

$$E_{net} = \sqrt{E_x^2 + E_y^2}$$

$$= \sqrt{13.5^2 + 0^2}$$

$$= \sqrt{182.25}$$

$$= 13.5 \text{ N/C}$$

$$E_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{3^2} = \frac{72}{9} = 8 \text{ N/C}$$

$$E_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{5^2} = \frac{108}{25} = 4.32 \text{ N/C}$$

Vector	Angle	X-component	Y-component
$E_1 = 8 \text{ N/C}$	$90^\circ$	$E_1 = 8 \cos 90^\circ = 0 \text{ N/C}$	$E_1 = 8 \sin 90^\circ = 8 \text{ N/C}$
$E_2 = 4.32 \text{ N/C}$	$36.86^\circ$	$E_2 = 4.32 \cos 36.86^\circ = 3.45 \text{ N/C}$	$E_2 = 4.32 \sin 36.86^\circ = 2.59 \text{ N/C}$
		$\Sigma E_x = 3.45 \text{ N/C}$	$\Sigma E_y = 10.59 \text{ N/C}$

$$E_{net} = \sqrt{\Sigma E_x^2 + \Sigma E_y^2}$$

$$= \sqrt{(3.45)^2 + (10.59)^2}$$

$$= \sqrt{11.9 + 112.14}$$

$$= \sqrt{124.04}$$

$$= 11.13 \text{ N/C}$$

3 Volume charge density,  $\rho = \frac{dQ}{dV} \rightarrow dQ = \rho dV$

i) Surface charge density,  $\sigma = \frac{dQ}{dA} \rightarrow dQ = \sigma dA$

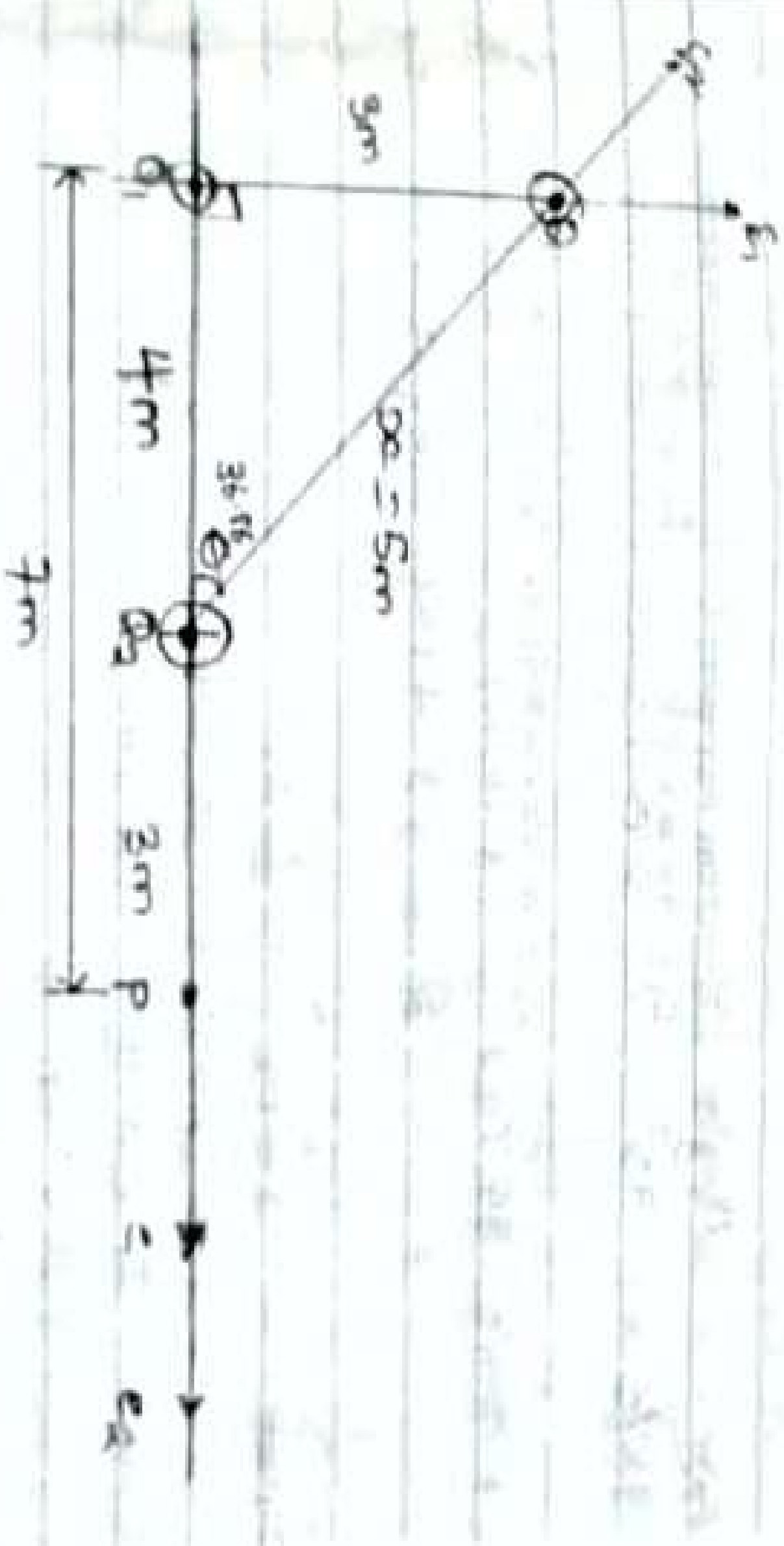
ii) Linear charge density,  $\lambda = \frac{dQ}{dL} \rightarrow dQ = \lambda dL$

