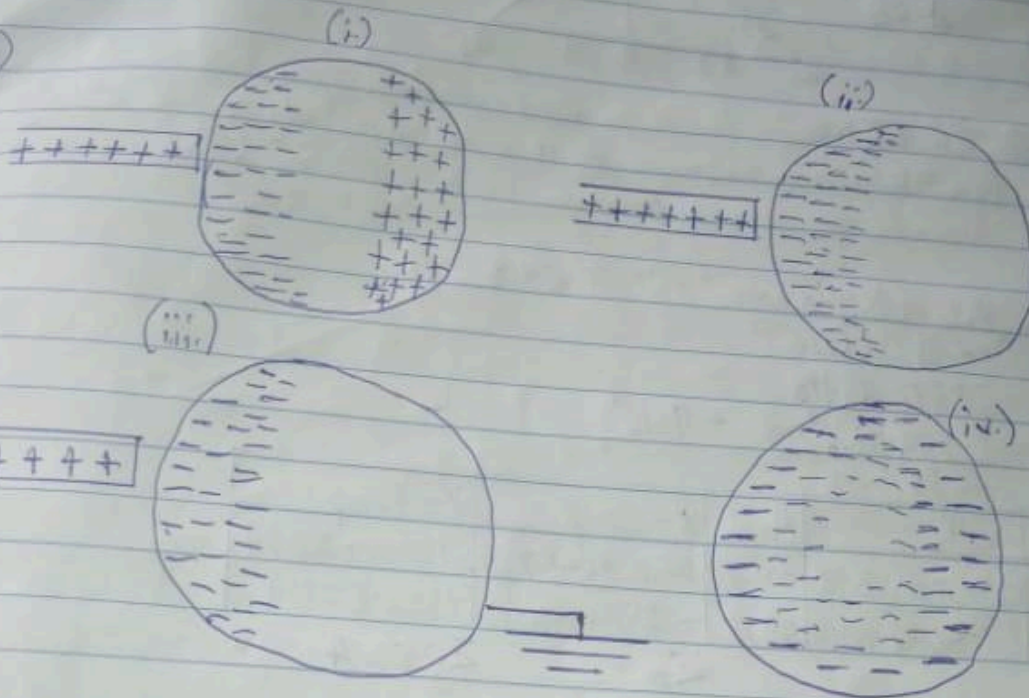
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Phy 102

MBBS

M/MS01/190

1a)



$$b) q_1 + q_2 = 5.0 \times 10^{-5} \text{ C}$$

$$F = \frac{k q_1 q_2}{r^2} \Rightarrow \frac{F r^2}{k} = q_1 q_2$$

where  $F = 1 \text{ N}$ ,  $r = 2 \text{ m}$ ,  $k = 9 \times 10^9$

$$q_1 q_2 = \frac{1 \times 2^2}{9 \times 10^9} = 4.444 \times 10^{-10}$$

$$q_1 + q_2 = 5.0 \times 10^{-5}$$

$$q_2 = 5.0 \times 10^{-5} - q_1$$

$$q_1 (5.0 \times 10^{-5} - q_1) = 4.444 \times 10^{-10}$$

$$q_1^2 - (5.0 \times 10^{-5} q_1) + 4.444 \times 10^{-10} = 0$$

$$5.0 \times 10^{-5} \pm \sqrt{(5.0 \times 10^{-5})^2 - 4(4.444 \times 10^{-10})}$$

2

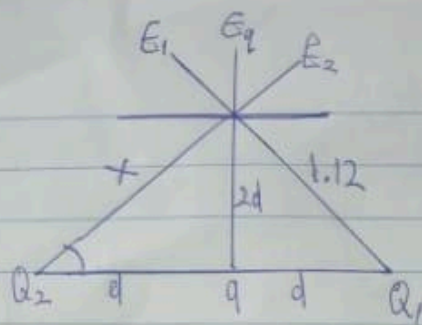
$$q_1 = 3.84 \times 10^{-5} \text{ C}$$

$$q_2 = 5.0 \times 10^{-5} - 3.84 \times 10^{-5}$$

$$q_2 = 1.16 \times 10^{-5} \text{ C}$$

c)

$$d = 0.5$$



$$x^2 = 1^2 + 0.5^2$$

$$\sqrt{x^2} = \sqrt{1.25}$$

$$x = 1.12$$

$$Q_2 = Q_1 = 8 \times 10^{-6}$$

$$E_2 = E_1$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\theta = \tan^{-1} \left( \frac{1}{0.5} \right)$$

$$\theta = 63.43^\circ$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2} = 57397.95918$$

$$E_1 = 57397.95918$$

$$E_q = \frac{kq}{r^2} = \frac{9 \times 10^9 \times q}{1}$$

Vector	Angle	X-Comp	Y-Comp
$E_1 = 57397.95918$	$63.4$	$25700.45785$	$51322.62339$
$E_2 = 57397.95918$	$63.4$	$-25700.45785$	$51322.62339$