Where:  
 $Q$  = charge,  $V$  = volume,  $L$  = length,  $A$  = Area

b) Electrica potential difference between two points in an electric field can be defined as the workdone per unit charge against electrical forces when a charge is transported

2a. Electric field is a region of space in which an electric charge will experience an electric force while electric field intensity is defined as the force per unit charge

b)  $Q_1 = 8 \text{ nC}$  ,  $Q_2 = 12 \text{ nC}$



$$E_1 = \frac{kQ_1}{r_1^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{4^2} = \frac{32}{4} = 8 \text{ N/C}$$

$$= 1.469 \text{ N/C} \approx 1.5 \text{ N/C}$$

$$E_2 = \frac{kQ_2}{r_2^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{9} = \frac{108}{9} = 12 \text{ N/C}$$

Vector	Angle	X-component	Y-component
$E_1 = 1.5 \text{ N/C}$	$0^\circ$	$E_1 = 1.5 \cos 0^\circ = 1.5 \text{ N/C}$	$E_1 = 1.5 \sin 0^\circ = 0 \text{ N/C}$
$E_2 = 12 \text{ N/C}$	$0^\circ$	$E_2 = 12 \cos 0^\circ = 12 \text{ N/C}$	$E_2 = 12 \sin 0^\circ = 0 \text{ N/C}$
		$\Sigma E_x = 13.5$	$\Sigma E_y = 0$

From one point to the other. It is measured in Volt (V) or Joule per coulomb (J/C) and it is a scalar quantity.

$$V = \text{Workdone} / \text{Charge} \quad (2)$$

$$\text{Workdone} = q \times V$$

— due to a single point charge  $q$

$$V_B - V_A = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{r_B} - \frac{1}{r_A} \right]$$

Where,  $q$  = point charge

$r_B$  = distance of  $Q$  to point B

$r_A$  = distance of  $Q$  to point A

— due to a several point charge

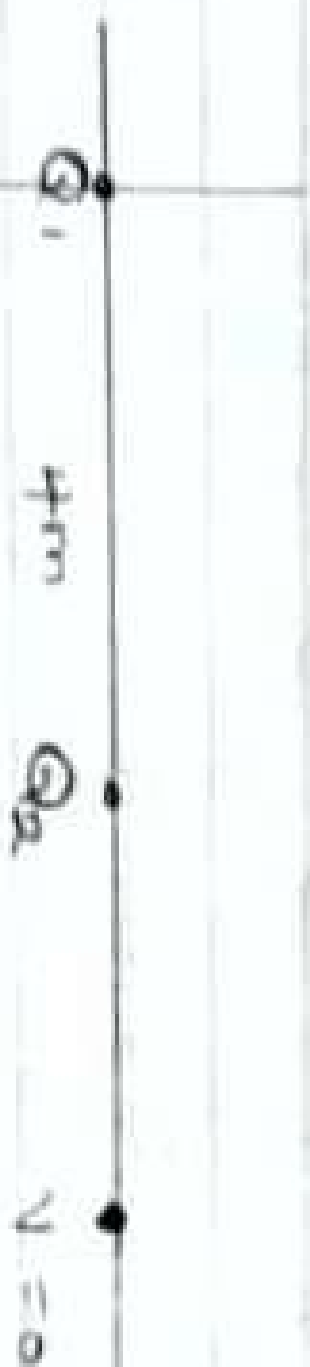
$$V_p = \frac{1}{4\pi\epsilon_0} \left[ \frac{Q_1}{r_1} \right] + \left[ \frac{Q_2}{r_2} \right]$$

Where  $V$  = Electric potential

$Q$  = point charge

$r$  = distance of  $Q$

2c)



$$V_p = \frac{1}{4\pi\epsilon_0} \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$0 = \frac{1}{4\pi\epsilon_0} \left[ \frac{9 \times 10^{-9}}{x} + \frac{-2 \times 10^{-6}}{x-4} \right]$$

$$V_p = k \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$V_p = 9 \times 10^9 \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = 9 \times 10^9 \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x}$$

$$= \frac{10 \times 10^{-6}}{4+x} - \frac{2 \times 10^{-6}}{x}$$

$$(10 \times 10^{-6})x = (4+x)(-2 \times 10^{-6})$$

$$8 \times 10^{-6} = 10 \times 10^{-6} \cos \theta - 2 \times 10^{-6} \sin \theta$$

$$8 \times 10^{-6} = 8 \times 10^{-6} \cos \theta$$

$$\cos \theta = \frac{8 \times 10^{-6}}{8 \times 10^{-6}}$$

$$\cos \theta = 1$$

position along the x-axis is 1m

$$V = k \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$0 = \left[ \frac{10 \times 10^{-6}}{4} + \frac{-2 \times 10^{-6}}{\infty} \right]$$

$$\frac{2 \times 10^{-6}}{\infty} = 10 \times 10^{-6}$$

$$(4 - \infty) (2 \times 10^{-6}) = (10 \times 10^{-6}) \infty$$

$$8 \times 10^{-6} - 2 \times 10^{-6} \infty = 10 \times 10^{-6} \infty$$

$$8 \times 10^{-6} = 10 \times 10^{-6} \infty + 2 \times 10^{-6} \infty$$

$$\infty = \frac{8 \times 10^{-6}}{12 \times 10^{-6}}$$

$$\infty = 0.67 \text{m}$$

position of V is 0.67m

### Section B

4) Magnetic flux is defined as the number of magnetic field lines passing through a given closed surface.

$$\Phi_B = B \cdot A = BA \cos \theta$$

15) Data:

$$m_e = 9.11 \times 10^{-31} \text{ kg}$$

$$r = 1.4 \times 10^{-7} \text{ m}$$

$$B = 3.5 \times 10^{-1} \text{ Weber/m}^2$$

Cyclotron frequency = Angular speed

$$\omega = 1.6 \times 10^8$$

$$f_B = \frac{2\pi V B}{r}$$

$$M_e V = 2BR$$

$$V = \frac{2BR}{M_e}$$

$$V = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-31} \times 1.4 \times 10^{-7}}{9.11 \times 10^{-31}}$$

$$= \frac{7.84 \times 10^{-27}}{9.11 \times 10^{-31}}$$

$$= 8605.9 \text{ m/s}$$

$$M = v = 2B = \frac{1.6 \times 10^{-19} \times 3.6 \times 10^{-21}}{9.11 \times 10^{-31}}$$

$$M = \frac{5.76 \times 10^{-20}}{9.11 \times 10^{-31}} = 6.14 \times 10^{10} \text{ e}^{-1}$$

14c) In 4b we were given parameters:  $M_e$  mass of electron as  $9.11 \times 10^{-31} \text{ kg}$ , radius as  $1.4 \times 10^{-7} \text{ m}$ ,  $B = 3.5 \times 10^{-31} \text{ Weber/m}^2$ . Asked to find the cyclotron frequency also known as angular speed. It is cyclotron frequency because it is frequency of an oscillation called CYCLOTRON.

Recall  $M = \text{Angular speed}$

$$M = \frac{2B}{M_e}$$

Since Cycle from frequency = Angular Speed  
The cyclotron frequency =  $6.14 \times 10^{10} \text{ e}^{-1}$  having a unit of  $f$  which is the unit of frequency dimensionally.