$$\sum x = 0$$

$$\sum y = 102645.2568$$

$$E_q = \sqrt{(0)^2 + (102645.2568)^2}$$

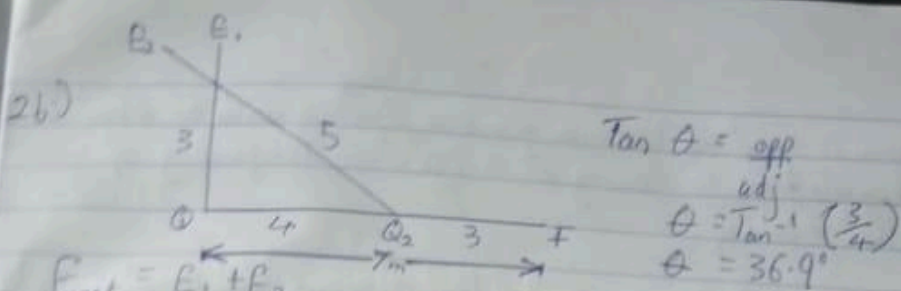
$$E_q = 0 + 102645.2568 = 102645.2568$$

$$q = \frac{E_q}{9 \times 10^9} = \frac{102645.2568}{9 \times 10^9}$$

$$q = 1.14 \times 10^{-5} \text{ C}$$

2a)

- Electric field is a region or space in which an electric charge will experience an electric force.
- Electric field intensity can be defined as the force per unit charge.



$$E_{\text{net}} = E_1 + E_2$$

$$E_1 = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{3^2} = 1.469 \text{ N/C}$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{3^2} = 12 \text{ N/C}$$

$$E_{\text{net}} = 12 + 1.469$$

$$\text{i) } E_{\text{net}} = 13.469 \text{ or } 135 \text{ W/C}$$

$$\text{ii) } E_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{3^2} = 8 \text{ N/C}$$

$$E_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{5^2} = 4.32 \text{ N/C}$$

Vector	Angle	X-Comp	Y-Comp
$E_1 = 8 \text{ N/C}$	$90^\circ$	0	8
$E_2 = 4.32 \text{ N/C}$	$36.9^\circ$	-3.45	2.59

$$\Sigma x = -3.45 \quad \Sigma y = 10.59$$

$$E_{\text{net}} = \sqrt{(-3.45)^2 + (10.59)^2}$$

$$= 11.14 \text{ N/C}$$

$$E_{\text{net}} = 11.14 \text{ N/C}$$

4(a) Magnetic flux is defined as the strength of the magnetic field represented by lines or force.

$$4(b) \quad m = 9.11 \times 10^{-31} \text{ Kg}, \quad r = 1.4 \times 10^{-7}, \quad B = 3.5 \times 10^{-1} \text{ weber/m}^2$$

$$q = -1.6 \times 10^{-19}$$

$$\omega = \frac{qB}{m} = \frac{-1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\omega = -6.15 \times 10^{10} \text{ rad/s}$$

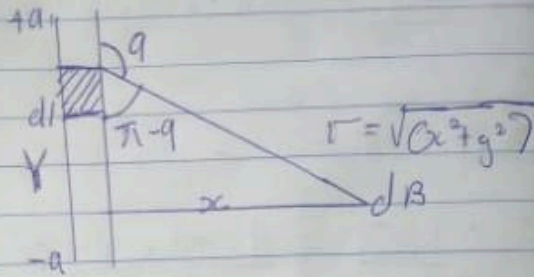
4(c) The arrow is negative because we are dealing with an electron but the electron is moving at a cyclotron frequency of  $6.15 \times 10^{10}$  rad/s.

5(a) The Biot-Savart law is an equation that describes the magnetic field created by a current-carrying wire and allows you to calculate the strength at various points.

$$5(b) B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \theta}{r^2}$$

$$\sin(\pi - \theta) = \sin \theta$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{r^2}$$



From diagram  $r^2 = x^2 + y^2$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{x^2 + y^2} \quad \text{--- (1)}$$

$$\text{but } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- (2)}$$

substituting (2) into (1)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cdot x}{(x^2 + y^2)(x^2 + y^2)^{1/2}} dy$$

$$B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- (3)}$$

Using special integrals:

$$\int \frac{1}{(x^2 + y^2)^{3/2}} dy = \frac{y}{x^2 \sqrt{x^2 + y^2}}$$

Equation (3) becomes

$$B = \frac{\mu_0 I x}{4\pi} \left[ \frac{y}{x^2 \sqrt{x^2 + y^2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I x}{4\pi} \left( \frac{2a}{x^2 \sqrt{x^2 + a^2}} \right)$$

$$B = \frac{\mu_0 I}{4\pi} \left( \frac{2a}{(x^2 + a^2)^{3/2}} \right)$$

$$(x^2 + a^2)^{3/2} \cong a, \text{ as } a \rightarrow \infty$$

$$B = \frac{\mu_0 I}{2\pi x}$$