5a) Biot-Savart Law state that is an equation that describes the magnetic field created by a current-carrying wire and allows you to calculate its strength at various points.



b) Magnetic field of a straight current carrying conductor

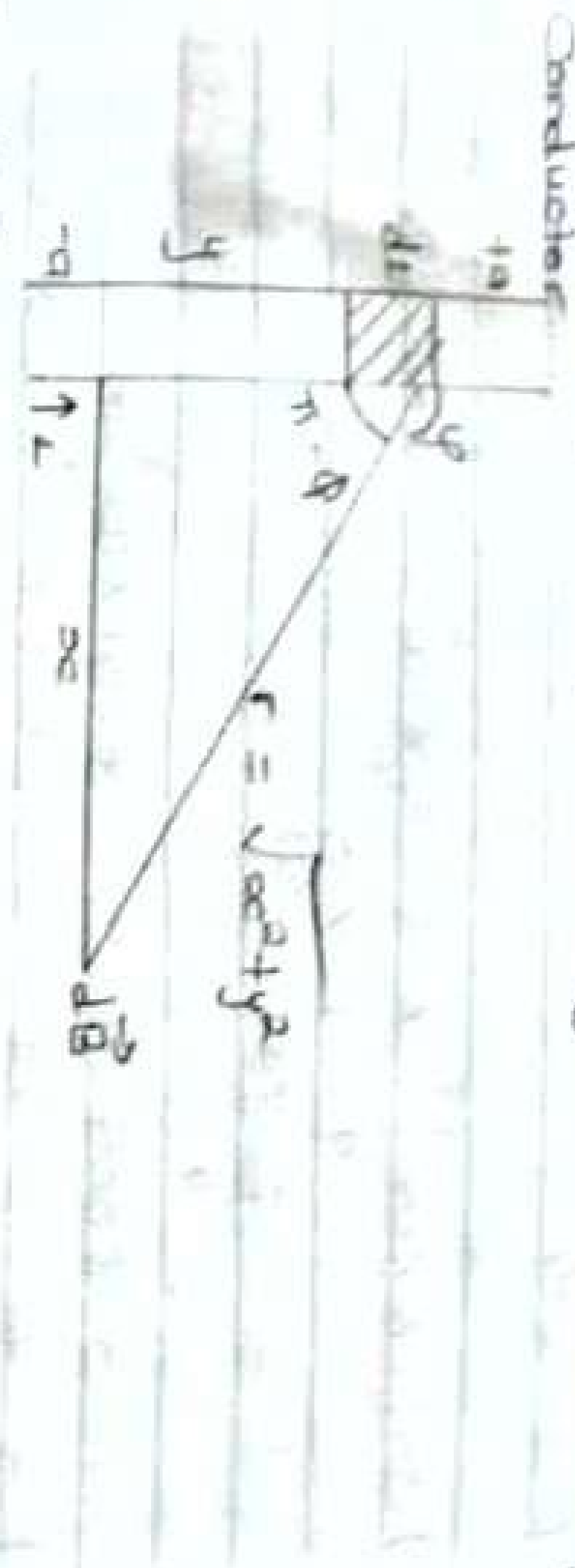


Fig 1: A section of straight current carrying conductor

Applying the Biot-savart law, we find the magnitude of the field  $d\vec{B}$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \theta}{r^2}$$

$$\sin(\pi - \theta) = \sin \theta$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{r^2} \quad \text{--- (1)}$$

From the diagram  $r^2 = x^2 + y^2$   
 But  $\sin(\pi - \theta) = \frac{y}{\sqrt{x^2 + y^2}}$  --- (2)

Substitute (2) into (1)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl}{\sqrt{x^2 + y^2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl}{\sqrt{x^2 + y^2}}$$

$$dl = dy \quad B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{\sqrt{x^2 + y^2}} dy \quad \text{--- (3)}$$

$$\int \frac{dy}{\sqrt{x^2 + y^2}} = \frac{1}{x} \frac{y}{\sqrt{x^2 + y^2}}$$

$$B = \frac{\mu_0 I}{4\pi x} \left( \frac{2a}{\sqrt{x^2 + a^2}} \right) = \frac{\mu_0 I}{2\pi x} \frac{a}{\sqrt{x^2 + a^2}}$$

$$B = \frac{\mu_0 I}{2\pi x}$$